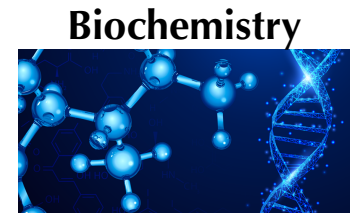
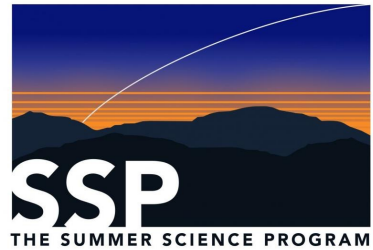


A COSMIC TEST OF QUANTUM ENTANGLEMENT

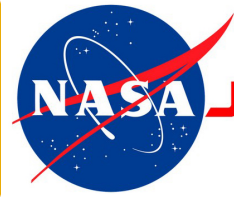
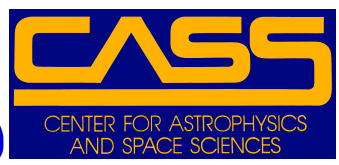
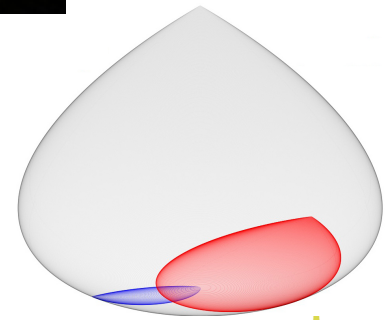
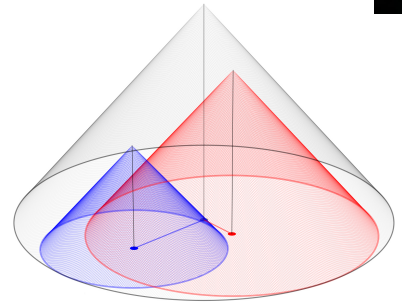


Dr. Andrew Friedman

UC San Diego

Center for Astrophysics and Space Sciences

<https://asfriedman.physics.ucsd.edu> asf@ucsd.edu



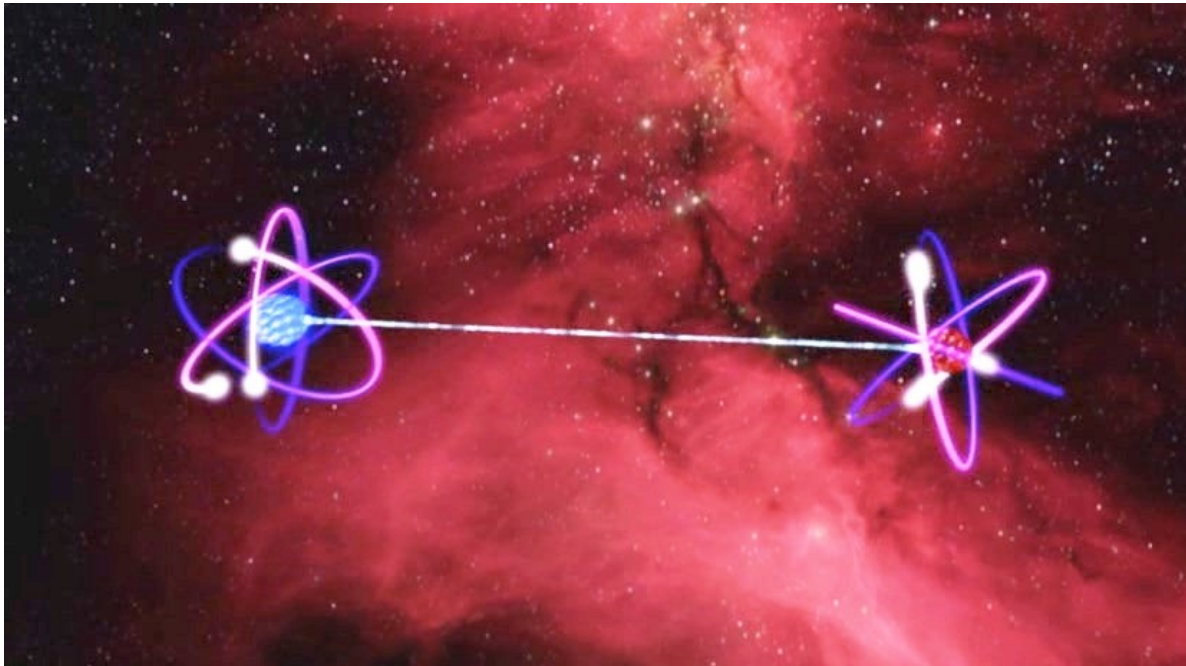
7/19/2019

Summer Science Program, UC San Diego

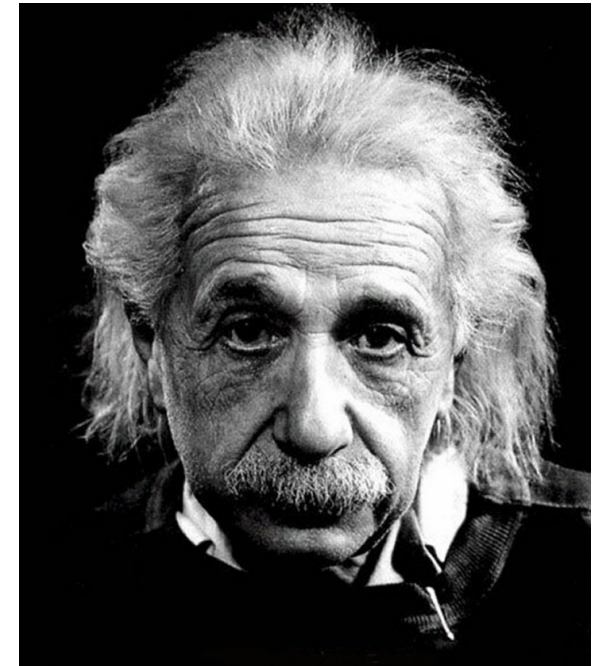
QUANTUM ENTANGLEMENT 101

Entanglement: Paired systems with correlated (or anti-correlated) properties

Measure #1, instantly know something about #2
Systems are **NOT** independent!



<https://kuleuvenblogt.files.wordpress.com/2014/06/entangled-atoms.jpg>



<http://xeon24.com/data/wallpapers/2/508769-albert-einstein.jpg>

Is quantum mechanics complete or just spooky?

COSMIC BELL TESTS

Milky Way Stars (2017)



High Redshift Quasars (2018)

The Canary Island of La Palma



SSP 2011 NEW MEXICO TECH



SSP 2011 NEW MEXICO TECH





Cosmic Bell Test: Measurement Settings from Milky Way Stars

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 Bo Liu,^{1,4} Hannes Hosp,¹ Johannes Kofler,⁵ David Bricher,¹ Matthias Fink,¹ Calvin Leung,³
 Anthony Mark,² Hien T. Nguyen,⁶ Isabella Sanders,² Fabian Steinlechner,¹ Rupert Ursin,^{1,7}
 Sören Wengerowsky,¹ Alan H. Guth,² David I. Kaiser,²
 Thomas Scheidl,¹ and Anton Zeilinger^{1,7,‡}

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(Received 21 November 2016; revised manuscript received 13 January 2017; published 7 February 2017)

Bell's theorem states that some predictions of quantum mechanics cannot be reproduced by a local-realist theory. That conflict is expressed by Bell's inequality, which is usually derived under the assumption that there are no statistical correlations between the choices of measurement settings and anything else that can causally affect the measurement outcomes. In previous experiments, this “freedom of choice” was addressed by ensuring that selection of measurement settings via conventional “quantum random number generators” was spacelike separated from the entangled particle creation. This, however, left open the possibility that an unknown cause affected both the setting choices and measurement outcomes as recently as mere microseconds before each experimental trial. Here we report on a new experimental test of Bell's inequality that, for the first time, uses distant astronomical sources as “cosmic setting generators.” In our tests with polarization-entangled photons, measurement settings were chosen using real-time observations of Milky Way stars while simultaneously ensuring locality. Assuming fair sampling for all detected photons, and that each stellar photon's color was set at emission, we observe statistically significant $\gtrsim 7.31\sigma$ and $\gtrsim 11.93\sigma$ violations of Bell's inequality with estimated p values of $\lesssim 1.8 \times 10^{-13}$ and $\lesssim 4.0 \times 10^{-33}$, respectively, thereby pushing back by ~ 600 years the most recent time by which any local-realist influences could have engineered the observed Bell violation.

COSMIC BELL TEAM



**Prof. David
Kaiser** ¹



**Dr. Andrew
Friedman** ^{1,5}



**Prof. Alan
Guth** ¹



**Prof. Brian
Keating** ⁵



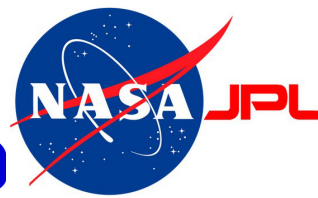
**Prof. Anton
Zeilinger** ²



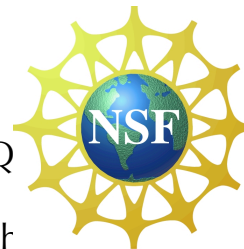
**Prof. Jason
Gallicchio** ³

Other Collaborators

Johannes Handsteiner ²,
Dominik Rauch ²,
Dr. Thomas Scheidl ²,
Dr. Johannes Kofler ⁴,
Dr. Hien Nguyen ⁶,
David Leon ⁵,
Calvin Leung ³
et al.



- 1: MIT Physics/CTP
- 2: Vienna IQOQI
- 3: Harvey Mudd
- 4: Max Planck MPQ
- 5: UCSD CASS
- 6: NASA JPL/Caltech



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Isabella Sanders, Anthony Mark



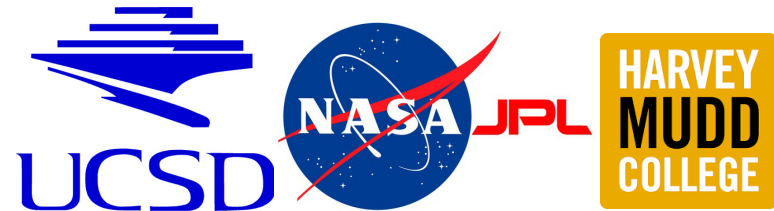
**Prof. Brian
Keating** ⁵



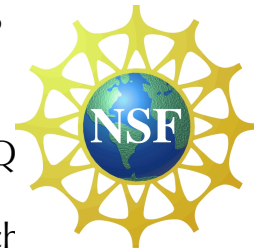
**Prof. Anton
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COSMIC BELL TEAM



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Isabella Sanders, Anthony Mark



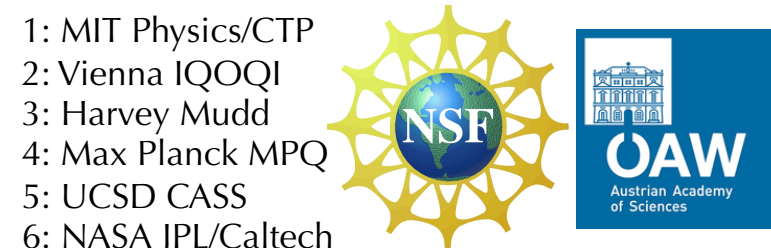
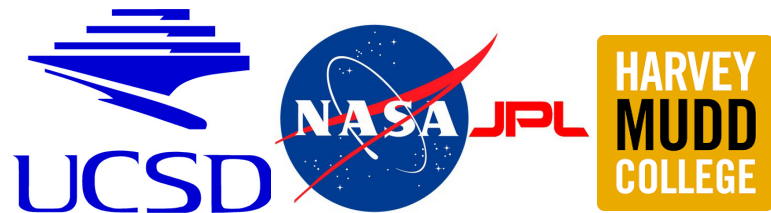
**Prof. Brian
Keating** ⁵



**Prof. Anton
Zeilinger** ²



**Prof. Jason
Gallicchio** ³



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- 4: Max Planck MPQ
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- 6: NASA JPL/Caltech

BACK OF THE ENVELOPE



11/23/12 $x_L = x_B - r_C$ Not true at 90°? $? r_C, x_{ab}$ $x_L = \sqrt{x_a^2 + x_b^2 - 2x_a x_b \cos \alpha}$ $\alpha + \delta + \delta = \pi$

$x_{ab} = \sqrt{x_b^2 + (r_B - r_C)^2 - 2r_B(r_B - r_C) \cos \delta}$ δ, δ unk.
 r_C, x_{ab} unk.
 \uparrow Eq. + unk.

$x_{ab} = \sqrt{x_a^2 + (r_B - r_C)^2 - 2x_a(r_B - r_C) \cos \delta}$ \uparrow Eq. + unk.

$x_B^2 = \sqrt{x_a^2 + x_L^2 - 2x_a x_L \cos \delta}$ \uparrow Eq. + unk.
 x_a, x_b
 r_a, r_b

$x_a^2 = \sqrt{x_b^2 + x_L^2 - 2x_b x_L \cos \delta}$ x_L

$x_L = r_B + r_C - 2r_C$

Solve for $\cos \delta, \cos \delta$

$x_a^2 = x_b^2 + x_L^2 - 2x_b x_L \cos \delta \Rightarrow 2x_b x_L \cos \delta = x_b^2 + x_L^2 - x_a^2$

$\cos \delta = \frac{x_b^2 - x_a^2 + (x_a^2 + x_b^2 - 2x_a x_b \cos \alpha)}{2x_b x_L} = \frac{2x_b^2 - 2x_a x_b \cos \alpha}{2x_b x_L} = \frac{x_b [x_b - x_a \cos \alpha]}{x_L}$

$\cos \delta = \frac{x_b - x_a \cos \alpha}{\sqrt{x_a^2 + x_b^2 - 2x_a x_b \cos \alpha}}$ $\cos \delta = \frac{x_a - x_b \cos \alpha}{\sqrt{x_a^2 + x_b^2 - 2x_a x_b \cos \alpha}}$ $\cos \delta = \frac{x_b - x_a \cos \alpha}{x_L}$ $\cos \delta = \frac{x_a - x_b \cos \alpha}{x_L}$

$x_b^2 = x_a^2 + x_L^2 - 2x_a x_L \cos \delta \Rightarrow 2x_a x_L \cos \delta = x_a^2 - x_b^2 + x_L^2 = x_a^2 - x_b^2 + x_a^2 + x_b^2 - 2x_a x_b \cos \alpha$

$\cos \delta = \frac{2x_a^2 - 2x_a x_b \cos \alpha}{2x_a x_L} = \frac{2x_a [x_a - x_b \cos \alpha]}{2x_a x_L} = \frac{x_a - x_b \cos \alpha}{x_L} = \cos \delta$

$x_b^2 + (r_B - r_C)^2 - 2x_b(r_B - r_C) \cos \delta = x_a^2 + (r_B - r_C)^2 - 2x_a(r_B - r_C) \cos \delta$ $? r_C$

$x_L = r_B - r_C + r_C - r_C = r_B + r_C - 2r_C \Rightarrow 2r_C = r_B + r_C - x_L$ $x_L = r_B + r_C - 2r_C$

$r_C = \frac{1}{2} [r_B + r_C - x_L]$ $r_C = \frac{1}{2} [r_B + r_C - \sqrt{x_a^2 + x_b^2 - 2x_a x_b \cos \alpha}]$

$x_{ab} = \sqrt{x_b^2 + (r_B - r_C)^2 - 2x_b(r_B - r_C) \cos \delta} = \sqrt{x_b^2 + x_L^2 - 2x_b x_L \cos \delta}$

$r_B - r_C = x_L - (r_C - r_C)$ $r_C - r_C = x_b - (r_B - r_C)$

COSMIC BELL TEST ON TV!



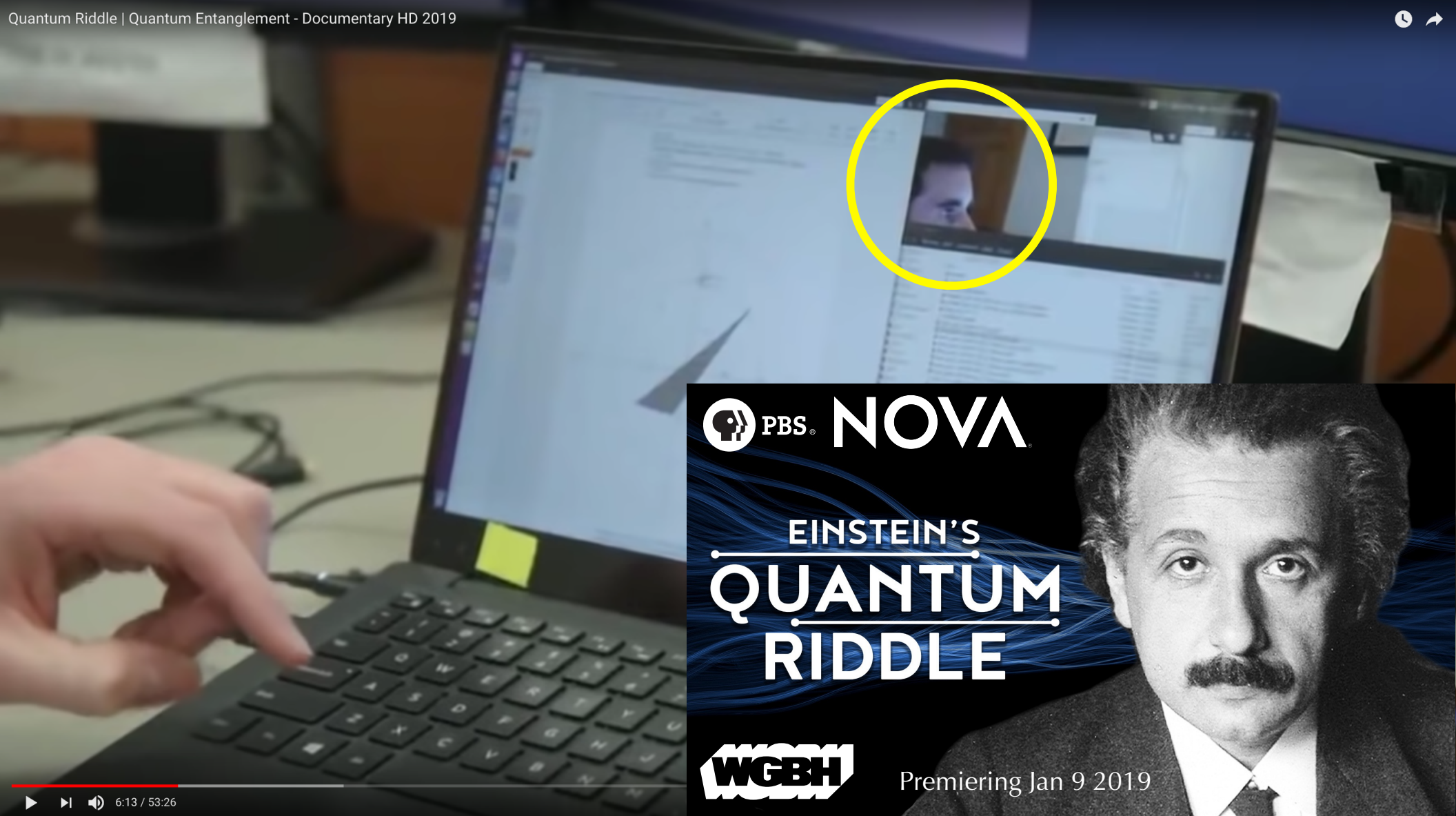
EINSTEIN'S
QUANTUM
RIDDLE



Premiering Jan 9 2019

3 SECONDS OF FAME!

Quantum Riddle | Quantum Entanglement - Documentary HD 2019



Einstein's Quantum Riddle, PBS NOVA, Season 46, Episode 2, 6:12-6:15

7/19/2019

Summer Science Program, UC San Diego

12

FEYNMAN ON FREE WILL

“We have an illusion that we can do any experiment that we want. We all, however, come from the same universe, have evolved with it, and don't really have any `real' freedom. For we obey certain laws and have come from a certain past. Is it somehow that we are correlated to the experiments that we do, so that the apparent probabilities don't look like they ought to look if you assume they are random...”

