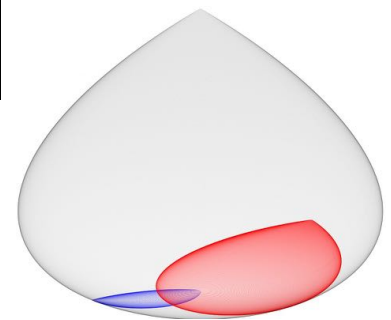
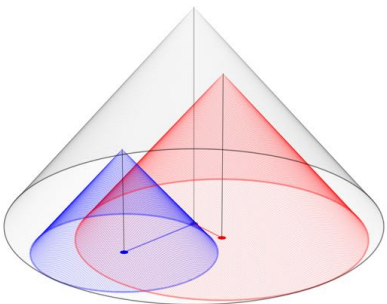


A COSMIC TEST OF QUANTUM ENTANGLEMENT

Choosing Experimental Bell Inequality Measurements with Light from High Redshift Quasars



Dr. Andrew Friedman

UC San Diego

Center for Astrophysics and Space Sciences

<https://asfriedman.physics.ucsd.edu> asf@ucsd.edu



11/30/2018

San Diego State University, Physics and Astronomy Colloquium

COSMIC BELL COLLABORATION



COSMIC BELL TEAM



**Prof. David
Kaiser** ¹



**Dr. Andrew
Friedman** ^{1,5}



**Prof. Alan
Guth** ¹



**Prof. Brian
Keating** ⁵



**Prof. Anton
Zeilinger** ²



**Prof. Jason
Gallicchio** ³

Other Collaborators

Johannes Handsteiner ²,
Dominik Rauch ²,
Dr. Thomas Scheidl ²,
Dr. Johannes Kofler ⁴,
Dr. Hien Nguyen ⁶,
Calvin Leung ³
et al.



UCSD



1: MIT Physics/CTP

2: Vienna IQOQI

3: Harvey Mudd

4: Max Planck MPQ

5: UCSD CASS

6: NASA JPL/Caltech



FEYNMAN ON FREE WILL

“We have an illusion that we can do any experiment that we want. We all, however, come from the same universe, have evolved with it, and don't really have any `real' freedom. For we obey certain laws and have come from a certain past. Is it somehow that we are correlated to the experiments that we do, so that the apparent probabilities don't look like they ought to look if you assume they are random...”

– **Richard Feynman 1982**

OUTLINE

1. Entanglement Tests

2. Bell's Inequality vs. Bell's Theorem

3. Loopholes / Freedom-Of-Choice Loophole

4. Cosmic Bell Test with Milky Way Stars

5. Cosmic Bell Test with Quasars

6. Future Tests

QUANTUM ENTANGLEMENT

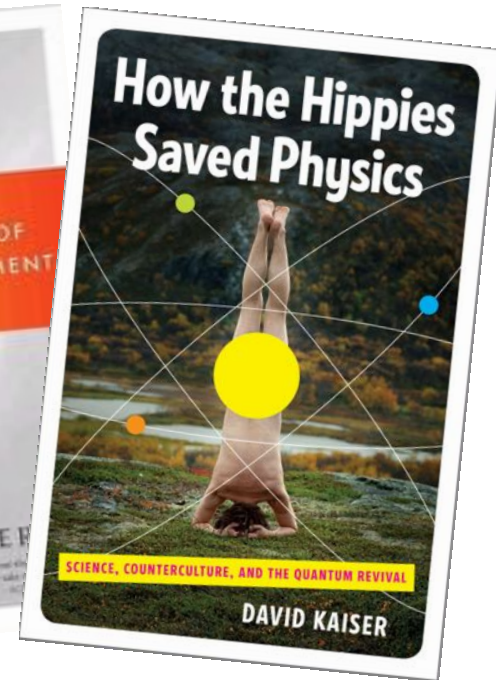
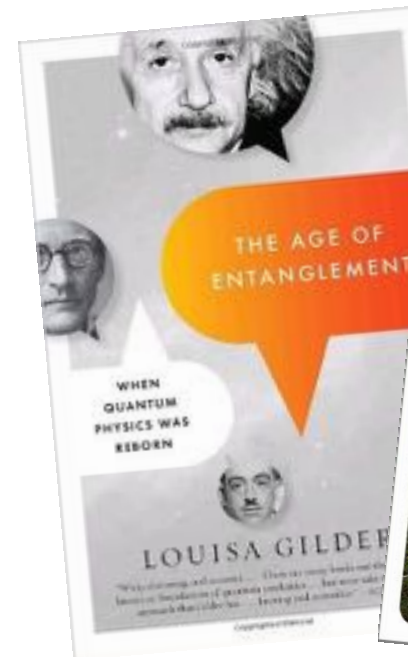
Beginning in the 1930s, the great architects of quantum theory struggled to understand the notion of “entanglement.”



Niels Bohr and
Albert Einstein



Erwin Schrödinger



EPR PARADOX



A. Einstein

E



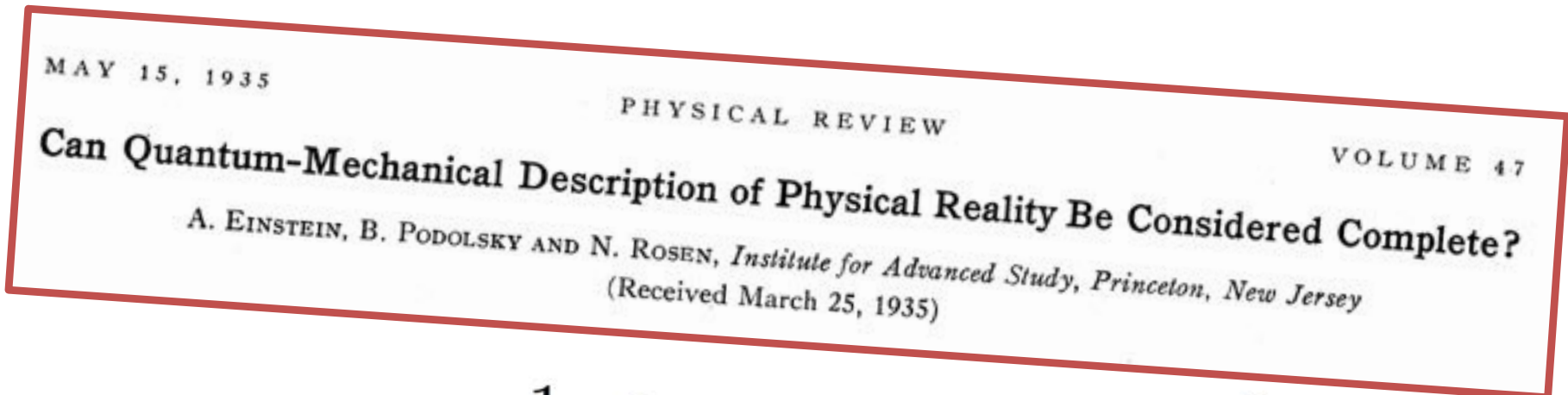
B. Podolsky

P



N. Rosen

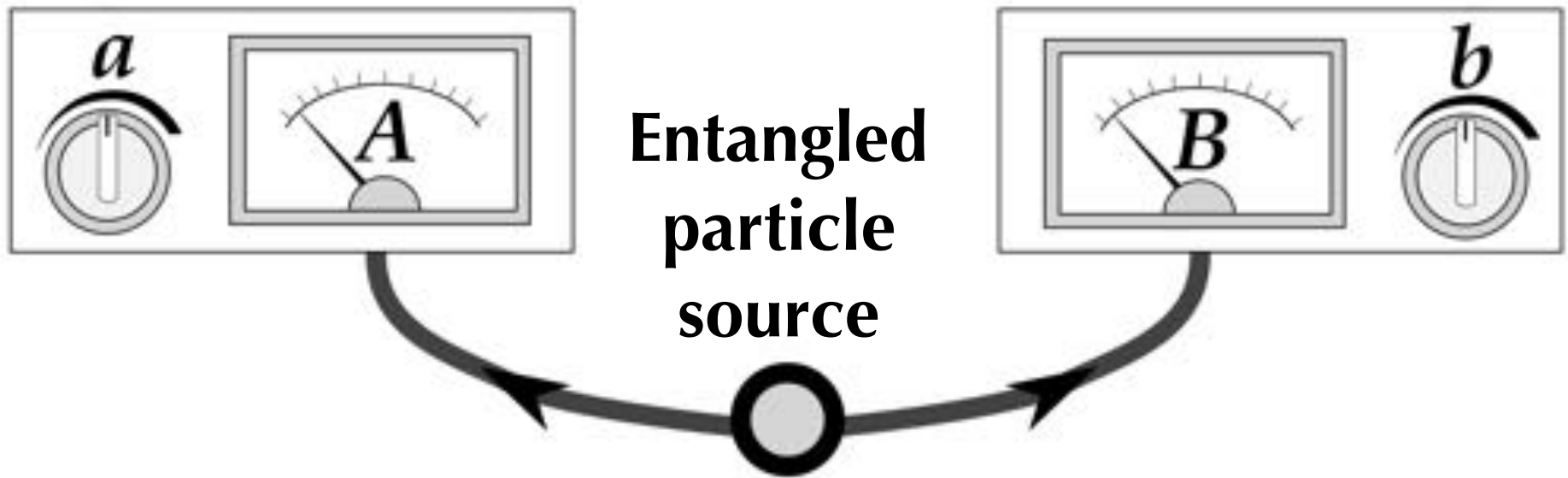
R



$$|\psi\rangle = \frac{1}{\sqrt{2}} \left\{ |u_1\rangle |v_2\rangle + |u_2\rangle |v_1\rangle \right\}$$