– **Richard Feynman 1982**

OUTLINE

1. Entanglement Tests

2. Bell's Inequality vs. Bell's Theorem

3. Loopholes / Freedom-Of-Choice Loophole

4. Cosmic Bell Test with Milky Way Stars

5. Cosmic Bell Test with Quasars

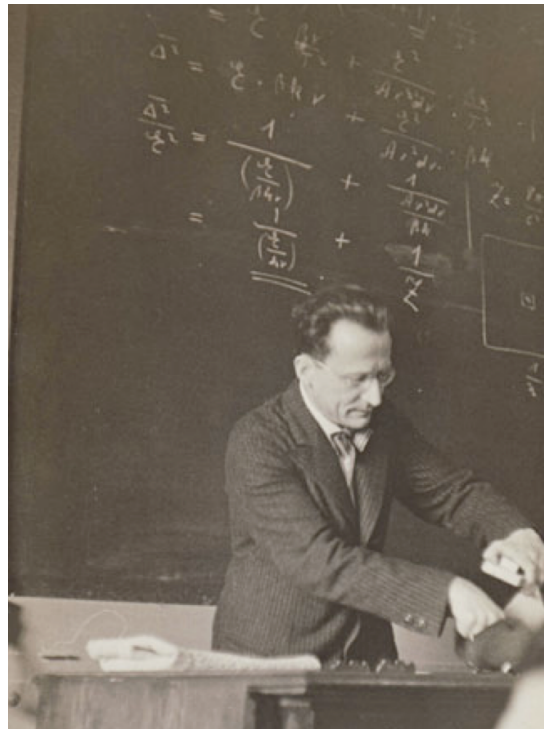
6. Future Tests

QUANTUM ENTANGLEMENT

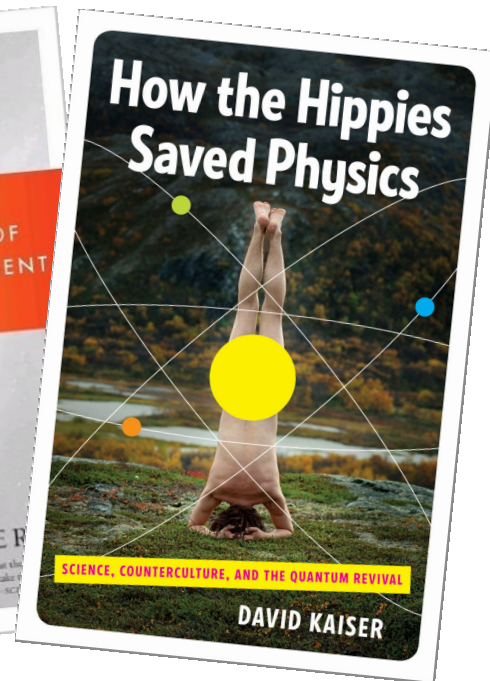
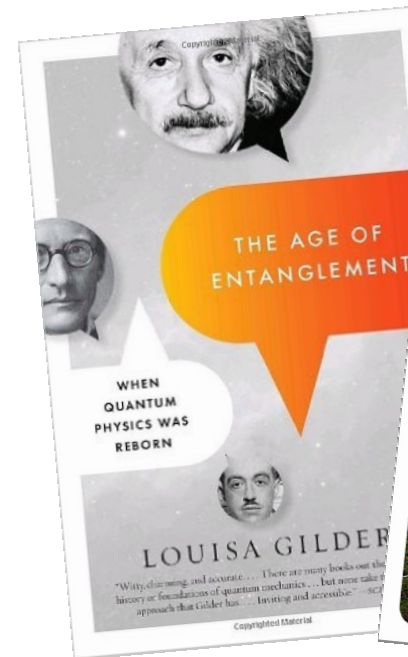
Beginning in the 1930s, the great architects of quantum theory struggled to understand the notion of “entanglement.”



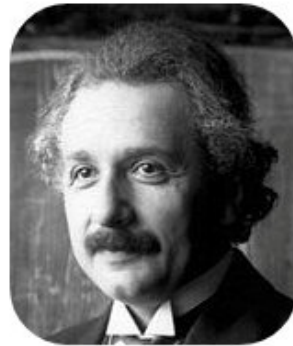
Niels Bohr and Albert Einstein



Erwin Schrödinger



EPR PARADOX AND HIDDEN VARIABLES



A. Einstein

E



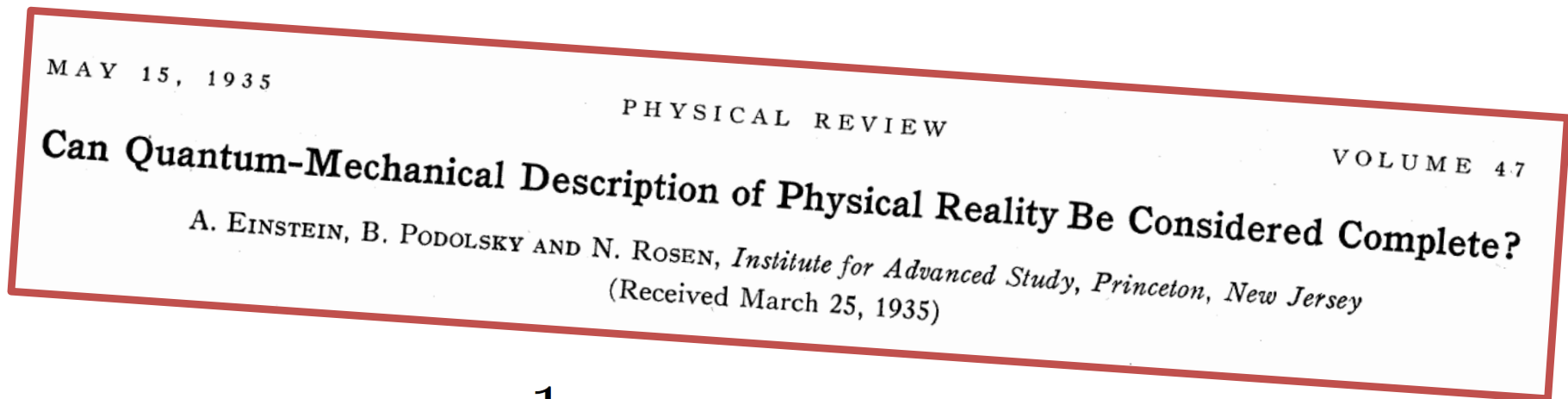
B. Podolsky

P



N. Rosen

R

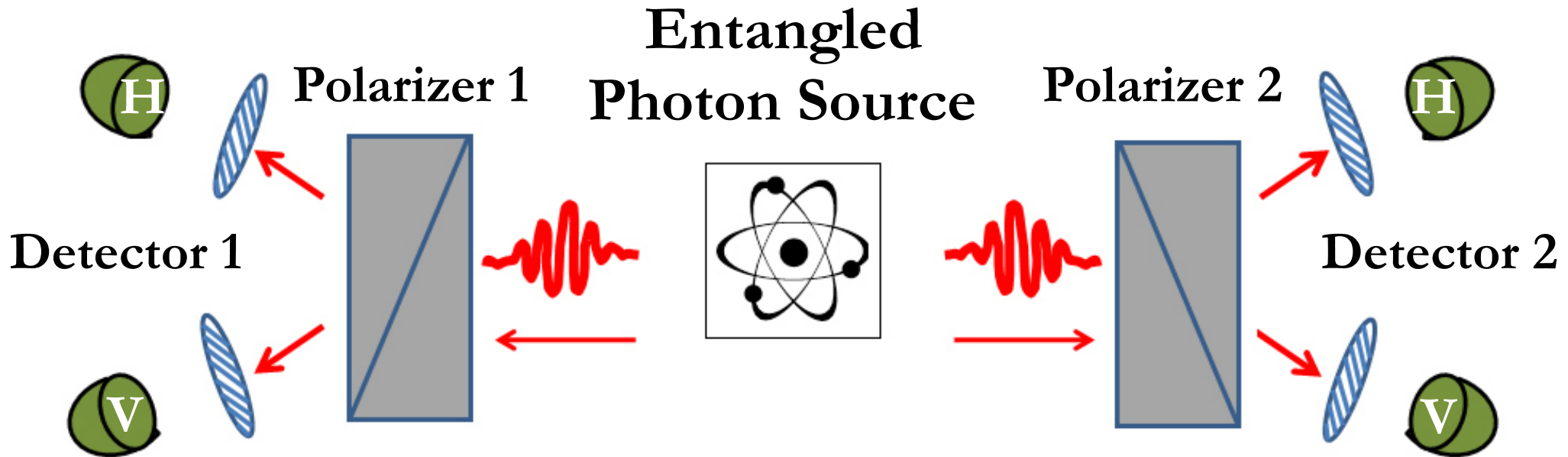


$$|\psi\rangle = \frac{1}{\sqrt{2}} \left\{ |u_1\rangle |v_2\rangle + |u_2\rangle |v_1\rangle \right\}$$

State does not factorize: no way to describe behavior of particle 1 (u) without referring to behavior of particle 2 (v).

ENTANGLED PARTICLE EXPERIMENTS

“Bell Test”



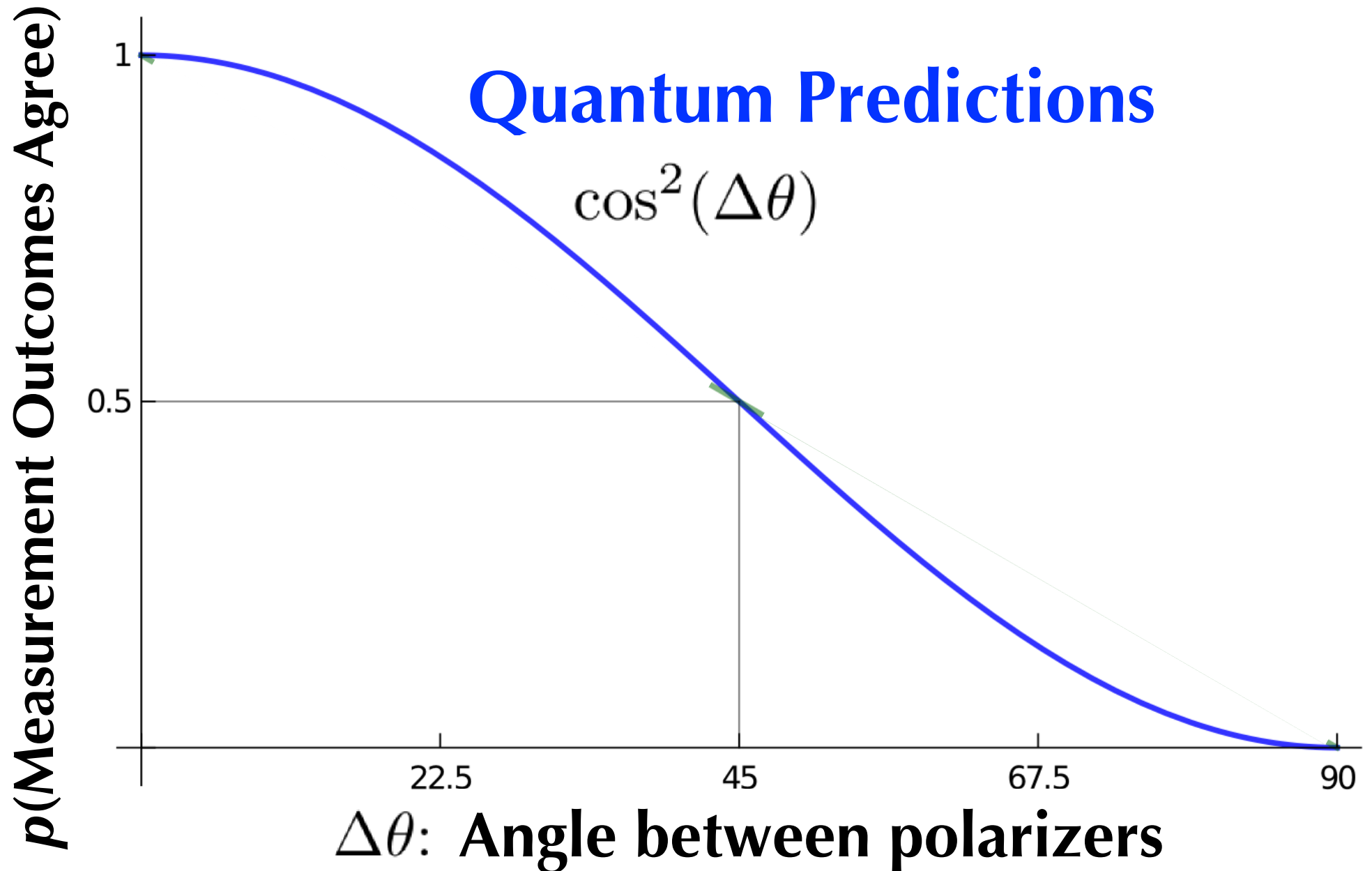
Can rotate polarizers

Same direction: same outcome (HH, VV)

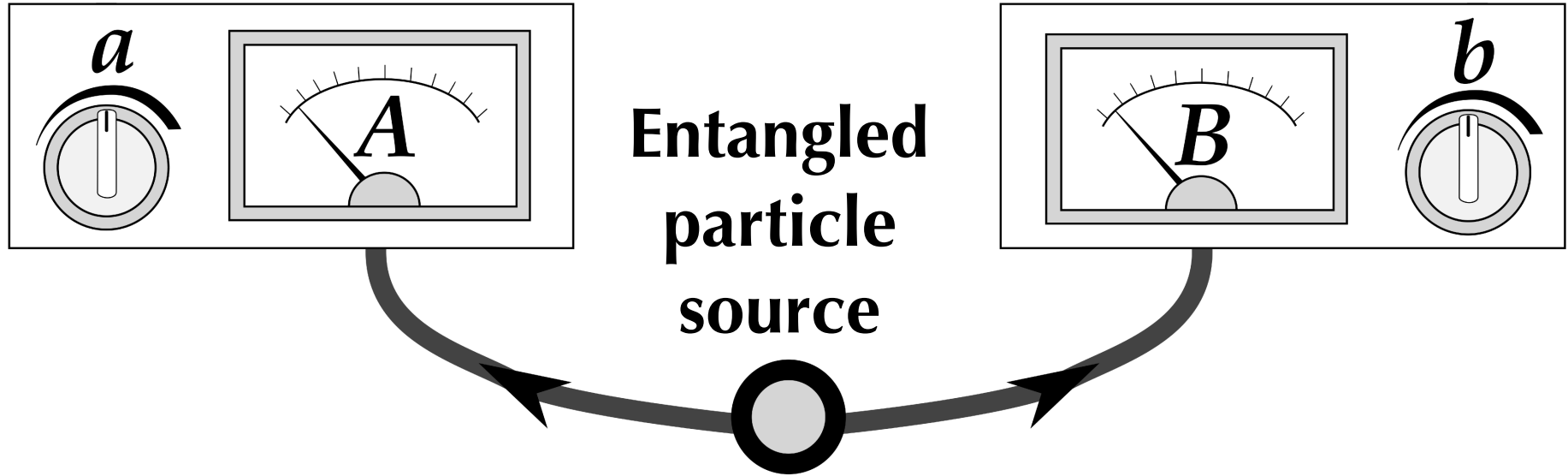
90 degrees: opposite outcome (HV, VH)

Image modified from <http://blogs-images.forbes.com/chadorzel/files/2015/07/aspect3.png>

PHOTON POLARIZATION CORRELATION



BELL TESTS



a, b : Settings

A, B : Outcomes

Big question: Are non-quantum explanations for entanglement viable?

If yes, QM incomplete → *Hidden variables*

WHY CAUSAL EXPLANATIONS FAIL

Quantum correlation is **NOT** like classical correlation!