State does not factorize: no way to describe behavior of particle 1 (u) without referring to behavior of particle 2 (v).

BELL TESTS



a, b : Settings

A, B : Outcomes

Big question: Are non-quantum explanations for entanglement viable?

If yes, QM incomplete \rightarrow *Hidden variables*

OUTLINE

1. Entanglement Tests

2. Bell's Inequality vs. Bell's Theorem

3. Loopholes / Freedom-Of-Choice Loophole

4. Cosmic Bell Test with Milky Way Stars

5. Cosmic Bell Test with Quasars

6. Future Tests

BELL'S INEQUALITY ASSUMPTIONS

1. Realism
2. Locality
3. Freedom



http://images.iop.org/objects/ccr/cern/54/7/19/CCfac8_07_14.jpg

John S. Bell (1928-1990)

1,2,3 → **Bell's Inequality**

Upper limits on entangled particle measurement correlations in a “**local-realist**” model

RELAXING BELL'S ASSUMPTIONS

1. Realism
2. Locality
3. Freedom

Experiments violate Bell's inequality as predicted by quantum mechanics!



→ **At least one of 1,2,3 are false!**

But relaxing any assumption → **LOOPHOLES**

Alternative models could mimic quantum theory

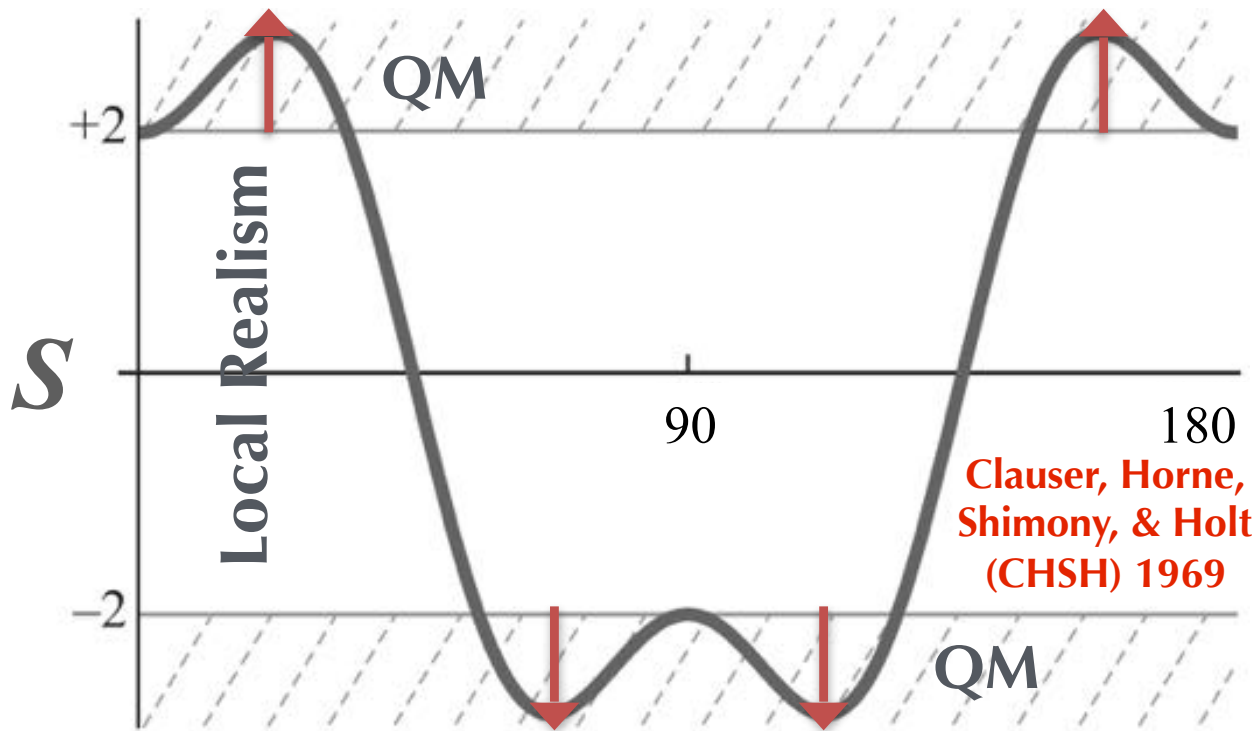
CORRELATIONS AT A DISTANCE

correlation function: $E(a,b) = \langle A B \rangle$

$$S = E(a, b) + E(a', b) + E(a, b') - E(a', b')$$

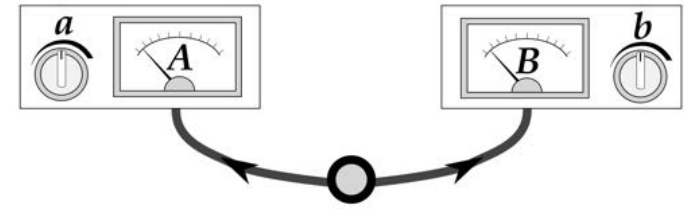
Bell: if $p(A, B|a, b) = \int d\lambda p(\lambda) \underbrace{p(A|a, \lambda)} p(B|b, \lambda)$

then $|S| \leq 2$. Locality: A does not depend on b or B, and vice versa.)



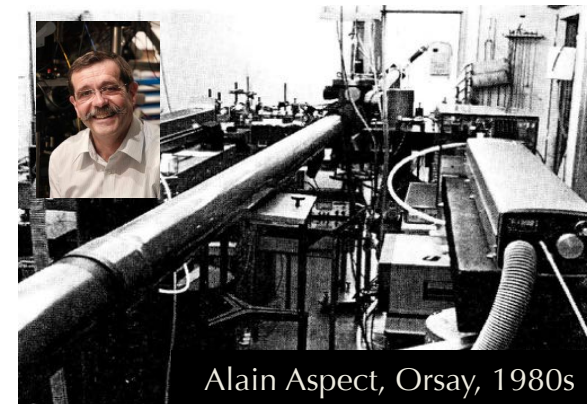
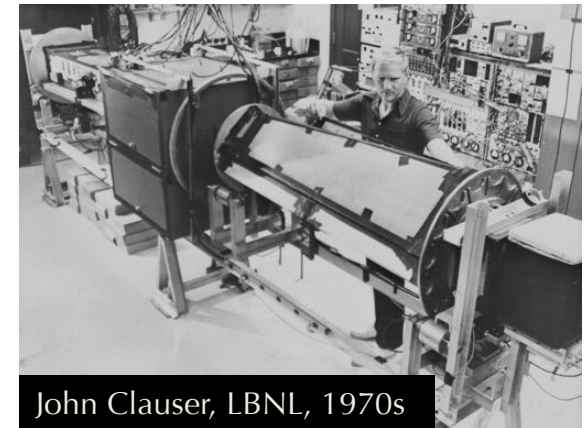
Angle Between Polarizers

Clauser, Horne,
Shimony, & Holt
(CHSH) 1969



QM prediction: $|S_{\max}| = 2\sqrt{2}$

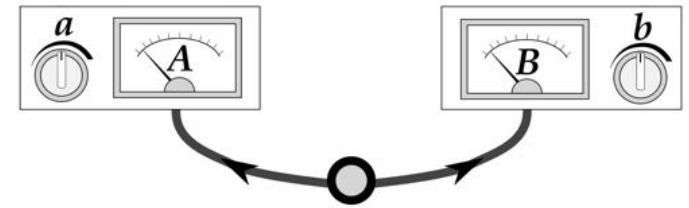
Dozens of experiments: $|S_{\max}| > 2$



BELL'S INEQUALITY

correlation function: $E(a,b) = \langle A B \rangle$

$$S = E(a, b) + E(a', b) + E(a, b') - E(a', b')$$



Bell: if $p(A, B|a, b) = \int d\lambda p(\lambda) \underbrace{p(A|a, \lambda)} p(B|b, \lambda)$

then $|S| \leq 2$. Locality: A does not depend on b or B, and vice versa.)

- **Bell's inequality:** $|S| \leq 2$ Places limits on how correlated measurement outcomes can be in local realistic theories.
- It says nothing directly about quantum mechanics!
- Until you compare it to quantum theory as a benchmark

BELL'S THEOREM

No local-realist theory can reproduce the quantum predictions!

e.g. QM prediction: $|S_{\max}| = 2\sqrt{2}$

OUTLINE

1. Entanglement Tests

2. Bell's Inequality vs. Bell's Theorem

3. Loopholes / Freedom-Of-Choice Loophole

4. Cosmic Bell Test with Milky Way Stars

5. Cosmic Bell Test with Quasars

6. Future Tests

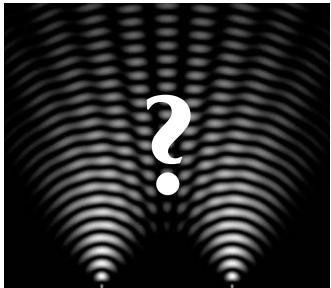
LOOPHOLES & WHY THEY MATTER

The standard interpretation of Bell tests — that “local realism” is incompatible with experiment — relies upon several assumptions.

So What?!

Quantum foundations!

Understanding reality at a deep level. If universe exploits loopholes, does not mean QM is “wrong”, but perhaps derived from a more fundamental underlying theory. Quantum gravity?



Quantum cryptography security

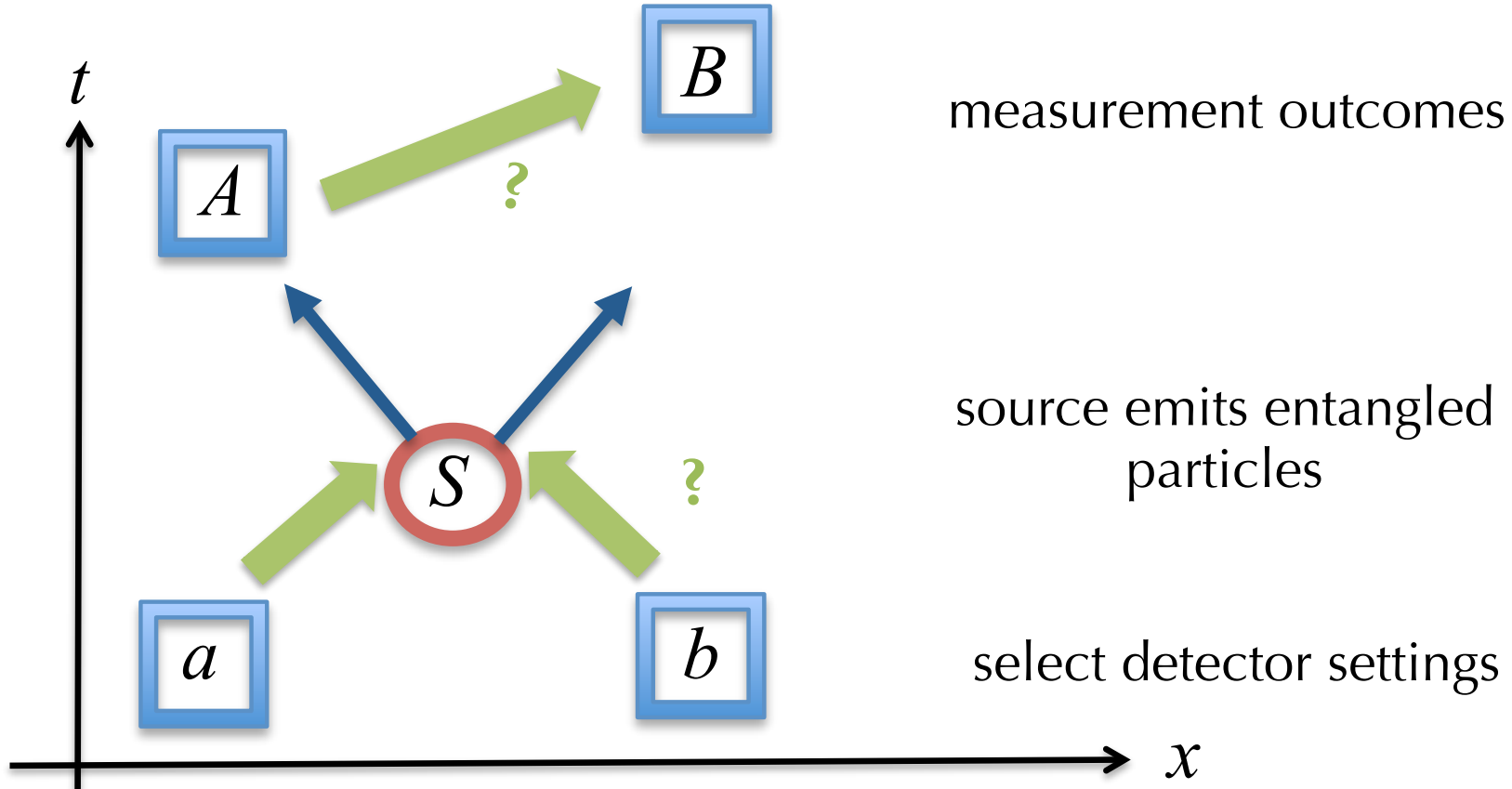
Tech applications! Hackers could exploit loopholes to undermine entanglement-based quantum information schemes



LOCALITY LOOPHOLE

The standard interpretation of Bell tests — that “local realism” is incompatible with experiment — relies upon several assumptions.

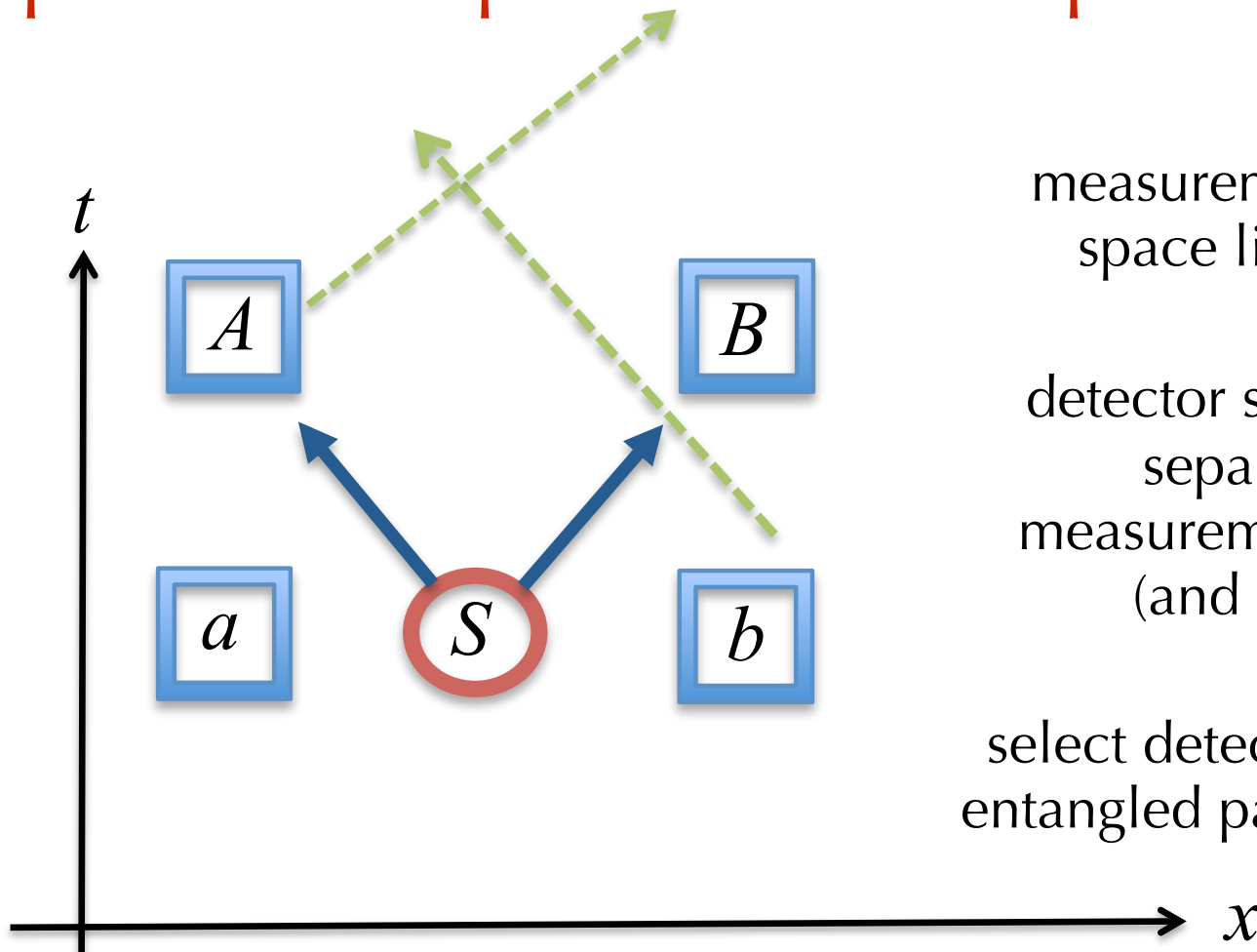
Hidden communication between parties?