<http://themassinvasion.com/wp-content/uploads/2015/07/Mystery-Box.jpg>

<http://youwantmetowearwhat.com/wp-content/uploads/2010/11/Left-Right-Gloves.jpg>

OUTLINE

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6. Future Tests

BELL'S INEQUALITY ASSUMPTIONS

1. Realism
2. Locality
3. Freedom



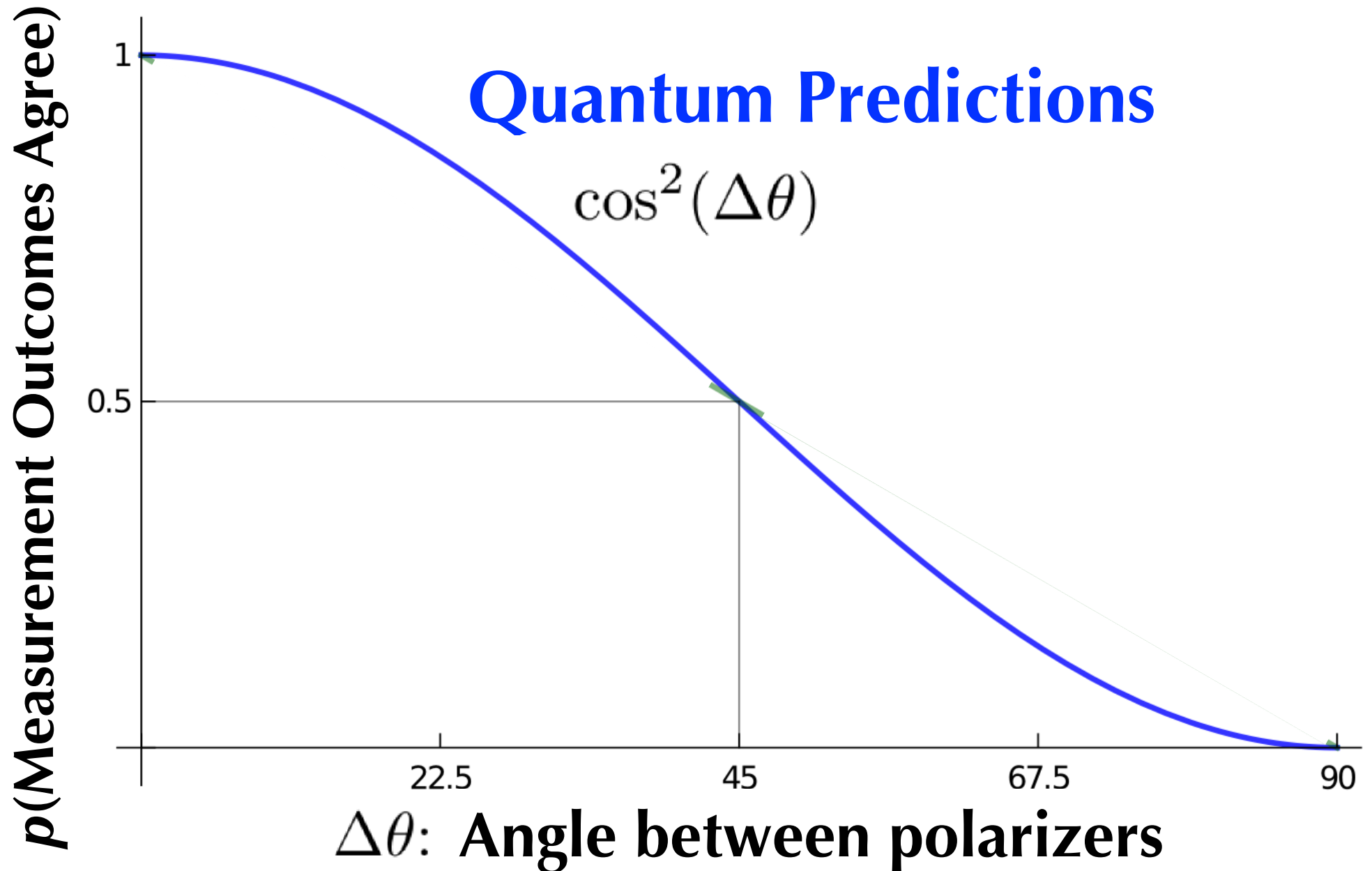
http://images.iop.org/objects/ccr/cern/54/7/19/CCfac8_07_14.jpg

John S. Bell (1928-1990)

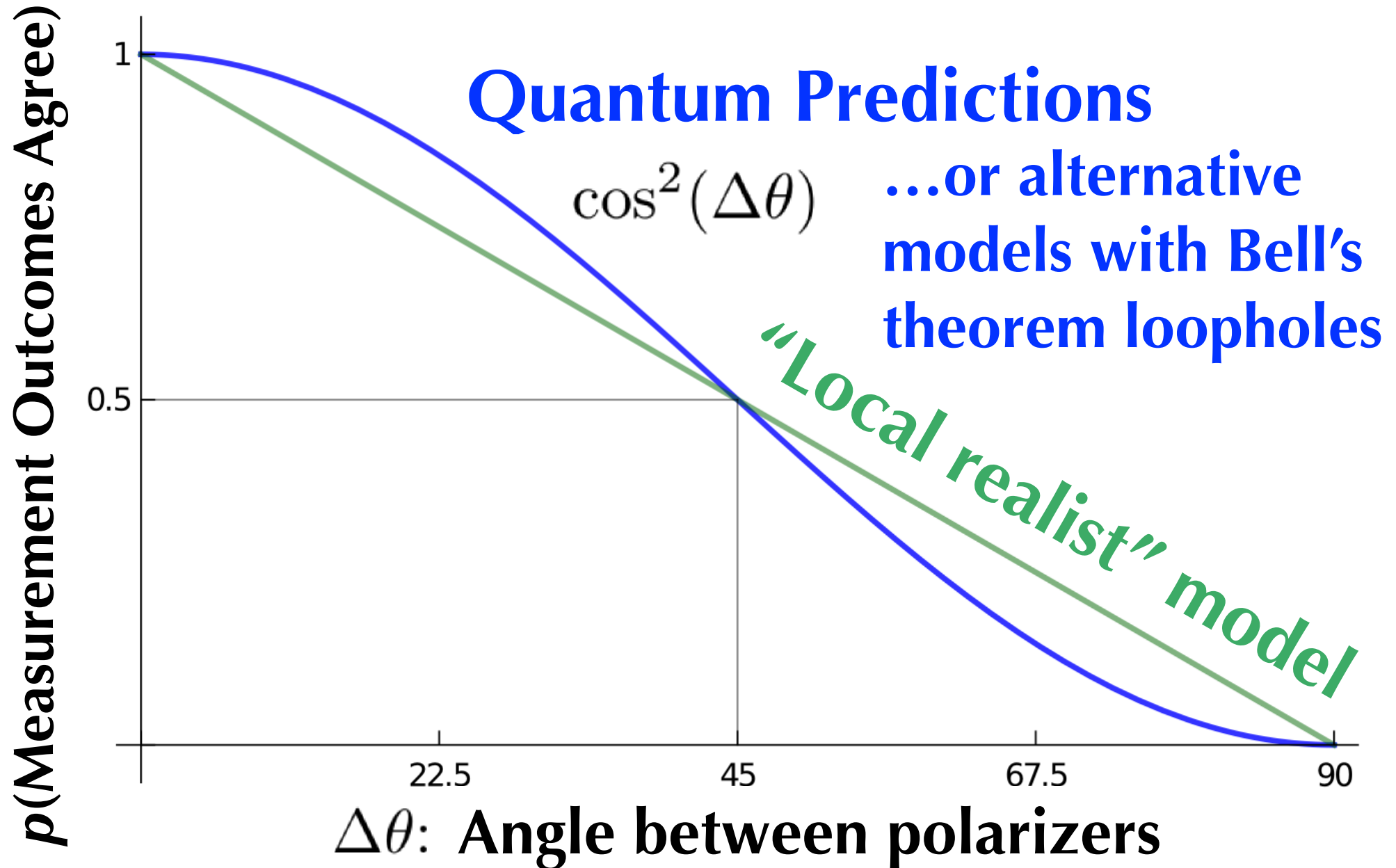
1,2,3 → **Bell's Inequality**

Upper limits on entangled particle measurement correlations in a “**local-realist**” model

PHOTON POLARIZATION CORRELATION



PHOTON POLARIZATION CORRELATION



BELL'S THEOREM

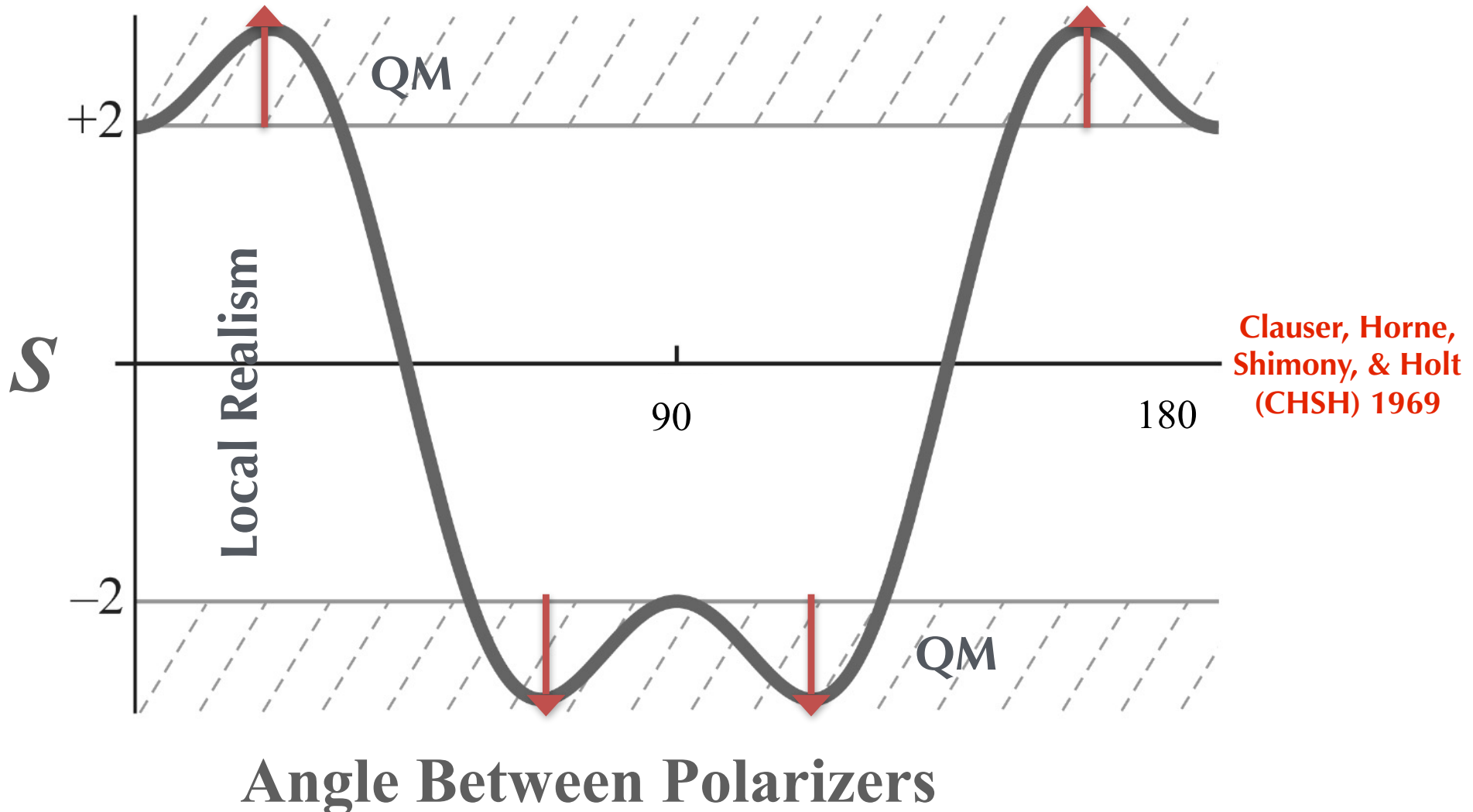
No local-realist theories can reproduce the quantum predictions!

$$S = E(a, b) + E(a', b) + E(a, b') - E(a', b')$$

Bell's assumptions imply $|S| \leq 2$.

QM prediction: $S_{\max} = 2\sqrt{2}$

Dozens of experiments: $S_{\max} > 2$



RELAXING BELL'S ASSUMPTIONS

1. Realism
2. Locality
3. Freedom

Experiments violate Bell's inequality as predicted by quantum mechanics!



→ **At least one of 1,2,3 are false!**

But relaxing any assumption → **LOOPHOLES**
Alternative models could mimic quantum theory

e.g. Can keep realism, locality. Relax Freedom.

Friedman, Guth, Hall, Kaiser, & Gallicchio 2019, *Phys Rev A*, 99, 1, 012121 (arXiv:1809.01307)

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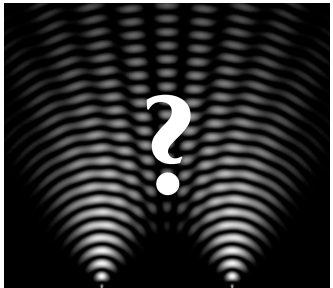
LOOPHOLES & WHY THEY MATTER

The standard interpretation of Bell tests — that “local realism” is incompatible with experiment — relies upon several assumptions.

So What?!

Quantum foundations!

Understanding reality at a deep level. If universe exploits loopholes, does not mean QM is “wrong”, but perhaps derived from a more fundamental underlying theory. Quantum gravity?



Quantum cryptography security

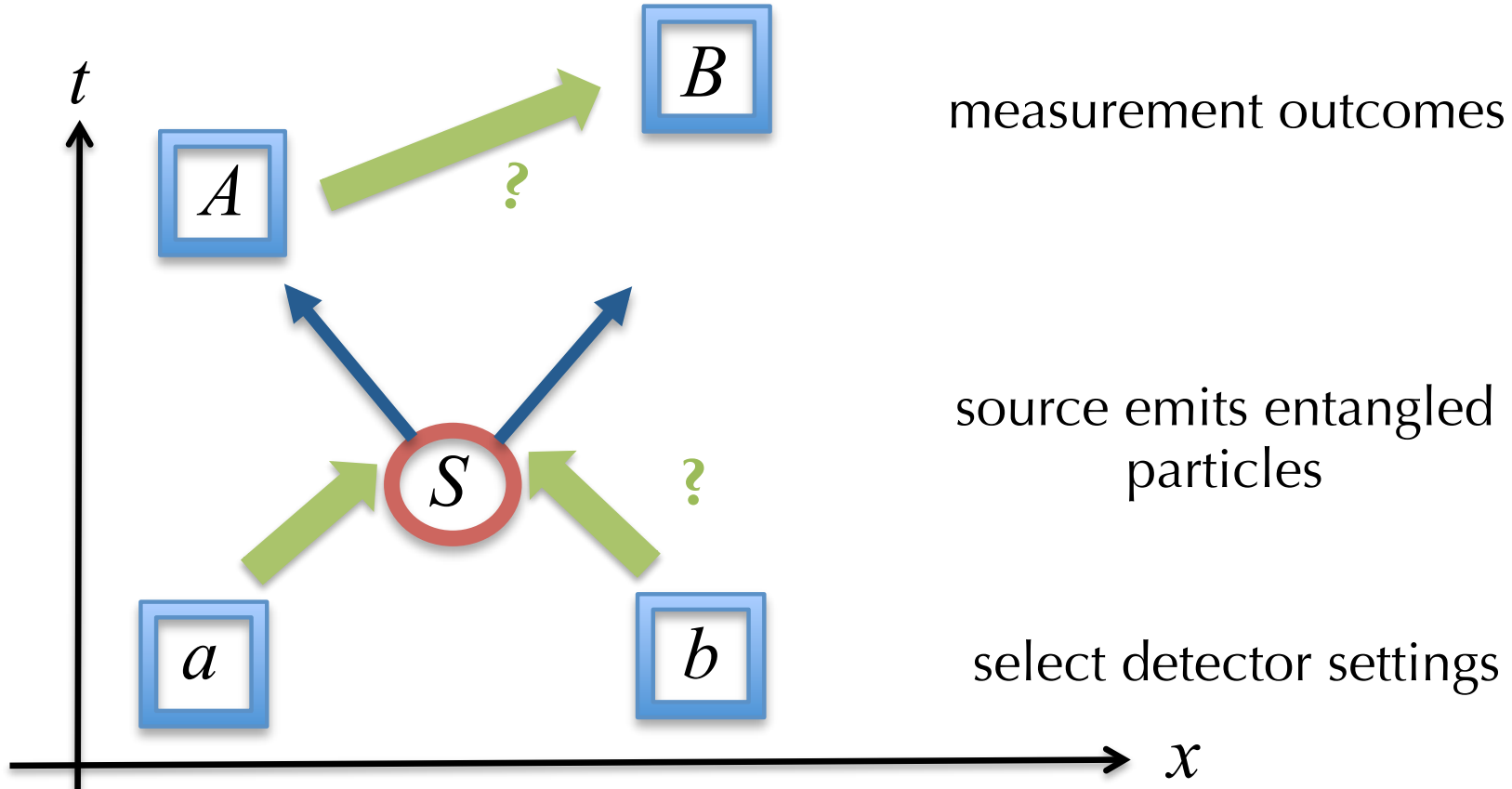
Tech applications! Hackers could exploit loopholes to undermine entanglement-based quantum information schemes



LOCALITY LOOPHOLE

The standard interpretation of Bell tests — that “local realism” is incompatible with experiment — relies upon several assumptions.

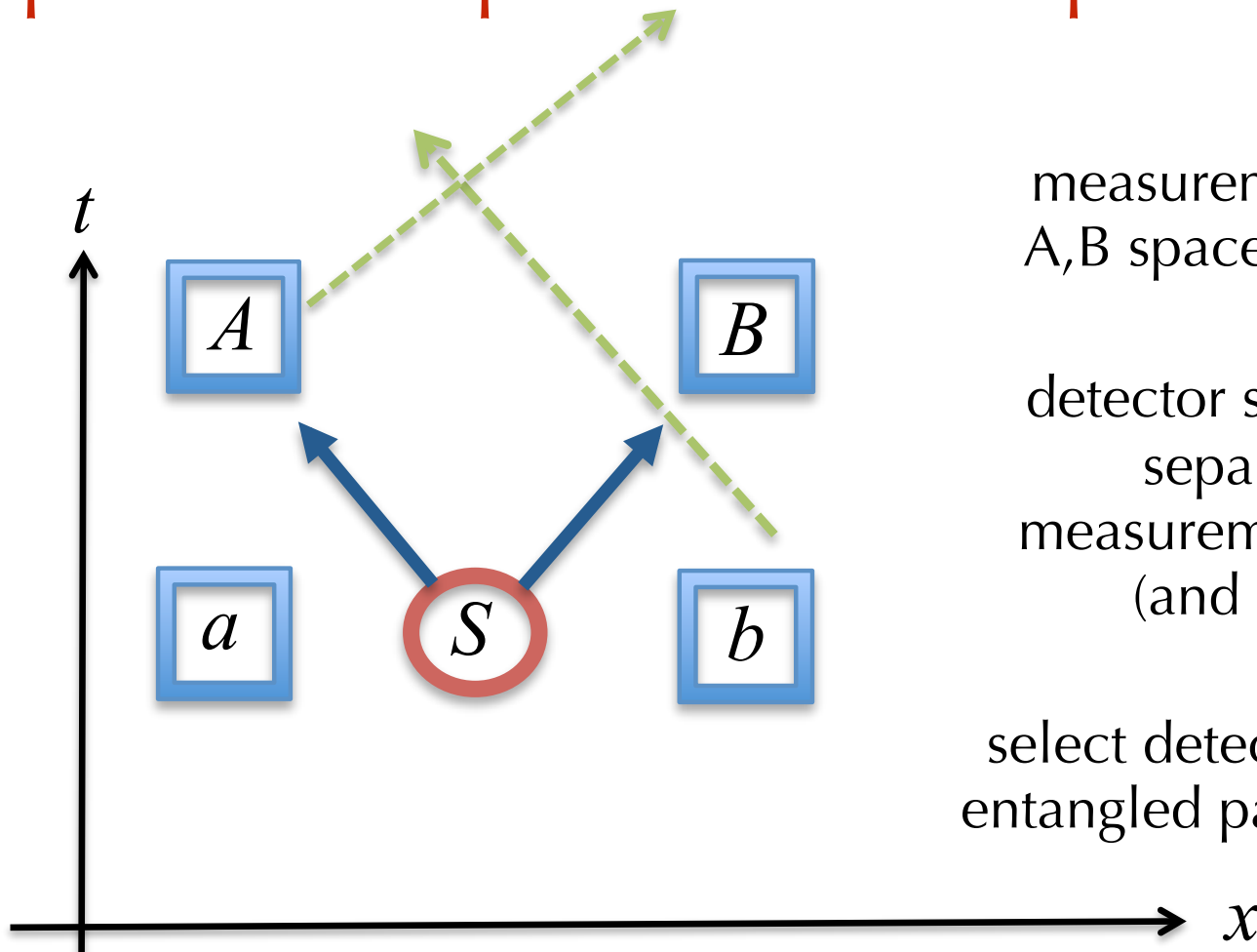
Hidden communication between parties?