CLOSING THE LOCALITY LOOPHOLE

The standard interpretation of Bell tests — that “local realism” is incompatible with experiment — relies upon several assumptions.

Space-like separate relevant pairs of events



measurement outcomes
space like separated

detector setting choice a
separated from
measurement outcome B
(and vice versa)

select detector settings while
entangled particles are in flight

DETECTION EFFICIENCY LOOPHOLE

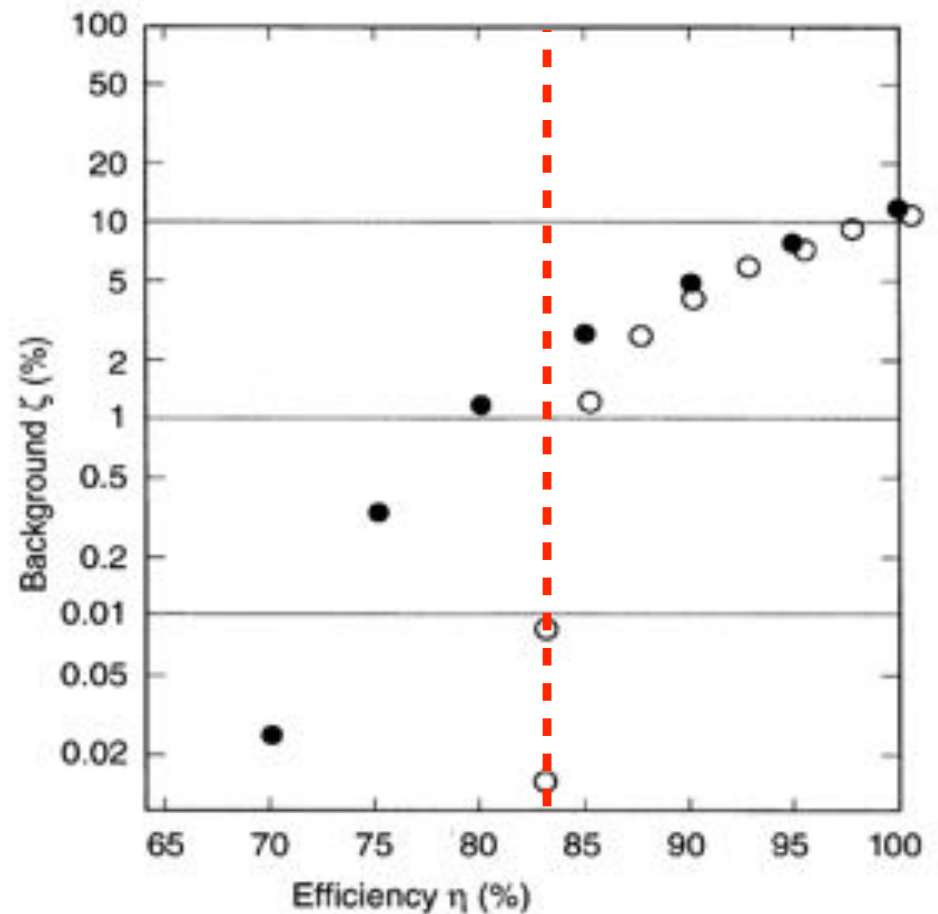
The standard interpretation of Bell tests — that “local realism” is incompatible with experiment — relies upon several assumptions.

Also called the “fair-sampling” loophole

No detectors are 100% efficient.

What if undetected photons skewed the statistics, faking Bell violation without genuine entanglement?

Closing loophole requires detector efficiencies $\geq 83\%$



Garg and Mermin, *Phys Rev D* (1987), Eberhard, *Phys Rev A* (1993)

TOWARD A LOOPHOLE FREE TEST

A. Locality Loophole

Hidden communication between parties

CLOSED

for photons: **Aspect+1982, Weihs+1998**

Closing Method?

Spacelike separated
measurements, settings

B. Detection Loophole

Measured sub-sample not representative

CLOSED

for atoms: **Rowe+2001**, superconducting qubits:

High efficiency
detectors

Ansmann+2009, photons: **Giustina+2013, Christensen+2013**

2 LOOPHOLES IN SAME TEST!

CLOSED

Locality & Detection

Hensen+2015 (Delft) (electrons)

Giustina+2015 (Vienna)

Shalm+2015 (NIST) (photons)

Rosenfeld+2017 (Germany) (atoms)

TOWARD A LOOPHOLE FREE TEST

C. Freedom-of-Choice Loophole

Settings correlated with hidden variables

 partially for photons: **Scheidl+2010**

**Settings spacelike
separated from
EPR source**

COSMIC BELL TESTS

Locality & Freedom (photons)





Handsteiner+2017 (Vienna)
*Settings chosen with Milky Way Stars. Closed locality,
constrained freedom-of-choice to ~600 years ago.*

Locality & Freedom (photons)





Rauch+2018 (Canary Islands)
*Settings from High Redshift Quasars. Closed locality,
constrained freedom-of-choice to ~7.8 Billion years ago!*

Locality & Detection & Freedom (photons)







Li+2018 (China)
*Closed locality and detection, constrained
freedom-of-choice to ~11 years ago.*

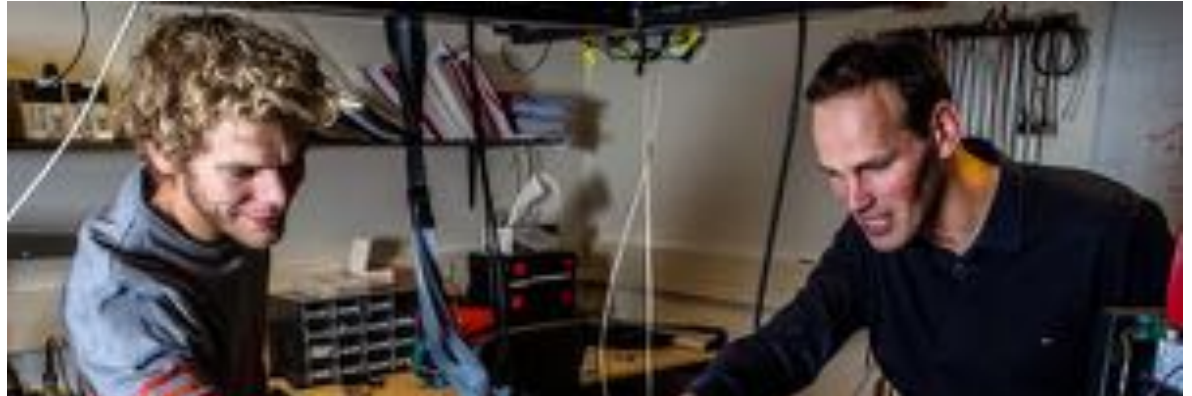
LATEST EXPERIMENTS

DELFT

Loophole-free Bell inequality violation using electron spins separated by 1.3 kilometres

B. Hensen^{1,2}, H. Bernien^{1,2,†}, A. E. Dréau^{1,2}, A. Reiserer^{1,2}, N. Kalb^{1,2}, M. S. Blok^{1,2}, J. Ruitenberg^{1,2}, R. F. L. Vermeulen^{1,2}, R. N. Schouten^{1,2}, C. Abellán³, W. Amaya³, V. Pruneri^{3,4}, M. W. Mitchell^{3,4}, M. Markham⁵, D. J. Twitchen⁵, D. Elkouss¹, S. Wehner¹, T. H. Taminiau^{1,2} & R. Hanson^{1,2}

The New York Times



Sorry, Einstein. Quantum Study Suggests 'Spooky Action' Is Real.

By JOHN MARKOFF OCT. 21, 2015



First experiment to close *both* the locality and detection loopholes.

VIENNA LATEST EXPERIMENTS

PRL 115, 250401 (2015)

Selected for a Viewpoint in *Physics*
PHYSICAL REVIEW LETTERS

week ending
18 DECEMBER 2015

Significant-Loophole-Free Test of Bell's Theorem with Entangled Photons

Marissa Giustina,^{1,2,*} Marijn A. M. Versteegh,^{1,2} Sören Wengerowsky,^{1,2} Johannes Handsteiner,^{1,2} Armin Hochrainer,^{1,2} Kevin Phelan,¹ Fabian Steinlechner,¹ Johannes Kofler,³ Jan-Åke Larsson,⁴ Carlos Abellán,⁵ Waldimar Amaya,⁵ Valerio Pruneri,^{5,6} Morgan W. Mitchell,^{5,6} Jörn Beyer,⁷ Thomas Gerrits,⁸ Adriana E. Lita,⁸ Lynden K. Shalm,⁸ Sae Woo Nam,⁸ Thomas Scheidl,^{1,2} Rupert Ursin,¹ Bernhard Wittmann,^{1,2} and Anton Zeilinger^{1,2,†}

¹Institute for Quantum Optics and Quantum Information (IQOQI), Austrian Academy of Sciences, Boltzmannstr. 8, 1090 Vienna, Austria

²Quantum Optics, Quantum Nanophysics, University of Vienna, Boltzmannstr. 8, 1090 Vienna, Austria

³Max-Planck-Institute of Quantum Optics, Boltzmannstr. 8, 1090 Vienna, Austria

⁴Institutionen för Systemteori, Luleå University of Technology, Luleå, Sweden

⁵ICFO – Institut de Ciències Fotoniques, The Barcelona Institute of Science and Technology, C/Mar de la Plana 37, 08860 Castelldefels (Barcelona), Spain

⁶ICREA – Institució Catalana de Recerca i Innovació Tecnològica, C/Mar de la Plana 37, 08860 Castelldefels (Barcelona), Spain

⁷Physikalisch-Technische Bundesanstalt, Bundesallee 115, 38115 Braunschweig, Germany

⁸National Institute of Standards and Technology, Gaithersburg, Maryland 20899, USA

(Received 10 November 2015; published 16 December 2015)

PRL 115, 250402 (2015)

Selected for a Viewpoint in *Physics*
PHYSICAL REVIEW LETTERS

week ending
18 DECEMBER 2015

Strong Loophole-Free Test of Local Realism*

Lynden K. Shalm,^{1,†} Evan Meyer-Scott,² Bradley G. Christensen,³ Peter Bierhorst,¹ Michael A. Wayne,^{3,4} Martin J. Stevens,¹ Thomas Gerrits,¹ Scott Glancy,¹ Deny R. Hamel,⁵ Michael S. Allman,¹ Kevin J. Coakley,¹ Shellee D. Dyer,¹ Carson Hodge,¹ Adriana E. Lita,¹ Varun B. Verma,¹ Camilla Lambrocco,¹ Edward Tortorici,¹ Alan L. Migdall,^{4,6} Yanbao Zhang,² Daniel R. Kumor,³ William H. Farr,⁷ Francesco Marsili,⁷ Matthew D. Shaw,⁷ Jeffrey A. Stern,⁷ Carlos Abellán,⁸ Waldimar Amaya,⁸ Valerio Pruneri,^{8,9} Thomas Jennewein,^{2,10} Morgan W. Mitchell,^{8,9} Paul G. Kwiat,³ Joshua C. Bienfang,^{4,6} Richard P. Mirin,¹ Emanuel Knill,¹ and Sae Woo Nam^{1,‡}

¹National Institute of Standards and Technology, 325 Broadway, Boulder, Colorado 80305, USA

²Institute for Quantum Computing and Department of Physics and Astronomy, University of Waterloo, 200 University Avenue West, Waterloo, Ontario, Canada, N2L 3G1

³Department of Physics, University of Illinois at Urbana-Champaign, Urbana, Illinois 61801, USA

⁴National Institute of Standards and Technology, 100 Bureau Drive, Gaithersburg, Maryland 20899, USA

⁵Département de Physique et d'Astronomie, Université de Moncton, Moncton, New Brunswick E1A 3E9, Canada

⁶Technology and University of Maryland, 100 Bureau Drive, Gaithersburg, Maryland 20899, USA

⁷4800 Oak Grove Drive, Pasadena, California 91109, USA

⁸National Institute of Standards and Technology, 08860 Castelldefels (Barcelona), Spain

⁹ICREA – Institució Catalana de Recerca i Innovació Tecnològica, C/Mar de la Plana 37, 08860 Castelldefels (Barcelona), Spain

¹⁰Institute for Advanced Research, Toronto, Ontario, Canada

(Received 10 November 2015; published 16 December 2015)

Closed both locality and detection loopholes for the first time *with photons*

NIST

LATEST EXPERIMENTS

PRL 115, 250401 (2015) week ending
18 DECEMBER 2015

Selected for a Viewpoint in *Physics*
PHYSICAL REVIEW LETTERS

Significant-Loophole-Free Test of Bell's Theorem with Entangled Photons

Marissa Giustina,^{1,2,*} Marijn A. M. Versteegh,^{1,2} Sören Wengerowsky,^{1,2} Johannes Handsteiner,^{1,2} Armin Hochrainer,^{1,2} Kevin Phelan,¹ Fabian Steinlechner,¹ Johannes Kofler,³ Jan-Åke Larsson,⁴ Carlos Abellán,⁵ Waldimar Amaya,⁵ Valerio Pruneri,^{5,6} Morgan W. Mitchell,^{5,6} Jörn Beyer,⁷ Thomas Gerrits,⁸ Adriana E. Lita,⁸ Lynden K. Shalm,⁸ Sae Woo Nam,⁸ Thomas Scheidl,^{1,2} Rupert Ursin,¹ Bernhard Wittmann,^{1,2} and Anton Zeilinger^{1,2,†}

¹Institute for Quantum Optics and Quantum Information (IQOQI), Austrian Academy of Sciences, Boltzmannngasse 3, Vienna 1090, Austria

²Quantum Optics, Quantum Nanophysics and Quantum Information, Faculty of Physics, University of Vienna, Boltzmannngasse 5, Vienna 1090, Austria

³Max-Planck-Institute of Quantum Optics, Hans-Kopfermann-Strasse 1, 85748 Garching, Germany

⁴Institutionen för Systemteknik, Linköpings Universitet, 581 83 Linköping, Sweden

⁵ICFO – Institut de Ciències Fotoniques, The Barcelona Institute of Science and Technology, 08860 Castelldefels, Barcelona, Spain

⁶ICREA – Institució Catalana de Recerca i Estudis Avançats, 08015 Barcelona, Spain

⁷Physikalisch-Technische Bundesanstalt, Abbestr. 1, 10587 Berlin, Germany

⁸NIST, 375 Broadway, Boulder, Colorado 80305, USA

VIENNA



HOFBURG PALACE, VIENNA



HOFBURG PALACE BASEMENT



RECENT ENTANGLEMENT TESTS

- Closed “locality” and “detection” loopholes simultaneously
Hensen+2015 (Delft), Giustina+2015 (Vienna), Shalm+2015 (NIST), Rosenfeld+2017 (Germany)
- None of these tests designed to fully address “freedom-of-choice” loophole
- Cosmic Bell tests will progressively attempt to do so

FREEDOM OF CHOICE LOOPHOLE

QM is most vulnerable to the “freedom-of-choice” loophole*:
Are the detector settings correlated with the local hidden variable?

$$p(A, B|a, b) = \int d\lambda \underbrace{p(A, B|a, b, \lambda)}_{\text{equivalent to}} \underbrace{p(\lambda|a, b)}_{\text{Bell explicitly assumed}}$$

$p(\lambda|a, b) = p(\lambda)$

$p(a, b|\lambda) = p(a, b)$

Bell: “It has been assumed that the settings of instruments are in some sense free variables — say at the whim of the experimenters — or in any case not determined in the overlap of the backward light cones.” (1976)

locality assumption $p(A, B|a, b, \lambda) = p(A|a, \lambda)p(B|b, \lambda)$

*Also known as the “measurement-independence” and “settings-independence” loophole.