CLOSING THE LOCALITY LOOPHOLE

The standard interpretation of Bell tests — that “local realism” is incompatible with experiment — relies upon several assumptions.

Space-like separate relevant pairs of events



measurement outcomes
 A, B space like separated

detector setting choice a
separated from
measurement outcome B
(and vice versa)

select detector settings while
entangled particles are in flight

DETECTION EFFICIENCY LOOPHOLE

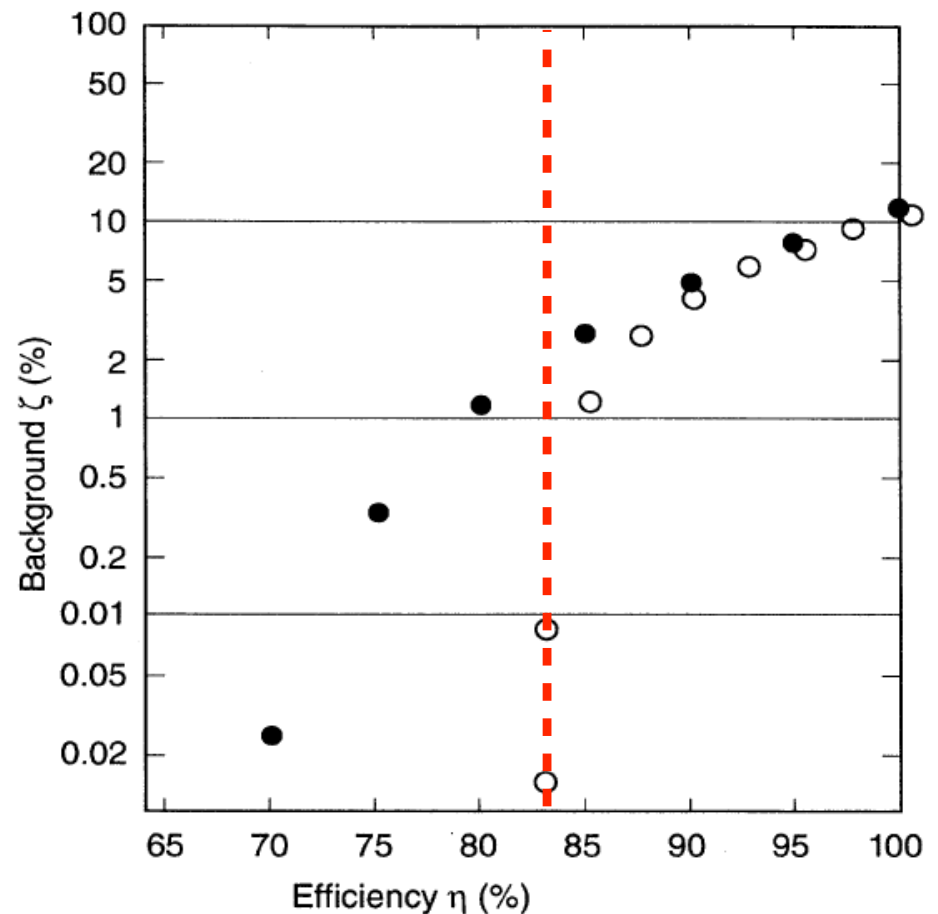
The standard interpretation of Bell tests — that “local realism” is incompatible with experiment — relies upon several assumptions.

Also called the “fair-sampling” loophole

No detectors are 100% efficient.

What if undetected photons skewed the statistics, faking Bell violation without genuine entanglement?

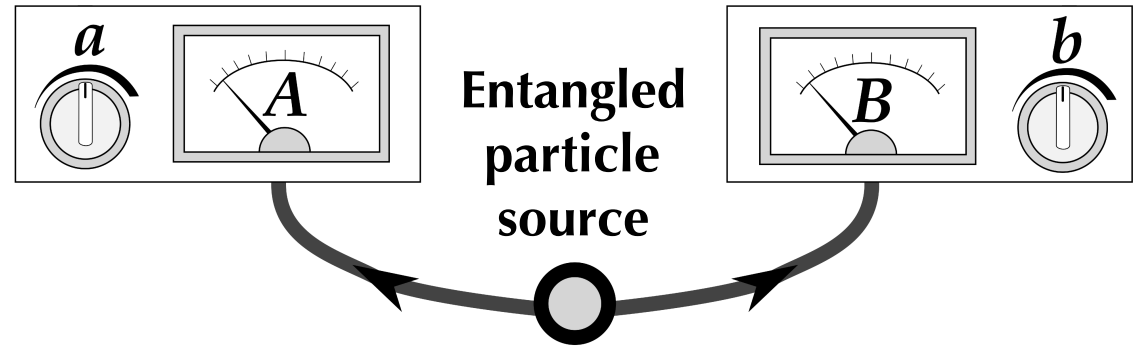
Closing loophole requires detector efficiencies $\geq 83\%$



Garg and Mermin, *Phys Rev D* (1987), Eberhard, *Phys Rev A* (1993)

FREEDOM OF CHOICE LOOPHOLE

X Shrimp & Chicken Fajita	\$12.99
X Fajita Salsas (for One) <i>A Combination of steak, chicken & shrimp.</i>	\$13.25
Fajita Salsas (for Two)	\$21.99
Fajita Mixed <i>Strips of steak & chicken.</i>	\$12.25
Fajita Mixed (for Two)	\$19.50
Fajita Quesadilla <i>2 flour tortillas grilled & stuffed with chicken or steak & cheese.</i>	\$ 9.50
X Shrimp Fajitas	\$14.25
Fajitas <i>Steak or Chicken</i> for One	\$11.99
for Two	\$18.99
X Parillada Mexicana (for One) <i>Pork tips, shrimp, chicken, chorizo & steak.</i>	\$13.99
X Parillada Mexicana (for Two)	\$22.99



If detector settings depend on hidden variables λ (e.g. from past events), experimental choices might not be perfectly free!

Still have free will!

But limited freedom

<http://salsasmexrestaurants.com/test/wp-content/uploads/2014/11/Fajitascombos.jpg>

TOWARD A LOOPHOLE FREE TEST

A. Locality Loophole

Hidden communication between parties

CLOSED for photons: **Aspect+1982, Weihs+1998**

Closing Method?

Spacelike separated measurements, settings

B. Detection Loophole

Measured sub-sample not representative

CLOSED for atoms: **Rowe+2001**, superconducting qubits:

High efficiency detectors

Ansmann+2009, photons: **Giustina+2013, Christensen+2013**

2 LOOPHOLES IN SAME TEST!

CLOSED Locality & Detection

Hensen+2015 (Delft) (electrons)

Giustina+2015 (Vienna)

Shalm+2015 (NIST) (photons)

Rosenfeld+2017 (Germany) (atoms)

TOWARD A LOOPHOLE FREE TEST

C. Freedom-of-Choice Loophole

Settings correlated with hidden variables

 partially for photons: **Scheidl+2010**

**Settings spacelike
separated from
EPR source**

COSMIC BELL TESTS

Locality & Freedom (photons)





Handsteiner+2017 (Vienna)
*Settings chosen with Milky Way Stars. Closed locality,
constrained freedom-of-choice to ~600 years ago.*

Locality & Freedom (photons)





Rauch+2018 (Canary Islands)
*Settings from High Redshift Quasars. Closed locality,
constrained freedom-of-choice to ~7.8 Billion years ago!*

Locality & Detection & Freedom (photons)





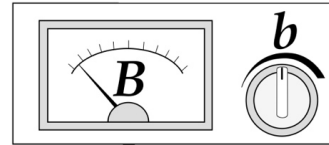
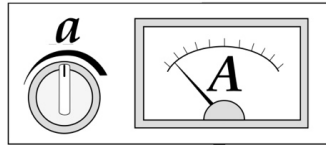


Li+2018 (China)
*Closed locality and detection, constrained
freedom-of-choice to ~11 years ago.*

CHOOSING DETECTOR SETTINGS



Albert



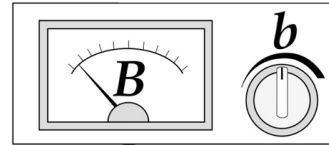
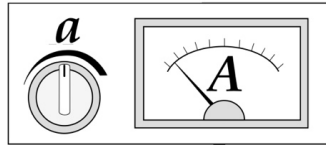
Bohr

Source of Entangled Particles

CHOOSING DETECTOR SETTINGS

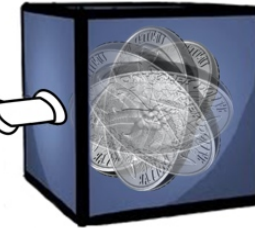


Albert

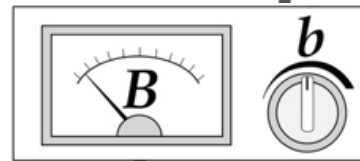
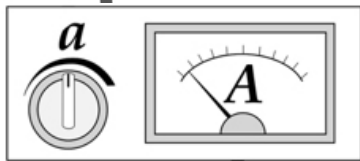


Bohr

Source of Entangled Particles



Quantum
Random
Number
Generator

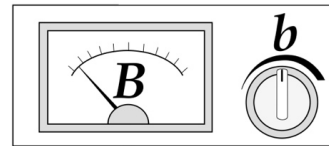
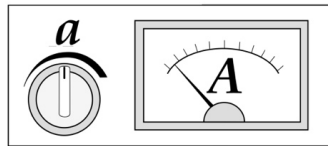


Quantum
Random
Number
Generator

CHOOSING DETECTOR SETTINGS

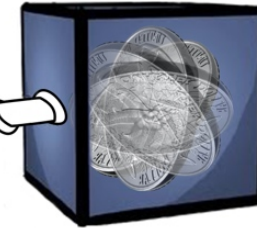


Albert

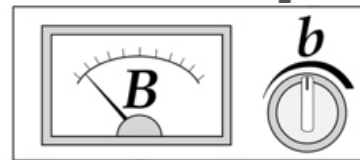
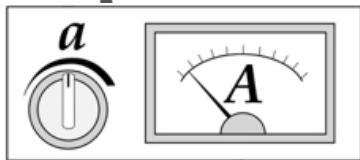


Bohr

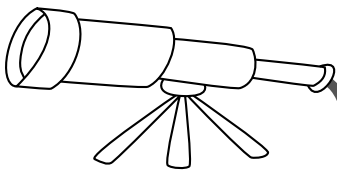
Source of Entangled Particles



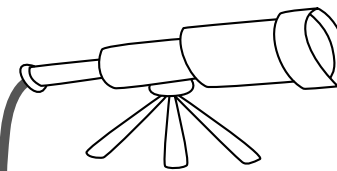
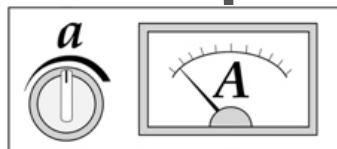
Quantum
Random
Number
Generator



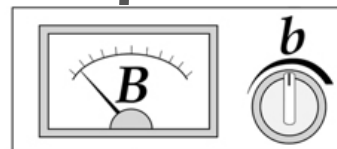
Quantum
Random
Number
Generator



Star A



Star B



Choose
settings with
real-time
observations
of distant
Milky Way
stars

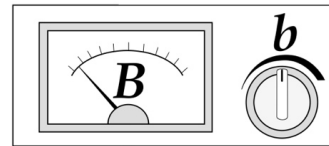
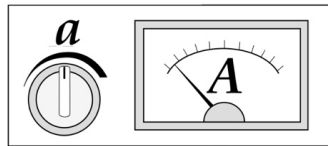
Requires
alternative
theories to
act hundreds
or thousands
of years ago

Adapted from:
Gallicchio, Friedman,
& Kaiser 2014

CHOOSING DETECTOR SETTINGS

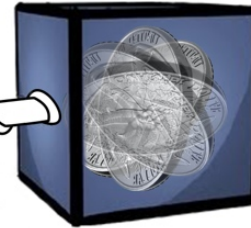


Albert

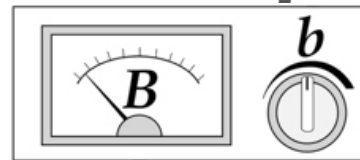
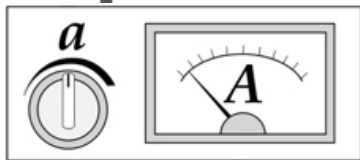


Bohr

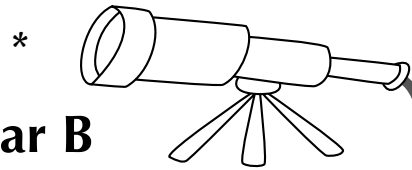
Source of Entangled Particles



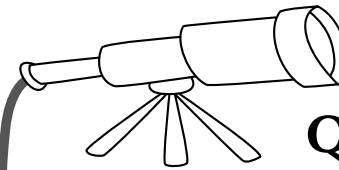
Quantum
Random
Number
Generator



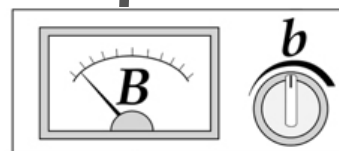
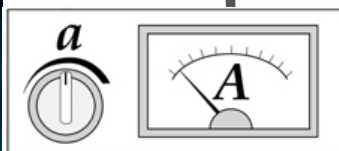
Quantum
Random
Number
Generator



Quasar B



Quasar A



Choose
settings with
observations
of **high
redshift
cosmic
sources**

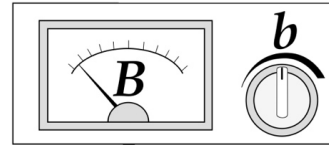
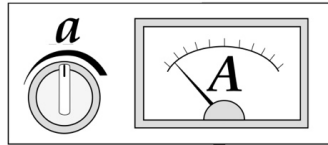
**Relegates
alternatives
to billions of
years ago!**

Adapted from:
Gallicchio, Friedman,
& Kaiser 2014

CHOOSING DETECTOR SETTINGS

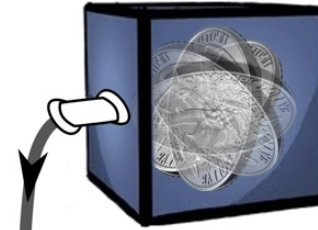


Albert

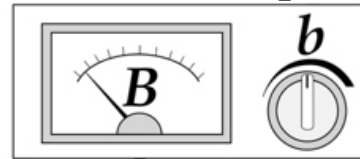
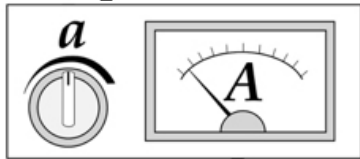


Bohr

Source of Entangled Particles

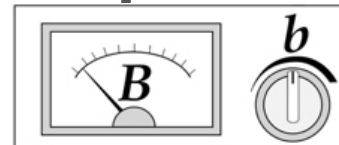
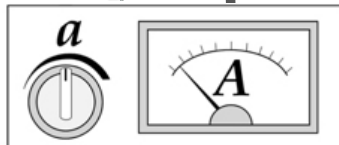
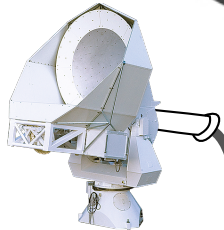


Quantum
Random
Number
Generator

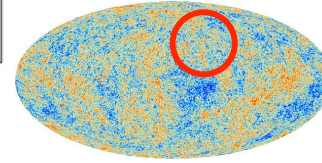
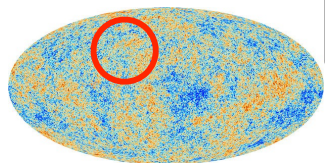


Quantum
Random
Number
Generator

*
CMB
Patch A



*
CMB
Patch B

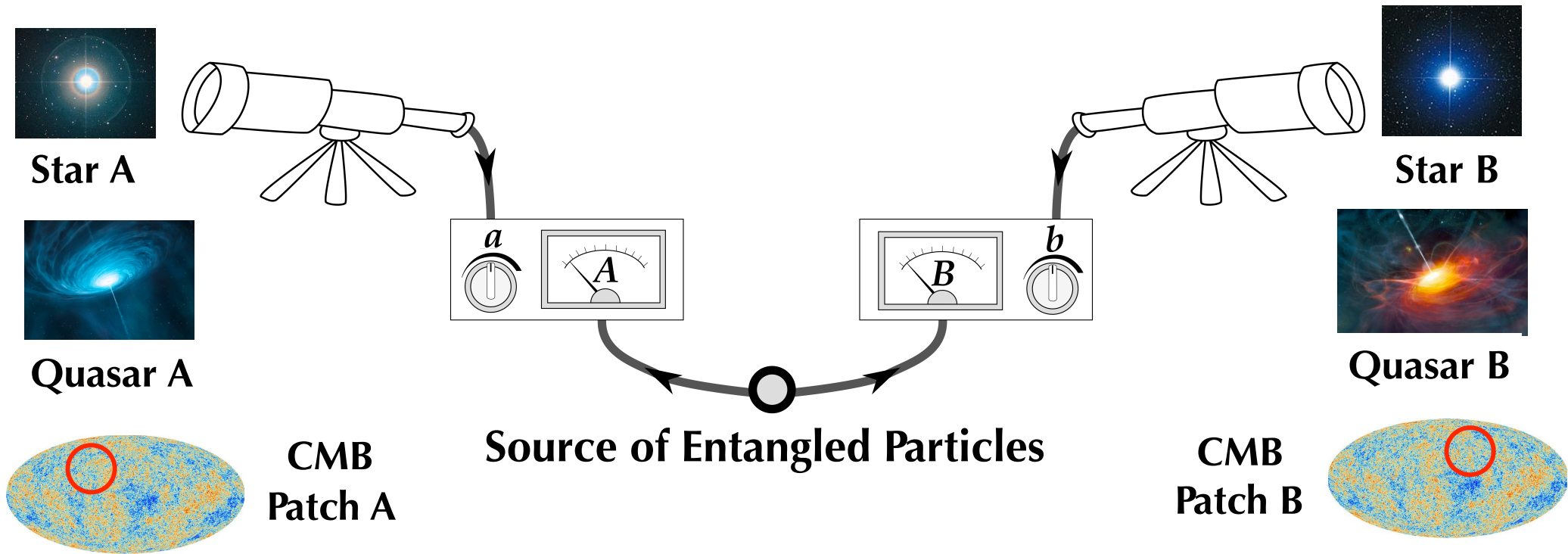


Choose
settings with
observations
of **CMB**
patches,
etc...

Relegates
alternatives
to Big Bang,
era of early
universe
inflation!

Adapted from:
Gallicchio, Friedman,
& Kaiser 2014

COSMIC BELL TESTS



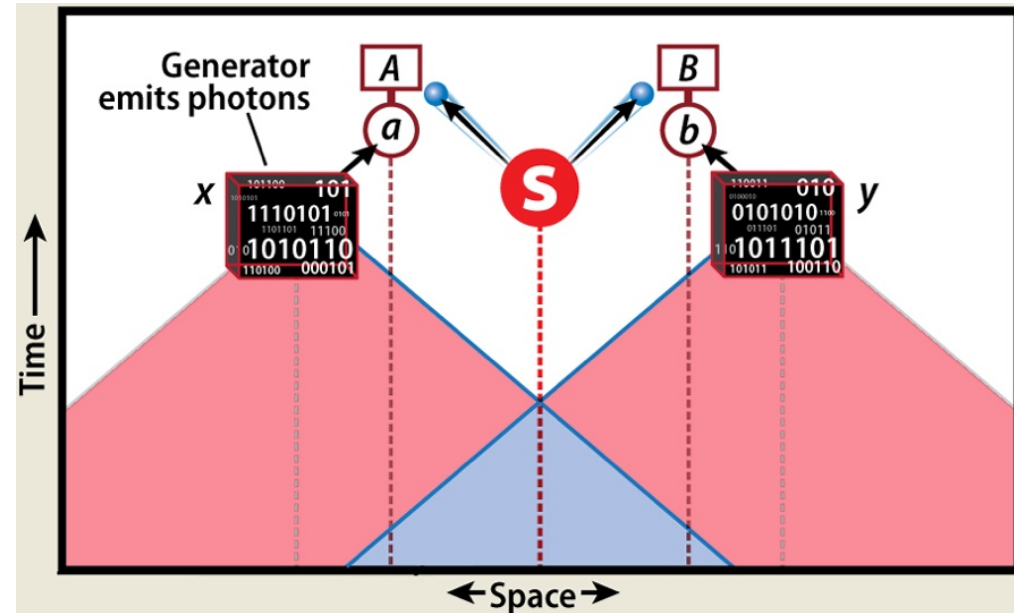
Let the Universe decide how to set up entanglement experiment!

Set a, b by using astronomical sources as cosmic random number generators

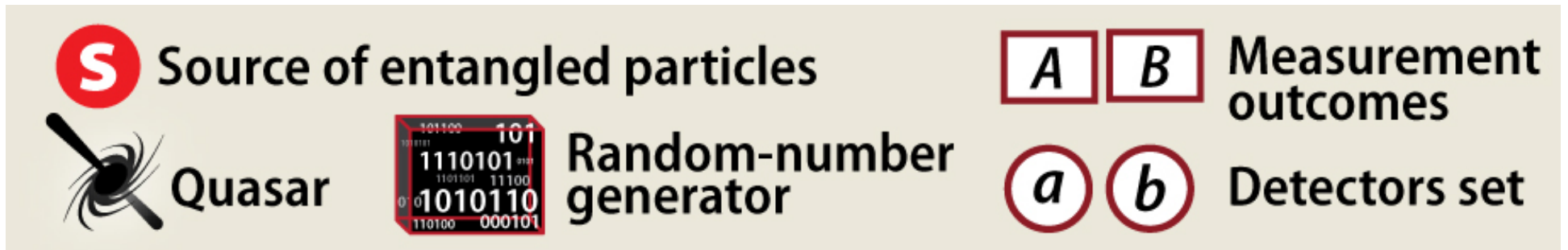
Galicchio, Friedman, & Kaiser 2014, Phys. Rev. Lett., Vol. 112, Issue 11, id. 110405, (arXiv:1310.3288)

SPACE-TIME DIAGRAMMS

Standard Bell Test



Past light cones from random number generators overlap milliseconds before test.

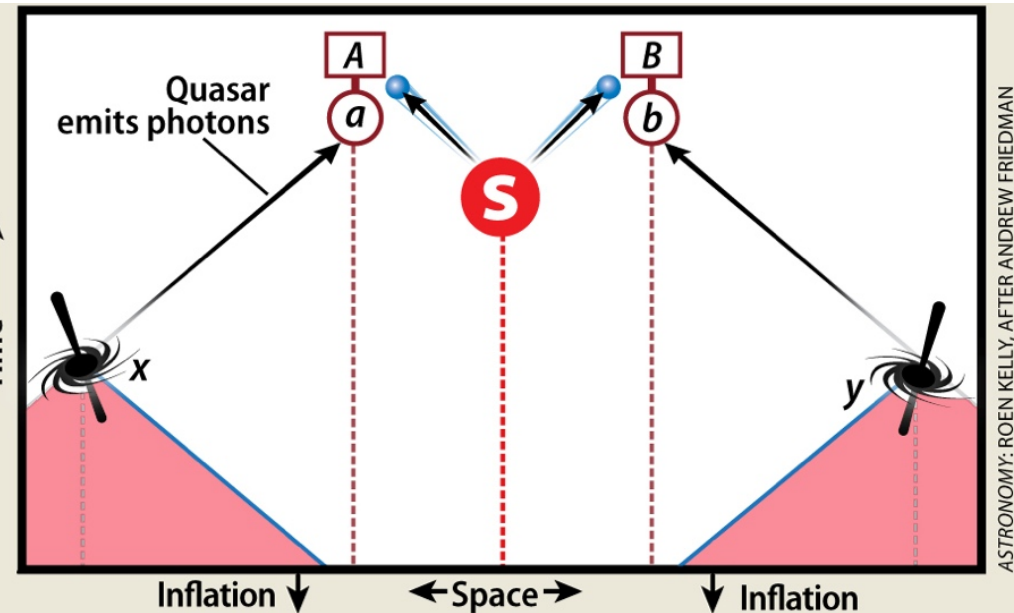
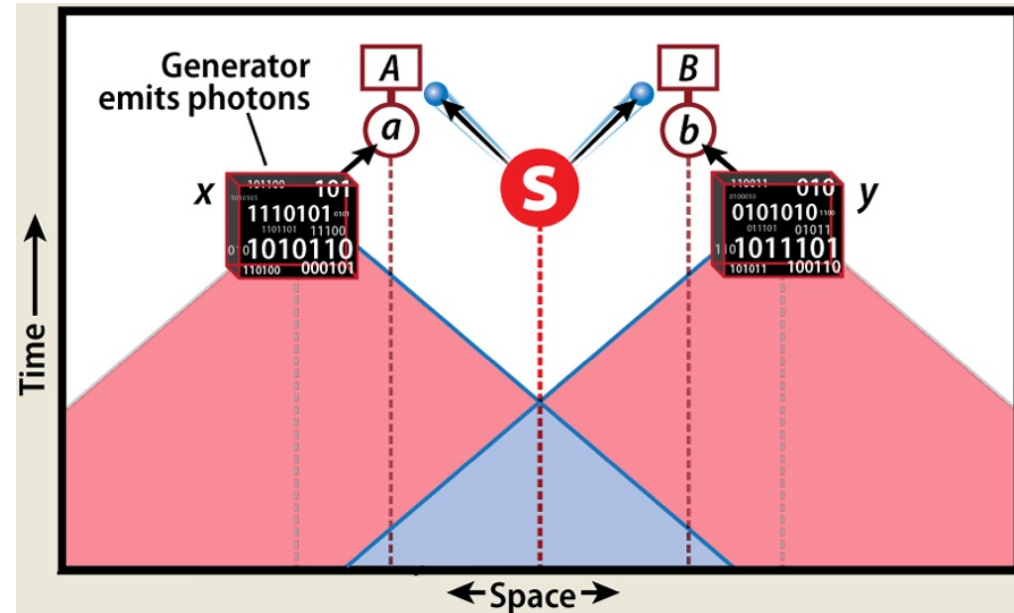


Adapted from: Friedman, Kaiser, & Gallicchio 2013a, *Phys. Rev. D*, Vol. 88, Iss. 4, id. 044038, 18 p. (arXiv:1305.3943)

SPACE-TIME DIAGRAM

Standard Bell Test

Ideal Cosmic Bell Test



ASTRONOMY: ROEN KELLY, AFTER ANDREW FRIEDMAN

Past light cones from random number generators overlap milliseconds before test.

Past light cones from quasars don't overlap since big bang, 13.8 billion years ago.



Source of entangled particles



Measurement outcomes



Quasar



Random-number generator



Detectors set

Adapted from: Friedman, Kaiser, & Gallicchio 2013a, *Phys. Rev. D*, Vol. 88, Iss. 4, id. 044038, 18 p. (arXiv:1305.3943)

OUTLINE

1. Entanglement Tests

2. Bell's Inequality vs. Bell's Theorem

3. Loopholes / Freedom-Of-Choice Loophole

4. Cosmic Bell Test with Milky Way Stars

5. Cosmic Bell Test with Quasars

6. Future Tests

FIRST COSMIC BELL TEST (VIENNA)

PRL 118, 060401 (2017)

PHYSICAL REVIEW LETTERS

week ending
10 FEBRUARY 2017



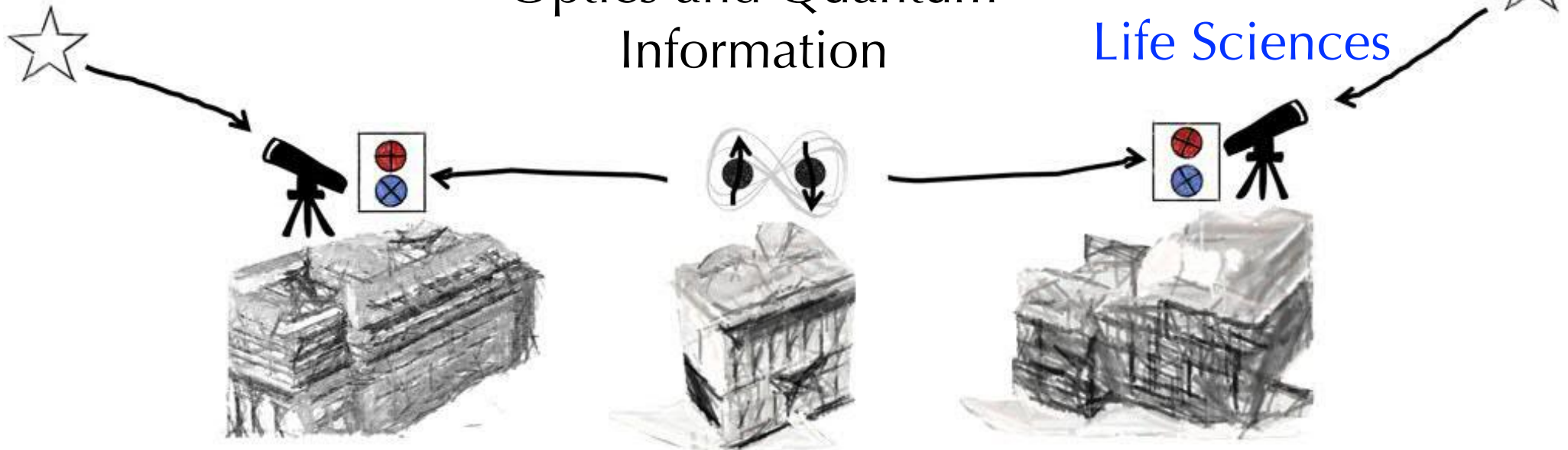
Cosmic Bell Test: Measurement Settings from Milky Way Stars

Johannes Handsteiner,^{1,*} Andrew S. Friedman,^{2,†} Dominik Rauch,¹ Jason Gallicchio,³
Bo Liu,^{1,4} Hannes Hosp,¹ Johannes Kofler,⁵ David Bricher,¹ Matthias Fink,¹ Calvin Leung,³
Anthony Mark,² Hien T. Nguyen,⁶ Isabella Sanders,² Fabian Steinlechner,¹ Rupert Ursin,^{1,7}
Sören Wengerowsky,¹ Alan H. Guth,² David I. Kaiser,²
Thomas Scheidl,¹ and Anton Zeilinger^{1,7,‡}

Alice: Austrian
National Bank

Entangled Particles:
Institute for Quantum
Optics and Quantum
Information

Bob: University
of Natural
Resources and
Life Sciences



Handsteiner, Friedman+2017, *Physical Review Letters*, 118, 6, 060401 (arXiv:1611.06985)

7/19/2019

Summer Science Program, UC San Diego

VIENNA COSMIC BELL TEST

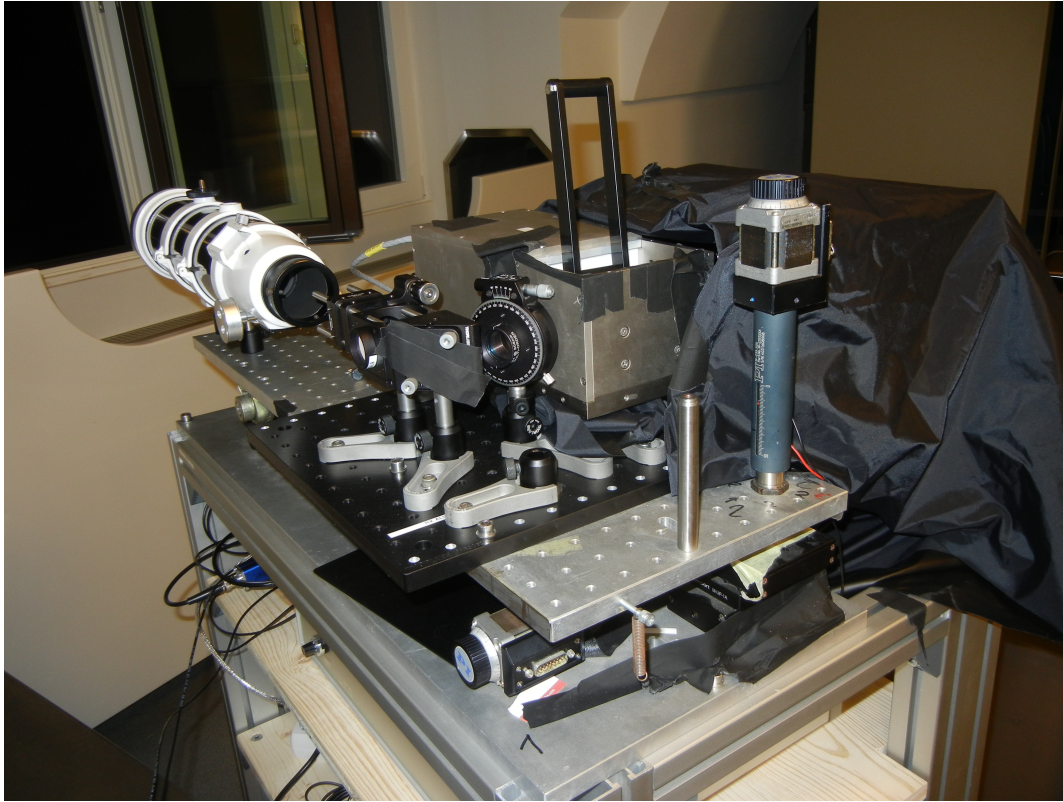


Johannes Handsteiner
with 8-inch stellar
photon telescope



Image Credit: Jason Gallicchio

VIENNA COSMIC BELL TEST



Entangled photon
receiver and
polarization analyzer



Image Credit: Jason Gallicchio

COSMIC SETTING GENERATOR

Red Arm

Guide Camera

Blue Arm



Light In
←

Credit: Jason Gallicchio, Amy Brown, Calvin Leung (HMC)

Leung+2018, *Physical Review A*, Vol. 97, Issue 4, id. 042120 (arXiv:1706.02276)