RELAXING FREEDOM OF CHOICE

If we do *not* assume $p(\lambda|a, b) = p(\lambda)$, then local-realist models would be compatible with

$$|S| \leq 2 + M_1 + M_2 + \min\{M_1, M_2\}$$

where

$$M_1 = \max\left\{ \int d\lambda |p(\lambda|x, y) - p(\lambda|x', y)|, \int d\lambda |p(\lambda|x, y') - p(\lambda|x', y')| \right\}$$

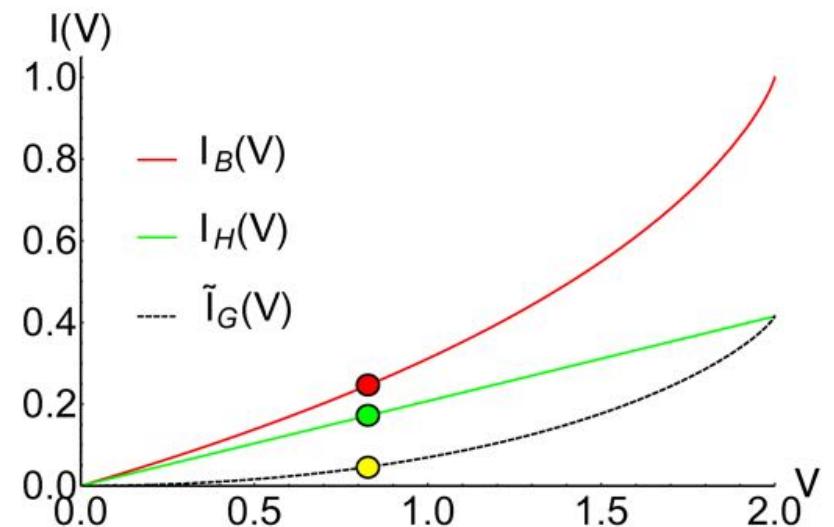
$$M_2 = \max\left\{ \int d\lambda |p(\lambda|x, y) - p(\lambda|x, y')|, \int d\lambda |p(\lambda|x', y) - p(\lambda|x', y')| \right\}$$

A *minuscule* amount of correlation between λ and a, b would suffice to mimic QM, with $|S| \rightarrow 2\sqrt{2}$.

Mutual Information

$$I = \sum_{\lambda, a, b} p(\lambda|a, b) p(a, b) \log_2 \frac{p(\lambda|a, b)}{p(\lambda)}$$

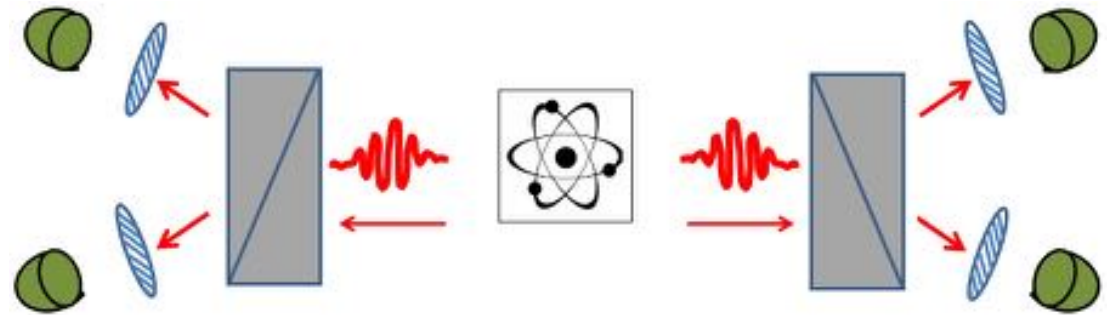
Only require $I = 0.046 \sim 1/22$ of a bit!



Friedman, Guth, Hall, Kaiser, Gallicchio, 1809.01307

FREEDOM OF CHOICE LOOPHOLE

X Shrimp & Chicken Fajita	\$12.99
X Fajita Salsas (for One) <i>A Combination of steak, chicken & shrimp.</i>	\$13.25
Fajita Salsas (for Two)	\$21.99
Fajita Mixed <i>Strips of steak & chicken.</i>	\$12.25
Fajita Mixed (for Two)	\$19.50
Fajita Quesadilla <i>2 flour tortillas grilled & stuffed with chicken or steak & cheese.</i>	\$ 9.50
X Shrimp Fajitas	\$14.25
Fajitas <i>Steak or Chicken</i> for One	\$11.99
for Two	\$18.99
X Parillada Mexicana (for One) <i>Pork tips, shrimp, chicken, chorizo & steak.</i>	\$13.99
X Parillada Mexicana (for Two)	\$22.99



If detector settings depend on hidden variables λ from past events, our choices might not be perfectly free!

Still have free will!

But limited freedom

<http://salsasmexrestaurants.com/test/wp-content/uploads/2014/11/Fajitascombos.jpg>

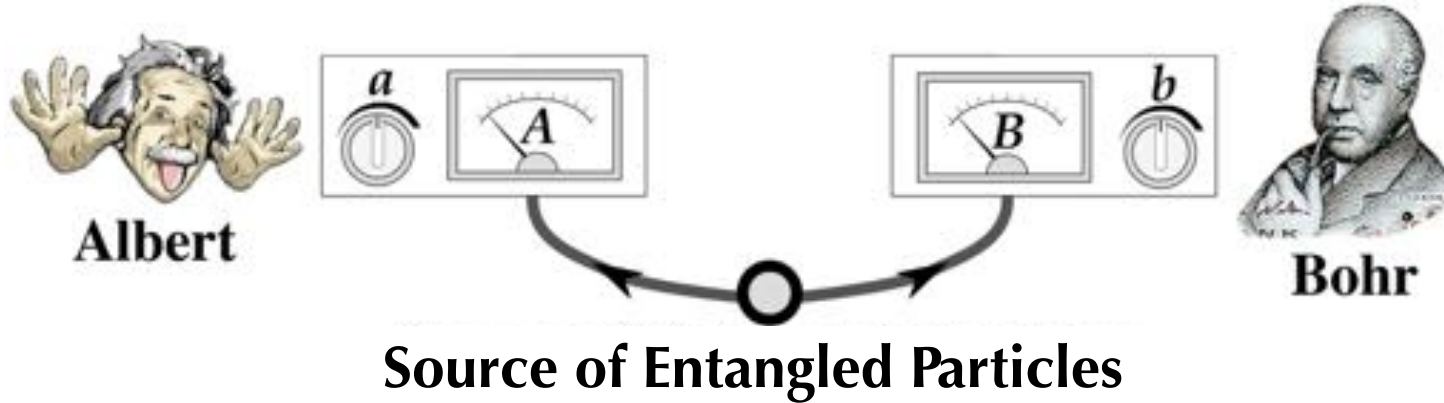
ADDRESSING FREEDOM OF CHOICE

- If we don't simply assume $p(\lambda|a, b) = p(\lambda)$, how might we address the “freedom-of-choice” assumption experimentally?
- Most recent experiments used QRNGs to select detector settings.
- Such devices produce output strings based on some physical process.
- *According to QM*, the outputs should be intrinsically random.



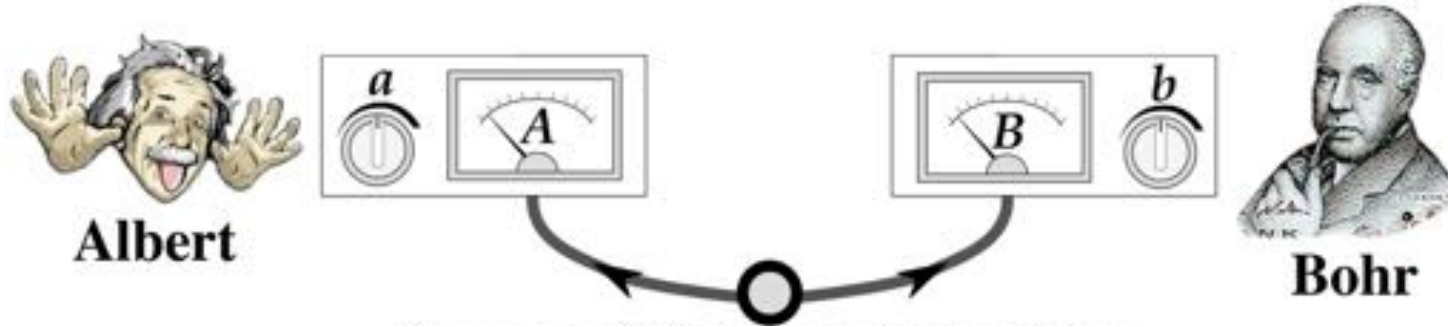
But the purported intrinsic randomness of QM is part of what is *at stake* in tests of Bell's inequality...