VIENNA COSMIC BELL TEST



Occupational Hazards



Image Credit: Jason Gallicchio

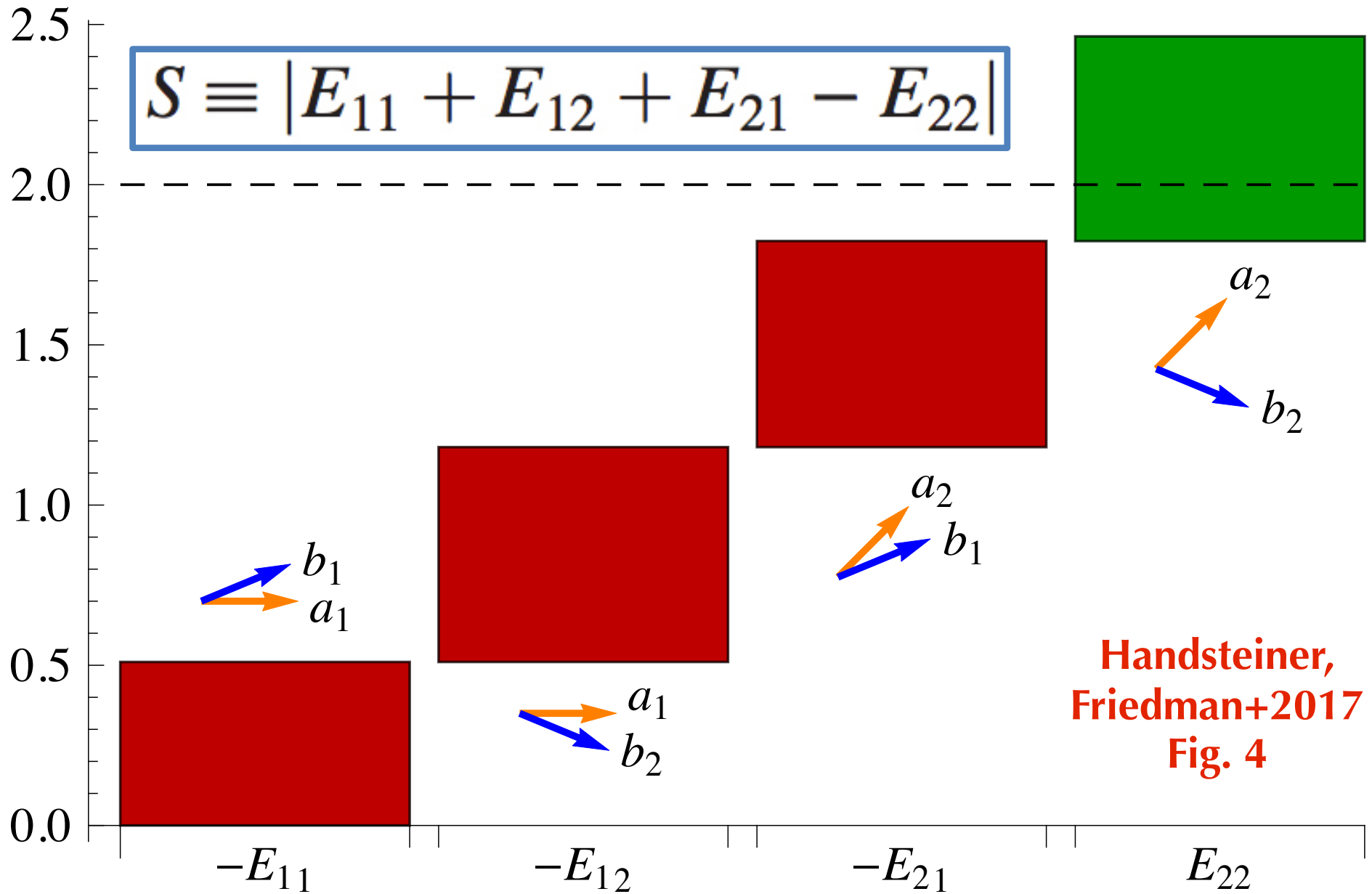
VIENNA COSMIC BELL TEST

Star Selection



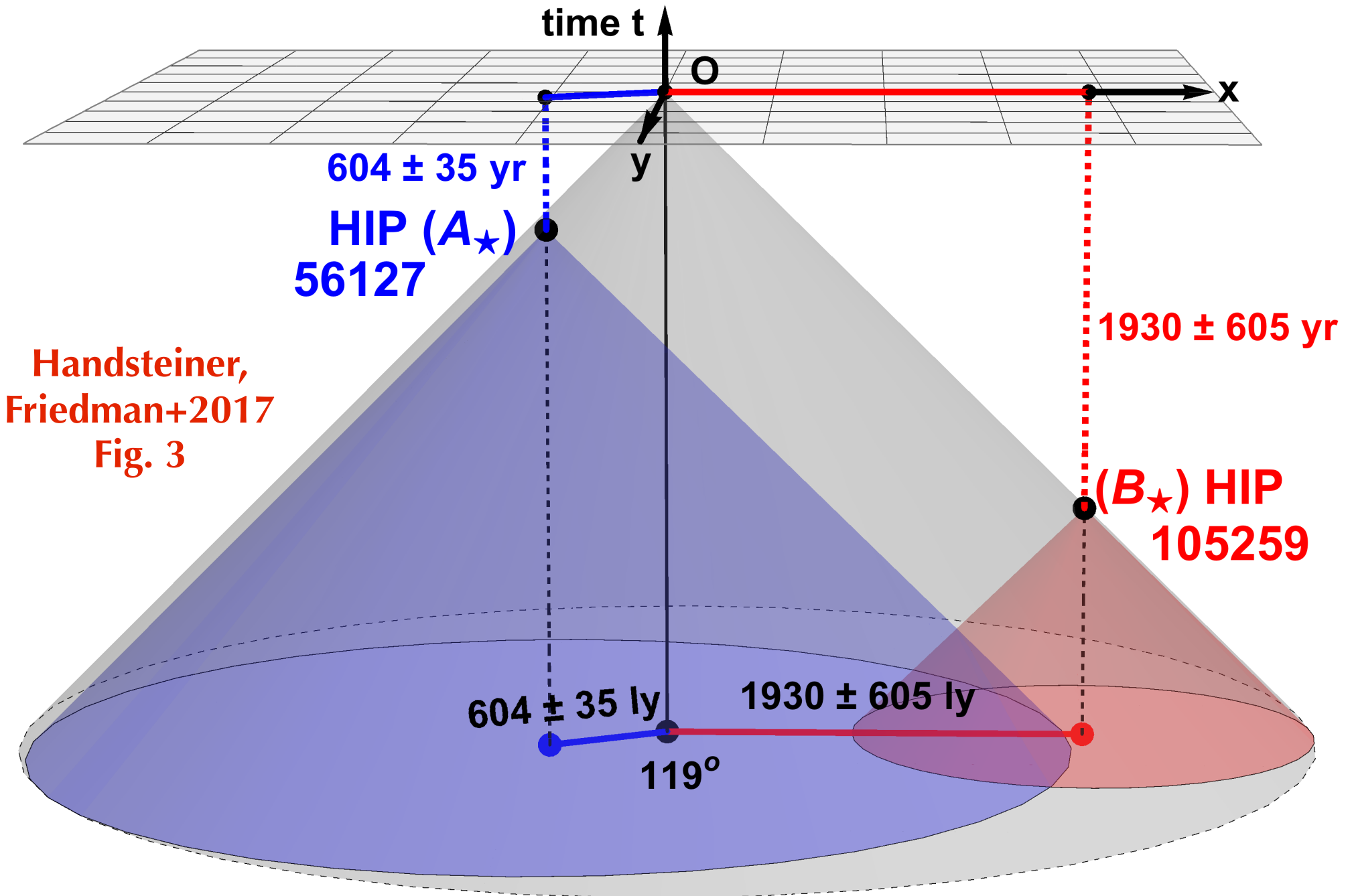
Image Credit: Jason Gallicchio

OBSERVED BELL VIOLATION



Handsteiner,
Friedman+2017
Fig. 4

SPACE-TIME DIAGRAM: STARS



OUTLINE

1. Entanglement Tests

2. Bell's Inequality vs. Bell's Theorem

3. Loopholes / Freedom-Of-Choice Loophole

4. Cosmic Bell Test with Milky Way Stars

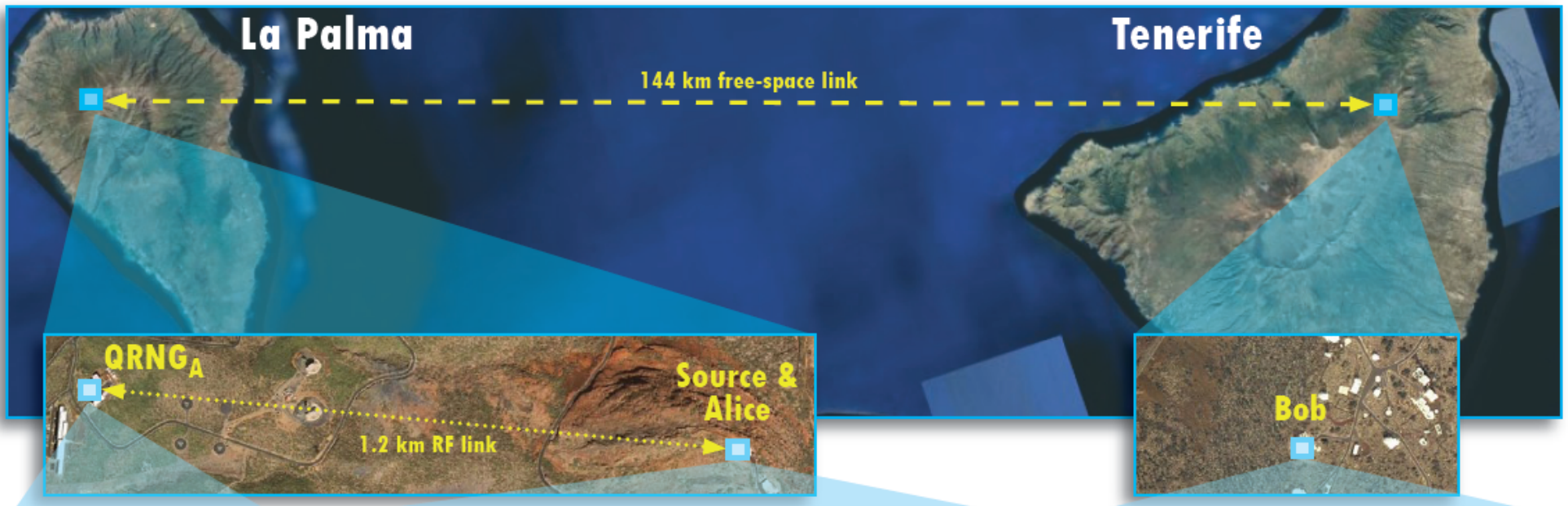
5. Cosmic Bell Test with Quasars

6. Future Tests

ZEILINGER GROUP EXPERIMENTS



Prof. Anton Zeilinger



COSMIC BELL TEST WITH QUASARS

PHYSICAL REVIEW LETTERS 121, 080403 (2018)

Editors' Suggestion

Rauch, D. + 2018, *Physical Review Letters*, Vol. 121, Issue 8, id. 080403 (arXiv:1808.05966)

Cosmic Bell Test Using Random Measurement Settings from High-Redshift Quasars

Dominik Rauch,^{1,2,*} Johannes Handsteiner,^{1,2} Armin Hochrainer,^{1,2} Jason Gallicchio,³ Andrew S. Friedman,⁴
Calvin Leung,^{1,2,3,5} Bo Liu,⁶ Lukas Bulla,^{1,2} Sebastian Ecker,^{1,2} Fabian Steinlechner,^{1,2} Rupert Ursin,^{1,2}
Beili Hu,³ David Leon,⁴ Chris Benn,⁷ Adriano Ghedina,⁸ Massimo Cecconi,⁸ Alan H. Guth,⁵
David I. Kaiser,^{5,†} Thomas Scheidl,^{1,2} and Anton Zeilinger^{1,2,‡}

Roque de los Muchachos Observatory on the Canary Island of La Palma



COSMIC BELL TEST WITH QUASARS

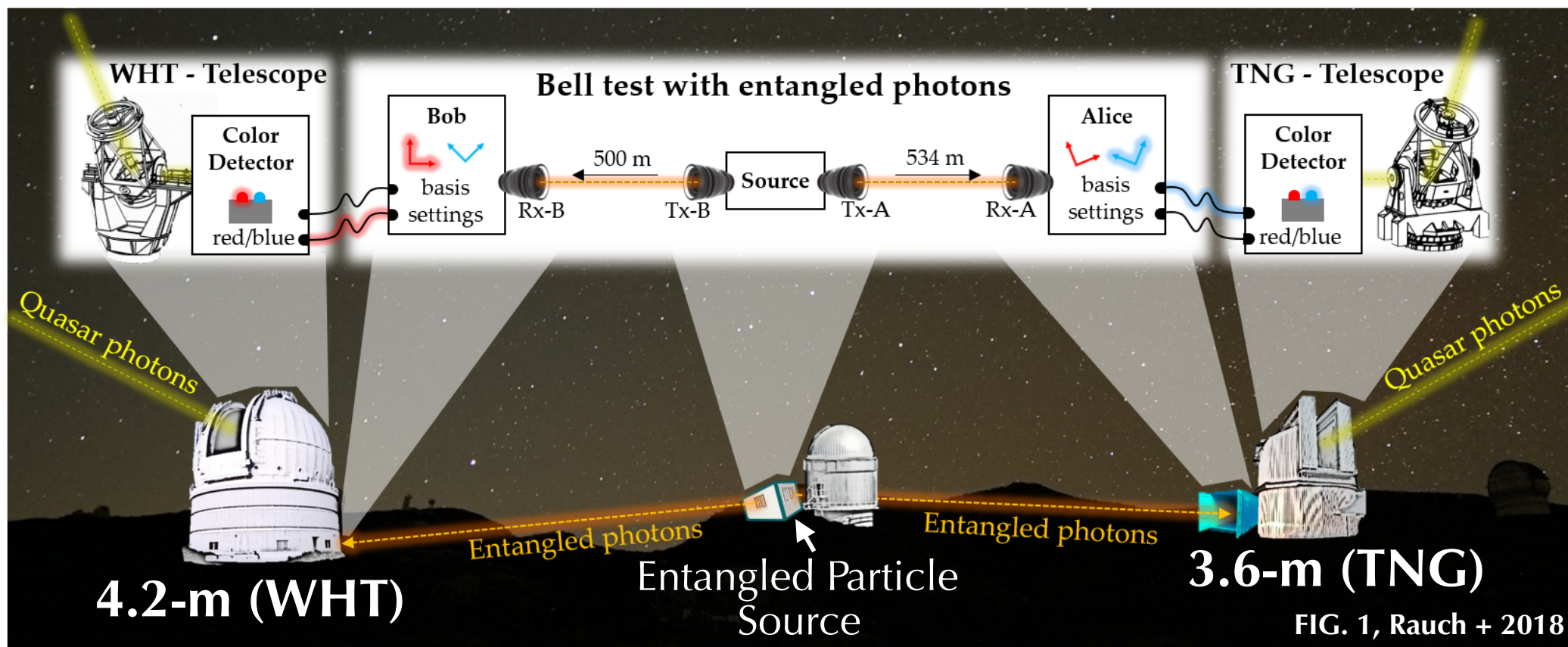
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Rauch, D. + 2018, *Physical Review Letters*, Vol. 121, Issue 8, id. 080403 (arXiv:1808.05966)

Pair	Side	ID	az_k°	alt_k°	z	t_{lb} [Gyr]	τ_{valid}^k [μs]	S_{exp}	p value	ν
1	A	QSO B0350 – 073	233	38	0.964	7.78	2.34	2.65	7.4×10^{-21}	9.3
	B	QSO J0831 + 5245	35	57	3.911	12.21	0.90			
2	A	QSO B0422 + 004	246	38	0.268	3.22	2.20	2.63	7.0×10^{-13}	7.1
	B	QSO J0831 + 5245	21	64	3.911	12.21	0.53			

Standard Deviations

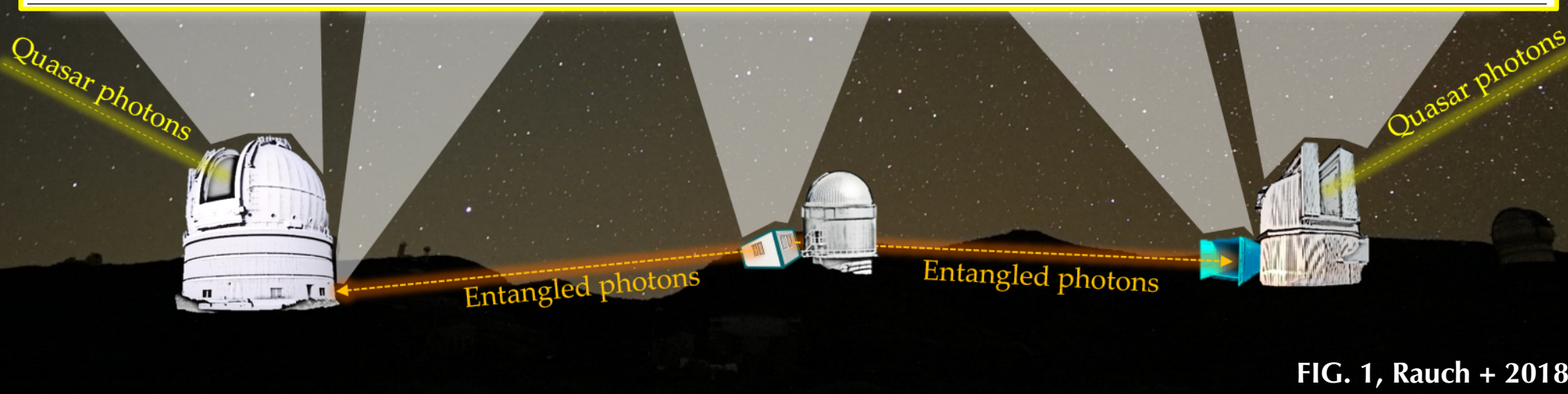


FIG. 1, Rauch + 2018

2+1D SPACETIME DIAGRAM

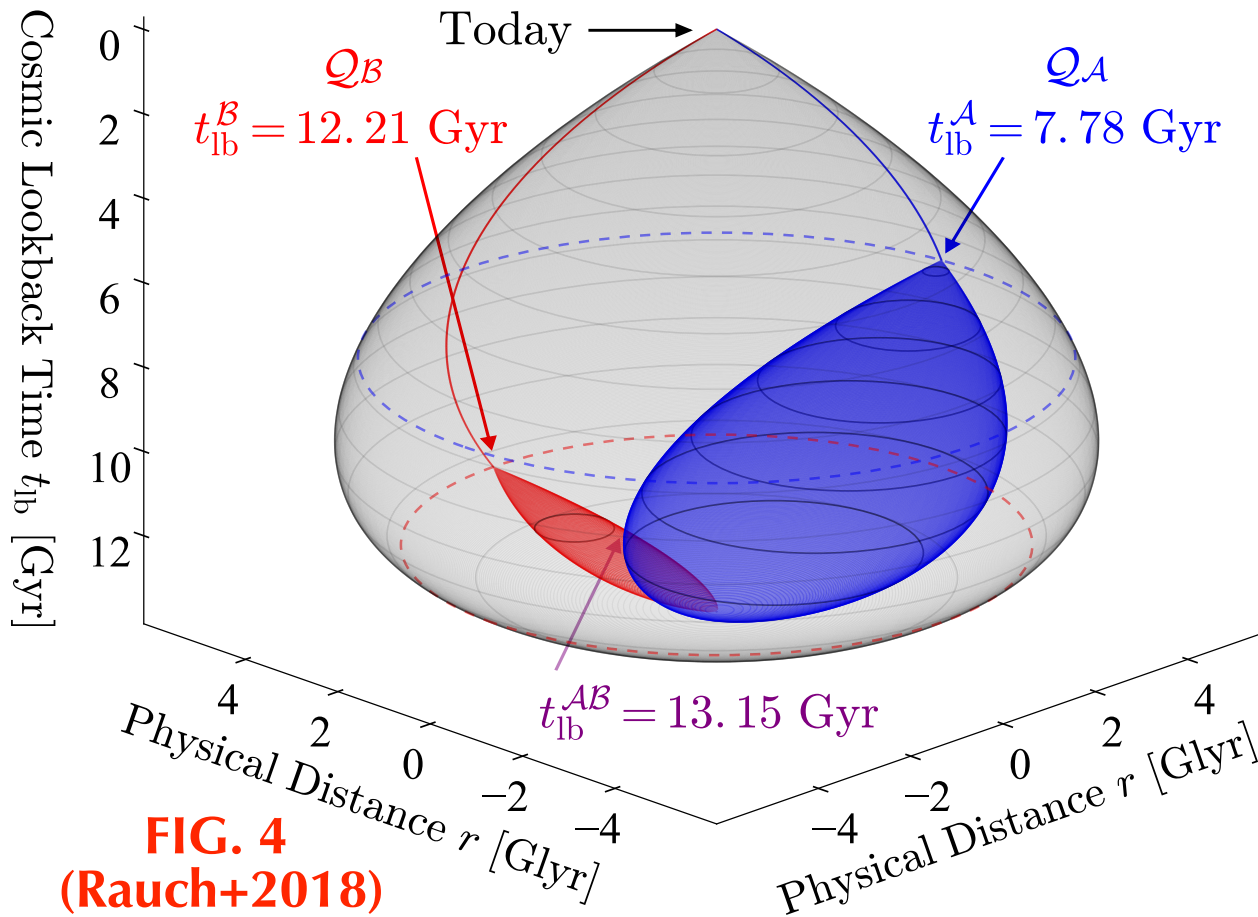


FIG. 4
(Rauch+2018)

- Past light cone of pair 1 experiment (gray)
- Quasar emission events Q_A (blue, 7.78 Gyr ago), Q_B (red, 12.21 Gyr ago)
- Past light cones overlap 13.15 Gyr ago
- Big Bang 13.80 Gyr ago
- Local-realist mechanism would need to have acted at least 7.78 Gyr ago.