CHOOSING DETECTOR SETTINGS

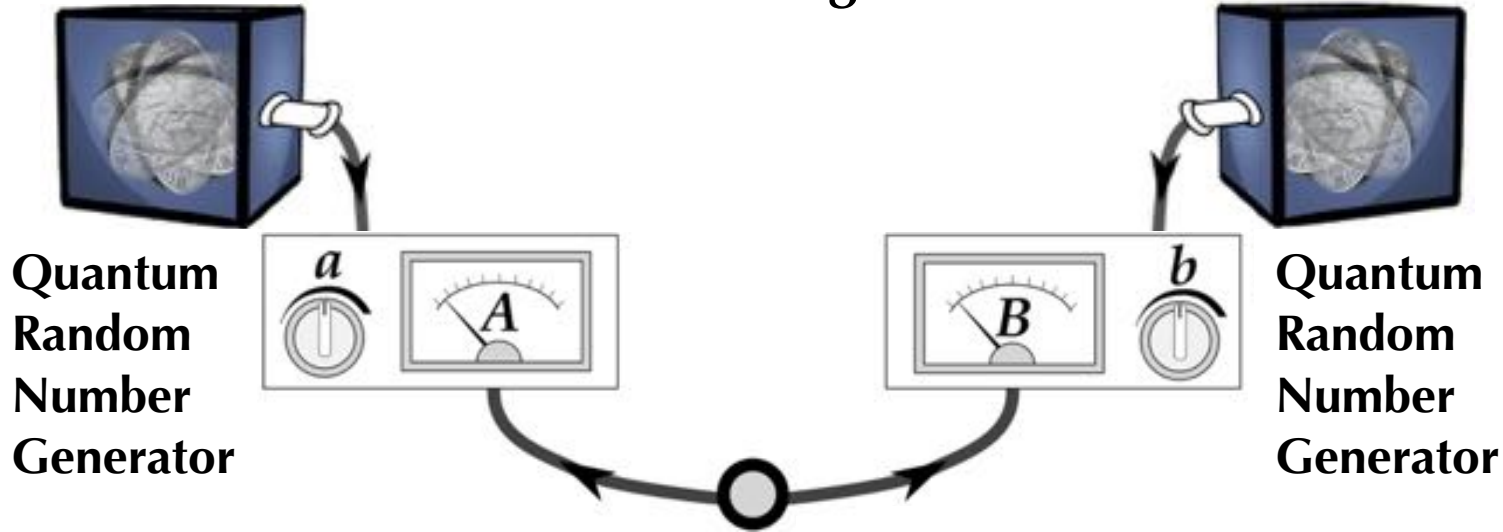


Adapted from:
Gallicchio, Friedman,
& Kaiser 2014

CHOOSING DETECTOR SETTINGS

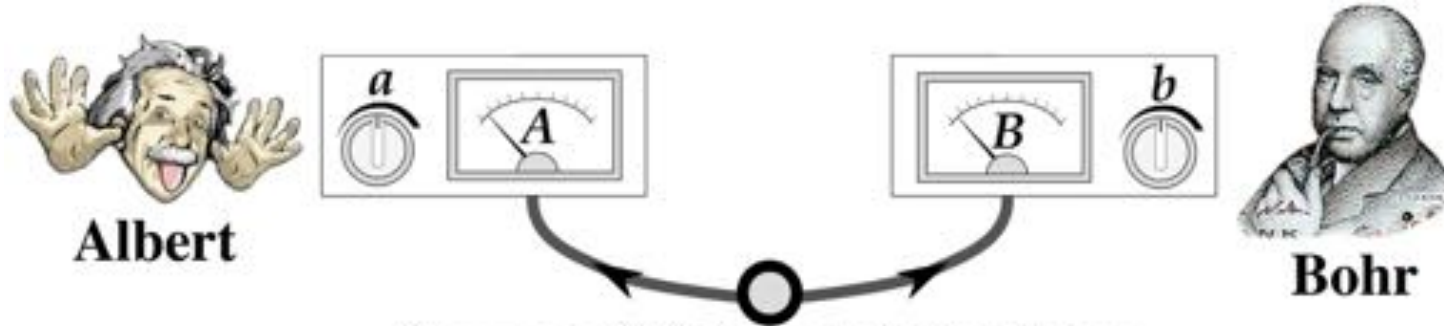


Source of Entangled Particles



Adapted from:
Gallicchio, Friedman,
& Kaiser 2014

CHOOSING DETECTOR SETTINGS

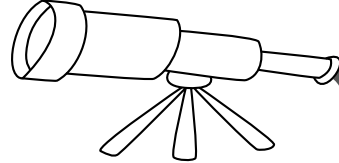


Source of Entangled Particles

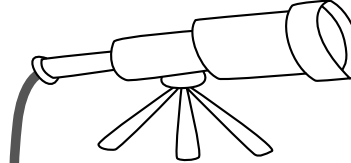
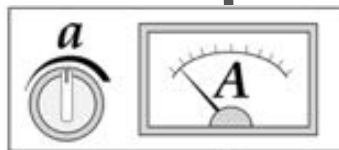


Quantum Random Number Generator

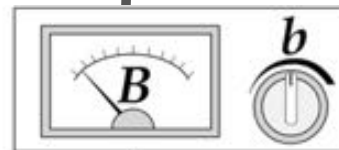
Quantum Random Number Generator



Star A



Star B

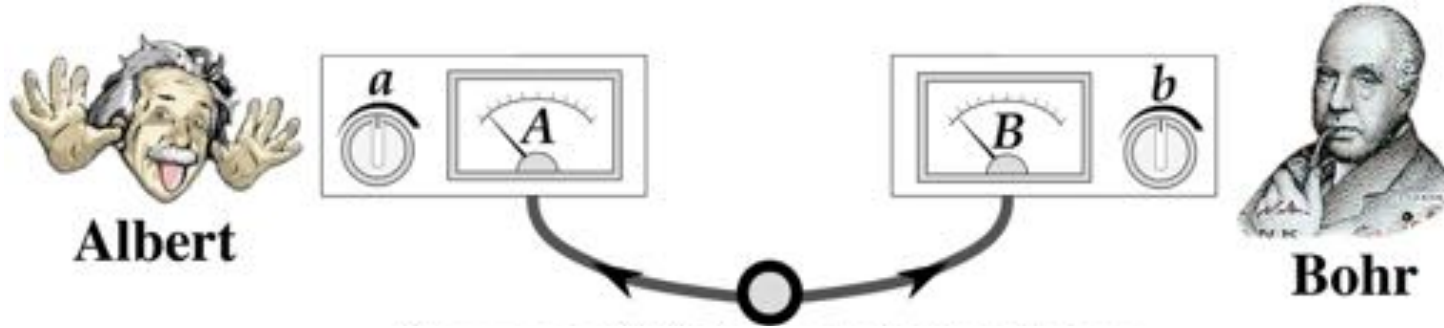


Choose settings with real-time observations of distant Milky Way stars

Requires alternative theories to act hundreds or thousands of years ago

Adapted from: Gallicchio, Friedman, & Kaiser 2014

CHOOSING DETECTOR SETTINGS



Source of Entangled Particles

Choose settings with observations of **high redshift cosmic sources**

Relegates alternatives to billions of years ago!