• Mechanism must affect detector settings + measurement outcomes from within Q_A (blue), Q_B (red), past light cones (or their overlap), a region with only 4.0% of physical space-time volume within our past light cone.

• **Rules out 96% of space-time from causally influencing our experiment!**

$$F_{\text{excl}} = 1 - \left(\frac{V_Q^{(4)}(\tau_A, \tau_B, \alpha)}{V_{\text{exp}}^{(4)}(\tau_0)} \right) = 0.960$$

COSMIC BELL TEST WITH QUASARS

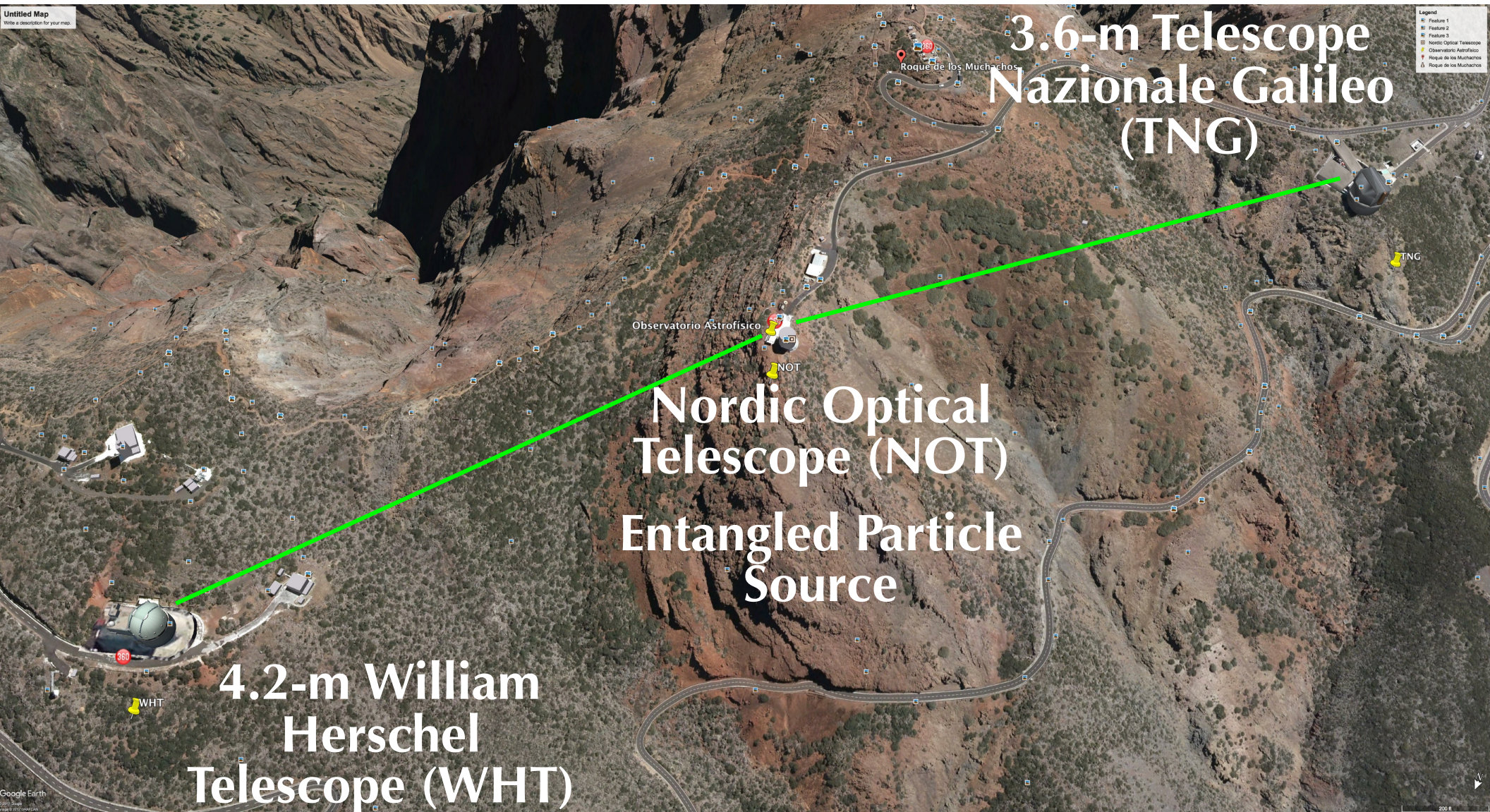


Image ©2018 DigitalGlobe (Google Earth)

CHOOSING THE BEST QUASARS

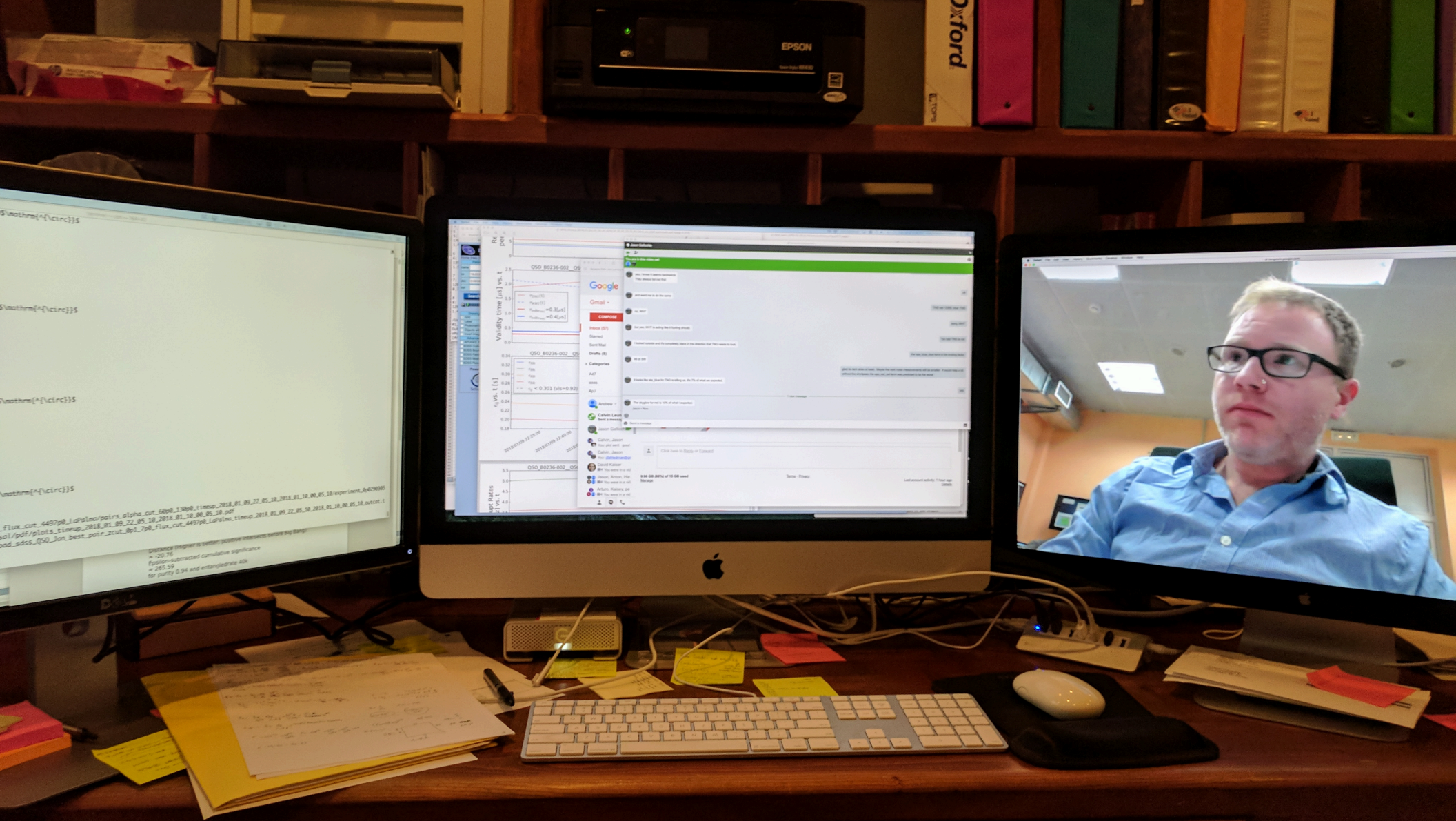


Image Credit: Andrew Friedman (UCSD)

NO PRESSURE!

Image Credit: Andrew Friedman (UCSD)



LA PALMA COSMIC BELL TEST

Nordic Optical
Telescope (NOT)

Cosmic Bell Test
Entangled
Particle Source
(Shipping
Container)

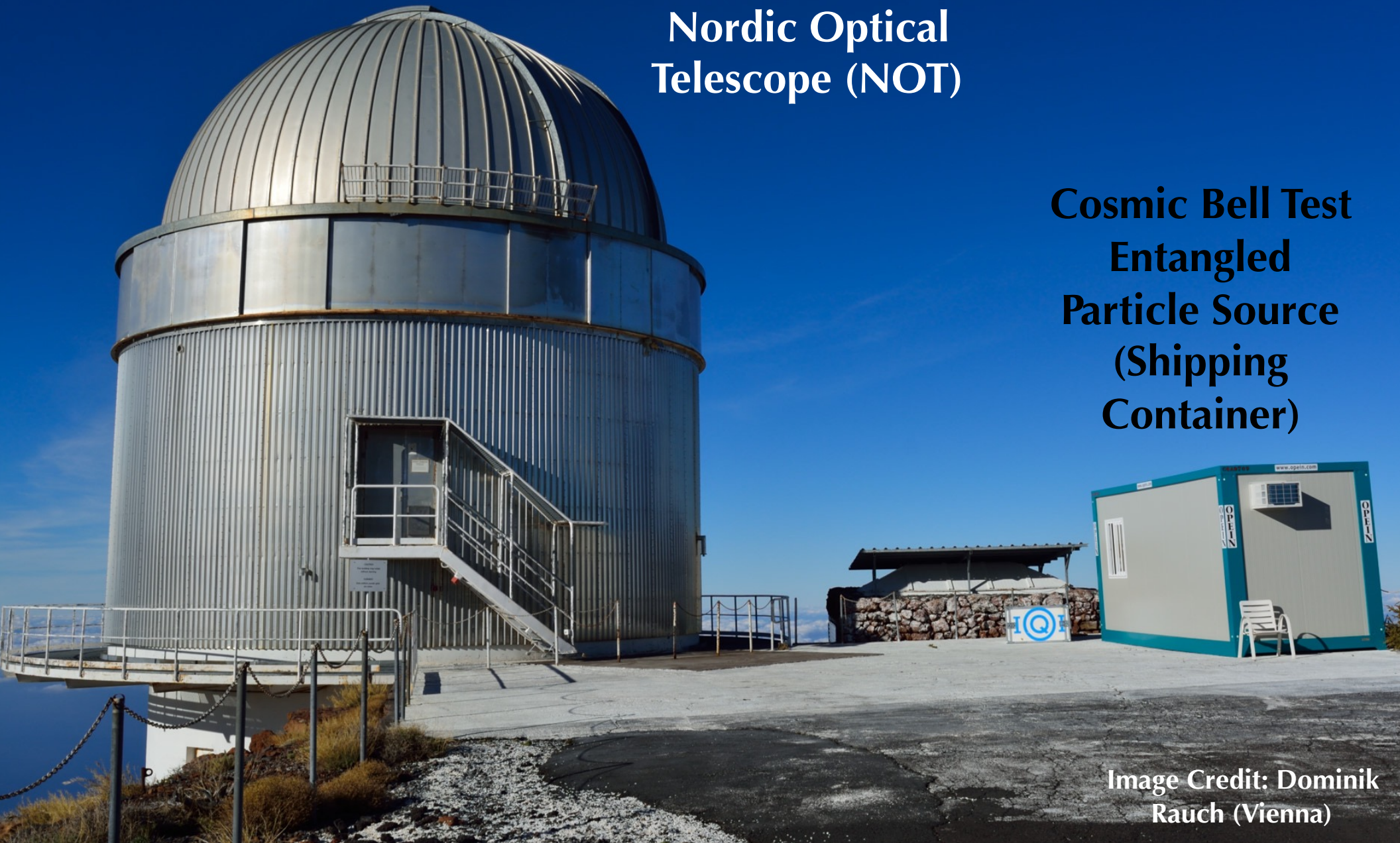


Image Credit: Dominik
Rauch (Vienna)

Nordic Optical
Telescope (NOT)

**NEAR
DISASTER!**

Cosmic Bell Test
Shipping
Container

Image Credit: Dominik
Rauch (Vienna)



Image Credit: Dominik Rauch (Vienna)

**NEAR
DISASTER!**



Image Credit: Dominik
Rauch (Vienna)

Image Credit: Dominik
Rauch (Vienna)

DISASTER AVERTED

Cosmic Bell Test
Shipping
Container



DISASTER AVERTED

Cosmic Bell Test
Shipping
Container



Image Credit: Dominik
Rauch (Vienna)

Entangled photon source fixed, reinstalled in now secured shipping container control room.

ADVENTURES IN LA PALMA

Chris Benn, Head of Astronomy,
Isaac Newton Group of
Telescopes, La Palma

Thomas Scheidl
(Vienna)

Armin Hochrainer
(Vienna)

Dominik Rauch
(Vienna)

Anton Zeilinger
(Vienna)

Image Credit: David Kaiser (MIT)

COSMIC BELL TEST WITH QUASARS

PHYSICAL REVIEW LETTERS **121**, 080403 (2018)

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Cosmic Bell Test Using Random Measurement Settings from High-Redshift Quasars

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Rauch, D. + 2018, *Physical Review Letters*, Vol. 121, Issue 8, id. 080403 (arXiv:1808.05966)

Let the Universe decide how to set up entanglement experiment!

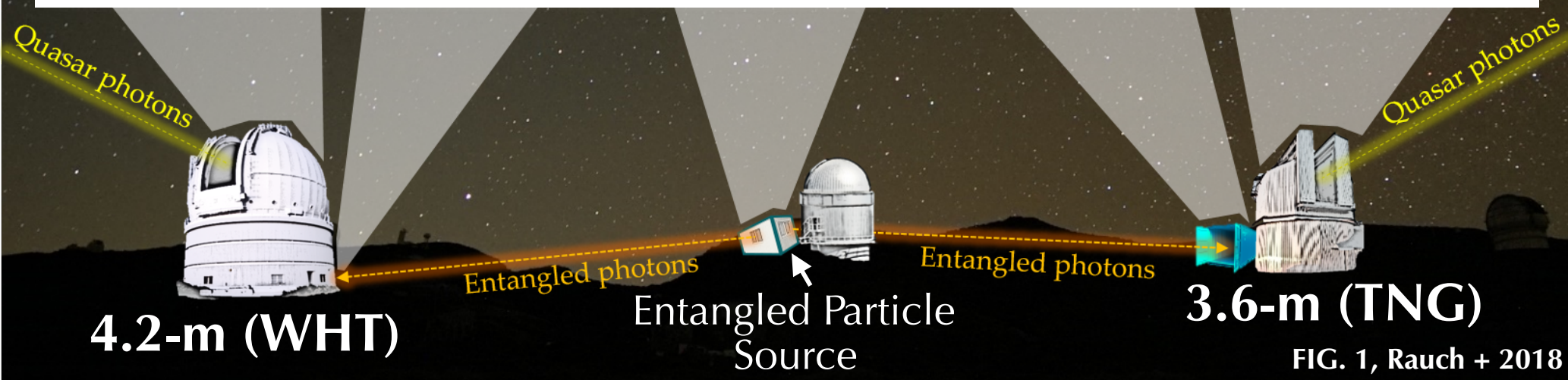
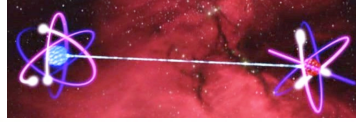


FIG. 1, Rauch + 2018

COSMIC BELL IN THE NEWS

MIT News

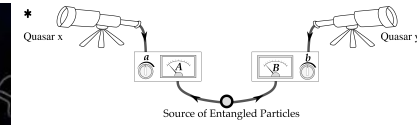
ON CAMPUS AND AROUND THE WORLD



Cosmic conundrum

Can the cosmos test quantum entanglement?

Albert Einstein hated the idea he called “spooky actions at a distance,” but astronomers now are hoping to illuminate some of these tricky quantum puzzles. by Andrew Friedman



https://asfriedman.physics.ucsd.edu/media_coverage.shtml

Closing the ‘free will’ loophole

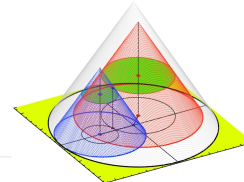
MIT researchers propose using distant quasars to test Bell’s theorem.

Forbes / Tech

Jennifer Chu, MIT News Office
February 20, 2014

JUN 18, 2014 @ 07:00 AM 16,356 VIEWS

Cosmic Test For Quantum Physics' Last Major Loophole



Sunday Review

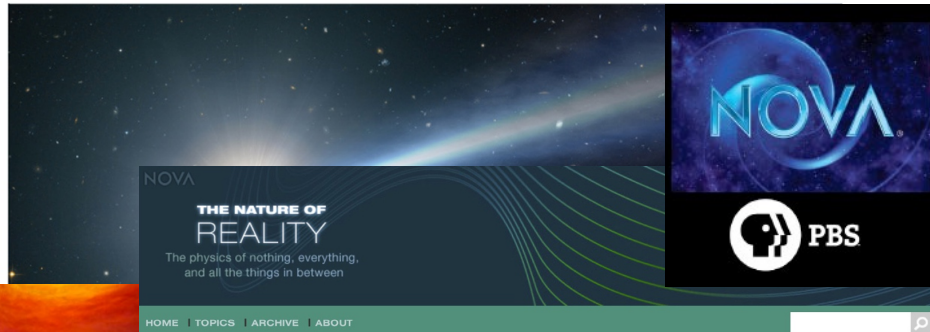
The New York Times

Is Quantum Entanglement Real?

Gray Matter

NOV. 14, 2014

By DAVID KAISER

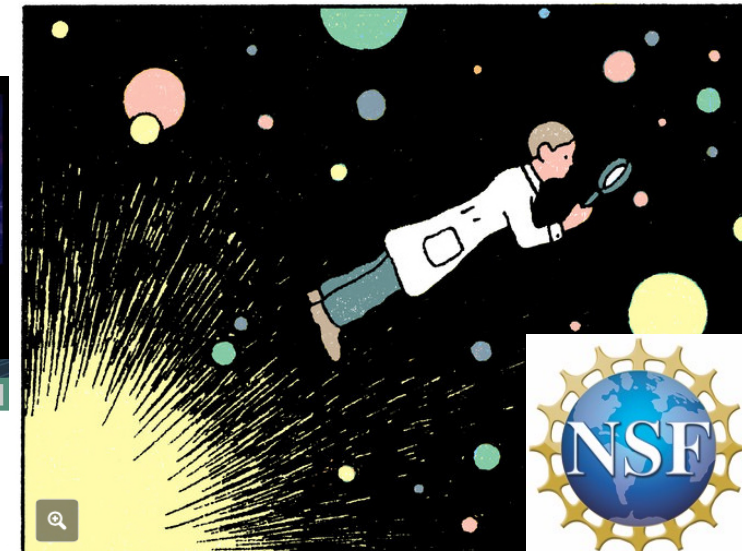


Quasar Experiment May Shed Light on Quantum Physics and Free Will

By CHARLES Q. CHOI, INSIDE SCIENCE

The Universe Made Me Do It? Testing “Free Will” With Distant Quasars

By Andrew Friedman on Wed, 19 Mar 2014



COSMIC BELL IN THE NEWS

QUANTUM THEORY BY STARLIGHT

By David Kaiser February 7, 2017



New Scientist

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NEWS & TECHNOLOGY 7 February 2017

Starlight test shows quantum world has been weird for 600 years



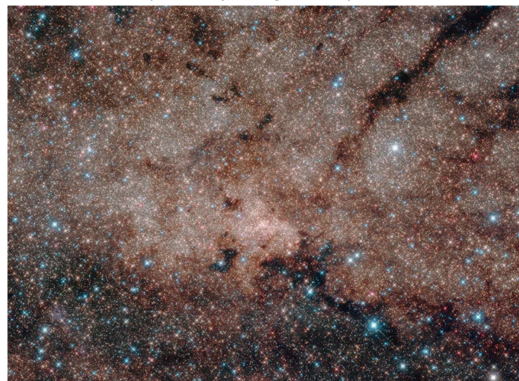
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PHYSICS

Cosmic Test Bolsters Einstein's "Spooky Action at a Distance"

Physicists harness starlight to support the case for entanglement.

By Elizabeth Gibney, Nature magazine on February 3, 2017



By CALLA COFIELD / SPACE.COM February 13, 2017, 1:00 PM

600-year-old starlight bolsters Einstein's "spooky action" theory



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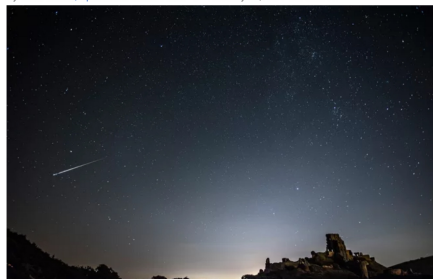
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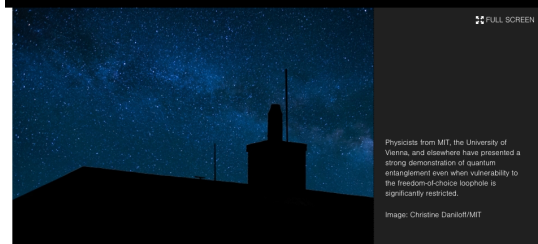
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600-Year-Old Starlight Bolsters Einstein's 'Spooky Action at a Distance'

By Calla Cofield, Space.com Senior Writer | February 13, 2017 01:25am ET



ON CAMPUS AND AROUND THE WORLD



Stars align in test supporting "spooky action at a distance"

Physicists address loophole in tests of Bell's inequality, using 600-year-old starlight.

Jennifer Chu | MIT News Office February 6, 2017

1 Dec 2016 in Research & Technology

Cosmic experiment is closing another Bell test loophole

A new experiment combines nanoscale measurements and interstellar distances to demonstrate quantum nonlocality.

Andrew Grant

ANIL ANANTHASWAMY SCIENCE 09.05.18 07:00 AM

LOOPHOLES AND THE 'ANTI-REALISM' OF THE QUANTUM WORLD



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Cosmic test backs 'quantum spookiness'

Physicists harness starlight to support the case for entanglement.

Elizabeth Gibney

02 February 2017

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Experiment Reaffirms Quantum Weirdness

Physicists are closing the door on an intriguing loophole around the quantum phenomenon Einstein called "spooky action at a distance."



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NATALIE WOLCHOVER | FEB 10, 2017 | SCIENCE

http://web.mit.edu/asf/www/media_coverage.shtml

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COSMIC BELL IN THE NEWS



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Observations

Photons, Quasars and the Possibility of Free Will

Flickers of light from the edge of the cosmos help physicists advance the idea that the future is not predetermined

By Brian Koberlein on November 21, 2018



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D-brief

Black Holes Bolster Case For Quantum Physics' Spooky Action

By Jake Parks | August 23, 2018 1:28 pm

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The quest to test quantum entanglement

11/06/18 | By Laura Dattaro

Quantum entanglement, doubted by Einstein, has passed increasingly stringent tests.

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FEATURE 14 November 2018

Einstein was wrong: Why 'normal' physics can't explain reality

The most ambitious experiments yet show that the quantum weirdness Einstein famously hated rules the roost – not just here, but across the entire universe



PHYS ORG Nanotechnology | Physics | Earth | Astronomy & Space

Home » Physics » Quantum Physics » August 27, 2018

Physicists race to demystify Einstein's 'spooky' science

August 27, 2018 by Cynthia Dillon, University of California - San Diego



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PHYSICS

'Spooky' Quantum Entanglement Confirmed Using Distant Quasars

By Ryan F. Mandelbaum

8/21/18 5:10pm | Filed to: SPOOKY ACTION AT A DISTANCE

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QUANTUM | RESEARCH UPDATE

Cosmic Bell test uses light from ancient quasars

21 Aug 2018 Hamish Johnston



MOTHERBOARD VICE

ENTANGLEMENT | By Daniel Oberhaus | Aug 21 2018, 7:38am

Ancient Starlight Just Helped Confirm the Reality of Quantum Entanglement

"The real estate left over for the skeptics of quantum mechanics has shrunk considerably."

SPACE

Space.com » Science & Astronomy

Ancient Quasars Provide Incredible Evidence for Quantum Entanglement

By Chelsea Gohd, Space.com Staff Writer | August 21, 2018 04:58pm ET

Astronomy

Quantum entanglement loophole quashed by quasar light

That's what happens when you let quasars decide what to measure.

By Jake Parks | Published Thursday, August 23, 2018

Astronomy Now The UK's best astronomy magazine

Closing a loophole in Bell's theorem with light from ancient quasars

© 21 August 2018 Astronomy Now

MIT News ON CAMPUS AND AROUND THE WORLD

Light from ancient quasars helps confirm quantum entanglement

Results are among the strongest evidence yet for "spooky action at a distance."

Jennifer Chu | MIT News Office August 19, 2018

The quasar dates back to less than one billion years after the Big Bang. Image: NASA/ESA/ISS/C. Beaman, STScI

COSMIC BELL TEST ON TV!



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OUTLINE

1. Entanglement Tests

2. Bell's Inequality vs. Bell's Theorem

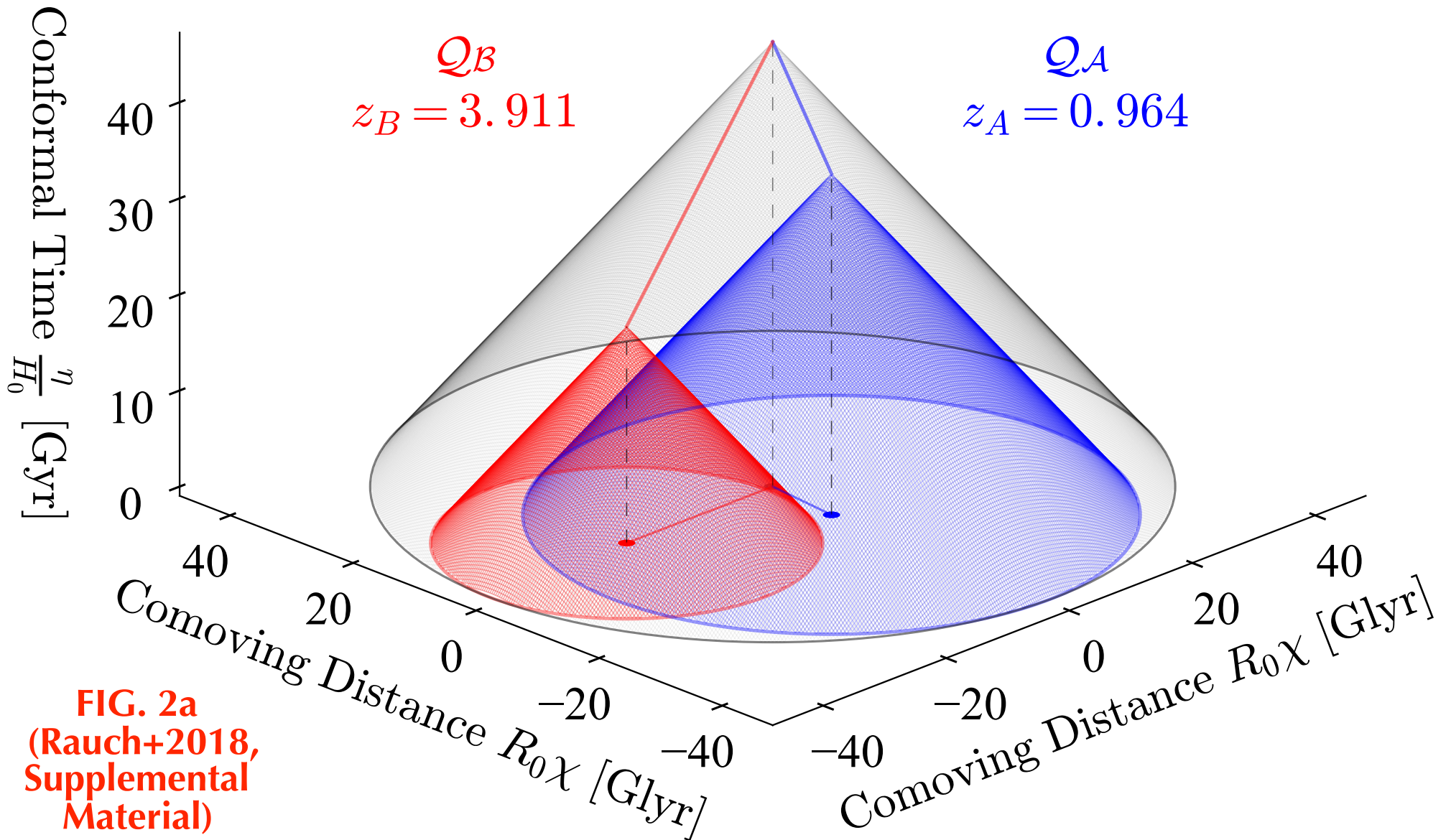
3. Loopholes / Freedom-Of-Choice Loophole

4. Cosmic Bell Test with Milky Way Stars

5. Cosmic Bell Test with Quasars

6. Future Tests

2+1D CONFORMAL SPACETIME DIAGRAM



La Palma cosmic Bell test didn't completely remove causal overlap

POSSIBLE OUTCOMES

Future 2-quasar/CMB Cosmic Bell tests with no causal overlap

Safe Bet

Bell inequalities always violated. Strengthen evidence for quantum theory.

Rule out alternative theories, progressively close freedom-of-choice loophole as much as possible.

Longshot

Experimental results depends on which cosmic sources we look at. Maybe Bell's limit is not violated for very distant sources.

Perhaps experimenter's lack complete freedom!



COSMIC BELL PAPERS

The Shared Causal Pasts and Futures of Cosmological Events,

Friedman, A.S., Kaiser, D.I., and Gallicchio, J. 2013, *Physical Review D*, Vol. 88, Issue 4, id. 044038, 18 pp. ([arXiv:1305.3943](#)) ([DOI](#))

Testing Bell's Inequality with Cosmic Photons: Closing the Setting-Independence Loophole,

Gallicchio, J., **Friedman, A.S.**, and Kaiser, D.I. 2014, *Physical Review Letters*, Vol. 112, Issue 11, id. 110405, 5 pp. ([arXiv:1310.3288](#)) ([DOI](#))

Cosmic Bell Test: Measurement Settings from Milky Way Stars,

Handsteiner, J., **Friedman, A.S.** + 2017, *Physical Review Letters*, Vol. 118, Issue 6, id. 060401, ([arXiv:1611.06985](#) | [PDF](#)) ([DOI](#)) ([Supplemental Material](#))

Astronomical Random Numbers for Quantum Foundations Experiments,

Leung, C., Brown, A., Nguyen, H., **Friedman, A.S.**, Kaiser, D.I., and Gallicchio, J., 2018, *Physical Review A*, Vol. 97, Issue 4, id. 042120 ([arXiv:1706.02276](#)) ([DOI](#)) [Featured in Physics]

Cosmic Bell Test Using Random Measurement Settings from High-Redshift Quasars,

Rauch, D., Handsteiner, J., Hochrainer, A., Gallicchio, J., **Friedman, A.S.** + 2018, *Physical Review Letters*, Vol. 121, Issue 8, id. 080403 ([arXiv:1808.05966](#) | [PDF](#)) ([DOI](#)) ([Supplemental Material](#)) [Editors' Suggestion]

Relaxed Bell Inequalities with Arbitrary Measurement Dependence for Each Observer,

Friedman, A.S., Guth, A.H., Hall, M.J.W., Kaiser, D.I., and Gallicchio, J. 2019, *Physical Review A*, Vol. 99, Issue 1, id. 012121 ([arXiv:1809.01307](#) | [PDF](#)) ([DOI](#))

COSMIC BELL DESIGN CONCEPT

PHYSICAL REVIEW D **88**, 044038 (2013)

The shared causal pasts and futures of cosmological events

Andrew S. Friedman,^{1,*} David I. Kaiser,^{1,†} and Jason Gallicchio^{2,‡}

Friedman, Kaiser, & Gallicchio 2013a, *Phys. Rev. D*, Vol. 88, Iss. 4, id. 044038, 18 p. (arXiv:1305.3943)

Why use quasars? Brightest continuous cosmological sources.

$z > 3.65$ quasars at 180 deg have no shared causal past since inflation

PRL **112**, 110405 (2014)

PHYSICAL REVIEW LETTERS

week ending
21 MARCH 2014

Testing Bell's Inequality with Cosmic Photons: Closing the Setting-Independence Loophole

Jason Gallicchio,^{1,*} Andrew S. Friedman,^{2,†} and David I. Kaiser^{2,‡}

Gallicchio, Friedman, & Kaiser 2014, *Phys. Rev. Lett.*, Vol. 112, Issue 11, id. 110405, (arXiv:1310.3288)

Experiment feasible with existing technology!

$z > 3.65$ quasars bright enough

CMB an intriguing possibility

Summer Science Program, UC San Diego

COSMIC BELL EXPERIMENTS

PRL 118, 060401 (2017)

PHYSICAL REVIEW LETTERS

week ending
10 FEBRUARY 2017



Cosmic Bell Test: Measurement Settings from Milky Way Stars

Johannes Handsteiner,^{1,*} Andrew S. Friedman,^{2,†} Dominik Rauch,¹ Jason Gallicchio,³
Bo Liu,^{1,4} Hannes Hosp,¹ Johannes Kofler,⁵ David Bricher,¹ Matthias Fink,¹ Calvin Leung,³
Anthony Mark,² Hien T. Nguyen,⁶ Isabella Sanders,² Fabian Steinlechner,¹ Rupert Ursin,^{1,7}
Sören Wengerowsky,¹ Alan H. Guth,² David I. Kaiser,²
Thomas Scheidl,¹ and Anton Zeilinger^{1,7,‡}

Handsteiner, Friedman+2017, *Physical Review Letters*, 118, 6, 060401 (arXiv:1611.06985)

Pushed back local hidden variable explanations for entanglement to
> 600 years ago, ~16 orders of magnitude better than previous tests.

PHYSICAL REVIEW LETTERS 121, 080403 (2018)

Editors' Suggestion

Cosmic Bell Test Using Random Measurement Settings from High-Redshift Quasars

Dominik Rauch,^{1,2,*} Johannes Handsteiner,^{1,2} Armin Hochrainer,^{1,2} Jason Gallicchio,³ Andrew S. Friedman,⁴
Calvin Leung,^{1,2,3,5} Bo Liu,⁶ Lukas Bulla,^{1,2} Sebastian Ecker,^{1,2} Fabian Steinlechner,^{1,2} Rupert Ursin,^{1,2}
Beili Hu,³ David Leon,⁴ Chris Benn,⁷ Adriano Ghedina,⁸ Massimo Cecconi,⁸ Alan H. Guth,⁵
David I. Kaiser,^{5,†} Thomas Scheidl,^{1,2} and Anton Zeilinger^{1,2,‡}

Rauch, D. + 2018, *Physical Review Letters*, Vol. 121, Issue 8, id. 080403 (arXiv:1808.05966)

Pushed this back to > 7.8 billion years ago! Excluded 96% of
spacetime that could have causally influenced our experiment!

OTHER RELEVANT PAPERS

PHYSICAL REVIEW A **97**, 042120 (2018)

Featured in Physics

Astronomical random numbers for quantum foundations experiments

Calvin Leung,^{1,*} Amy Brown,^{1,†} Hien Nguyen,^{2,‡} Andrew S. Friedman,^{3,§} David I. Kaiser,^{4,¶} and Jason Gallicchio^{1,**}

Leung+2018, *Physical Review A*, Vol. 97, Issue 4, id. 042120 (arXiv:1706.02276)

Describes an “Astronomical Random Number Generator”, built in Jason Gallicchio’s lab, used to turn cosmic photon colors into random numbers.

PHYSICAL REVIEW A **99**, 012121 (2019)

Relaxed Bell inequalities with arbitrary measurement dependence for each observer

Andrew S. Friedman,^{1,*} Alan H. Guth,^{2,†} Michael J. W. Hall,^{3,4,‡} David I. Kaiser,^{2,§} and Jason Gallicchio^{5,||}

Friedman+2019a, *Physical Review A*, Vol. 99, Issue 1, id. 012121 (arXiv:1809.01307)

Derives relaxed version of Bell’s inequality without the “freedom-of-choice” assumption. Shows local realistic models that can simulate quantum theory by quantitatively reducing freedom by only a minuscule amount.

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