Quantum Random Number Generator

Quantum Random Number Generator



*

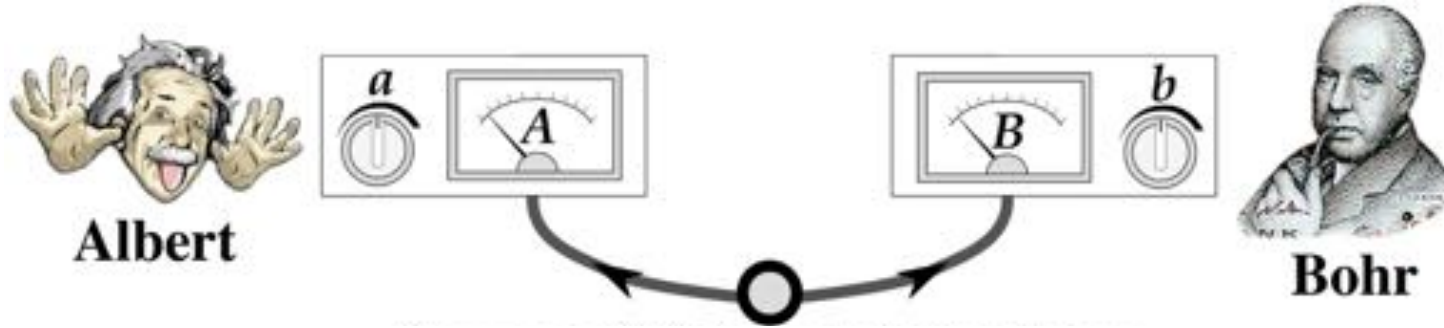
*

Quasar B

Quasar A

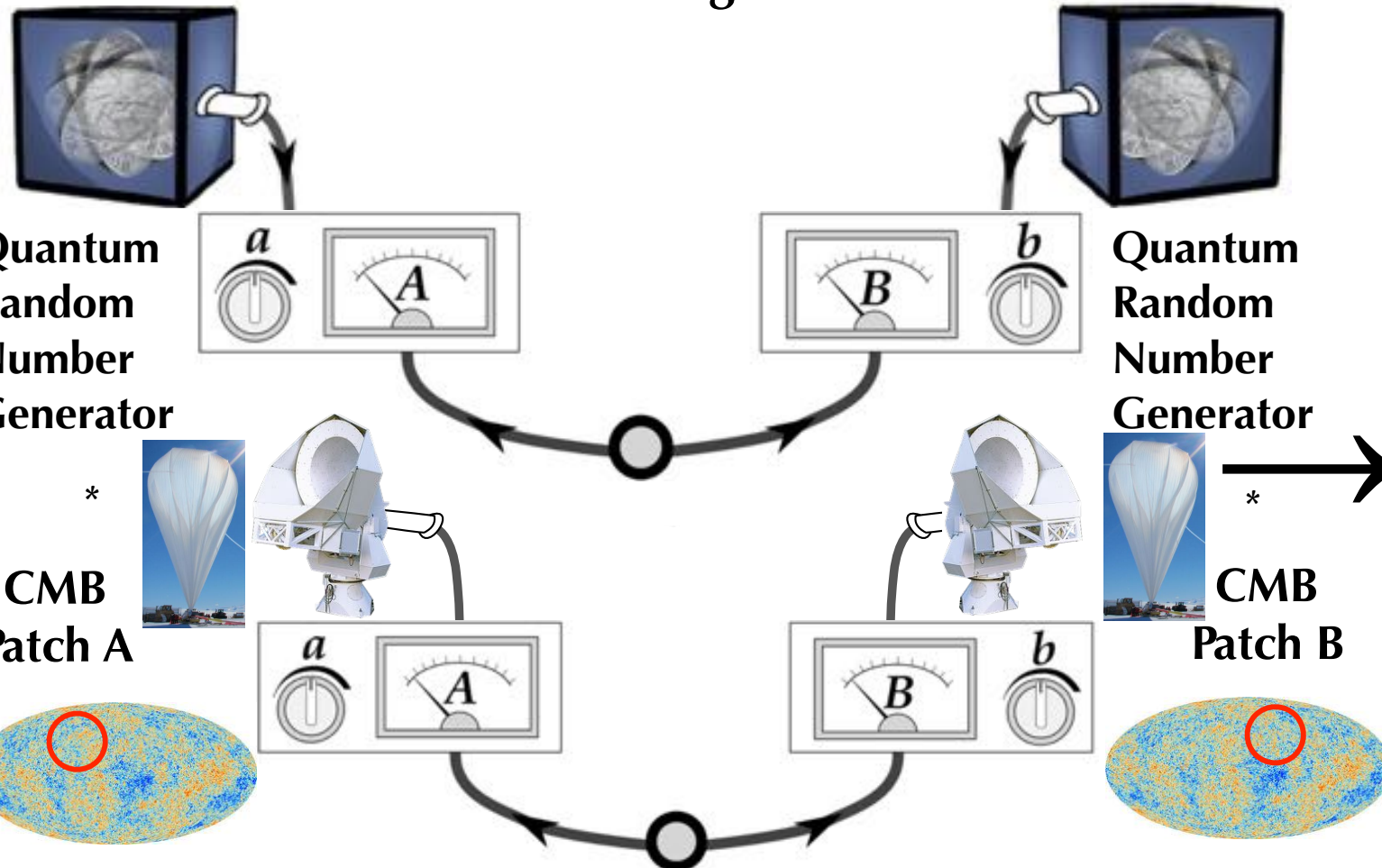


CHOOSING DETECTOR SETTINGS



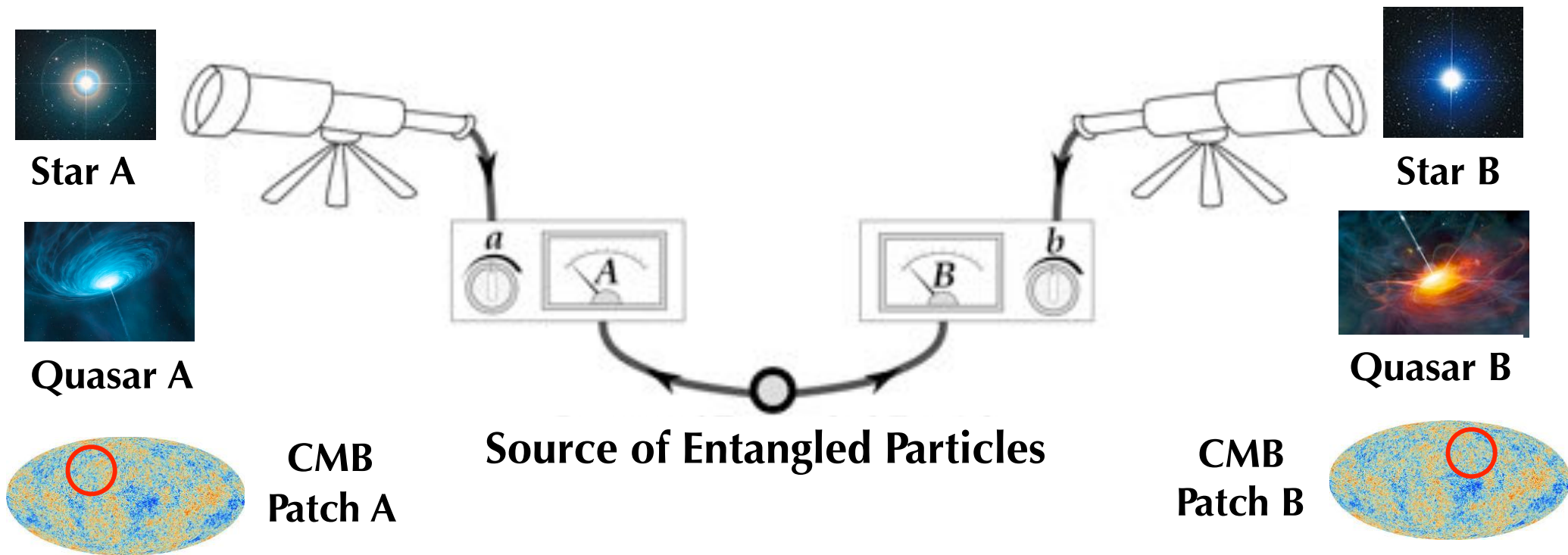
Choose settings with observations of **CMB** patches, etc...

Relegates alternatives to Big Bang, era of early universe inflation!



Adapted from:
Gallicchio, Friedman,
& Kaiser 2014

COSMIC BELL TESTS



Let the Universe decide how to set up entanglement experiment!

Set a, b by using astronomical sources as cosmic random number generators

Gallicchio, Friedman, & Kaiser 2014, Phys. Rev. Lett., Vol. 112, Issue 11, id. 110405, (arXiv:1310.3288)

OUTLINE

1. Entanglement Tests

2. Bell's Inequality vs. Bell's Theorem

3. Loopholes / Freedom-Of-Choice Loophole

4. Cosmic Bell Test with Milky Way Stars

5. Cosmic Bell Test with Quasars

6. Future Tests

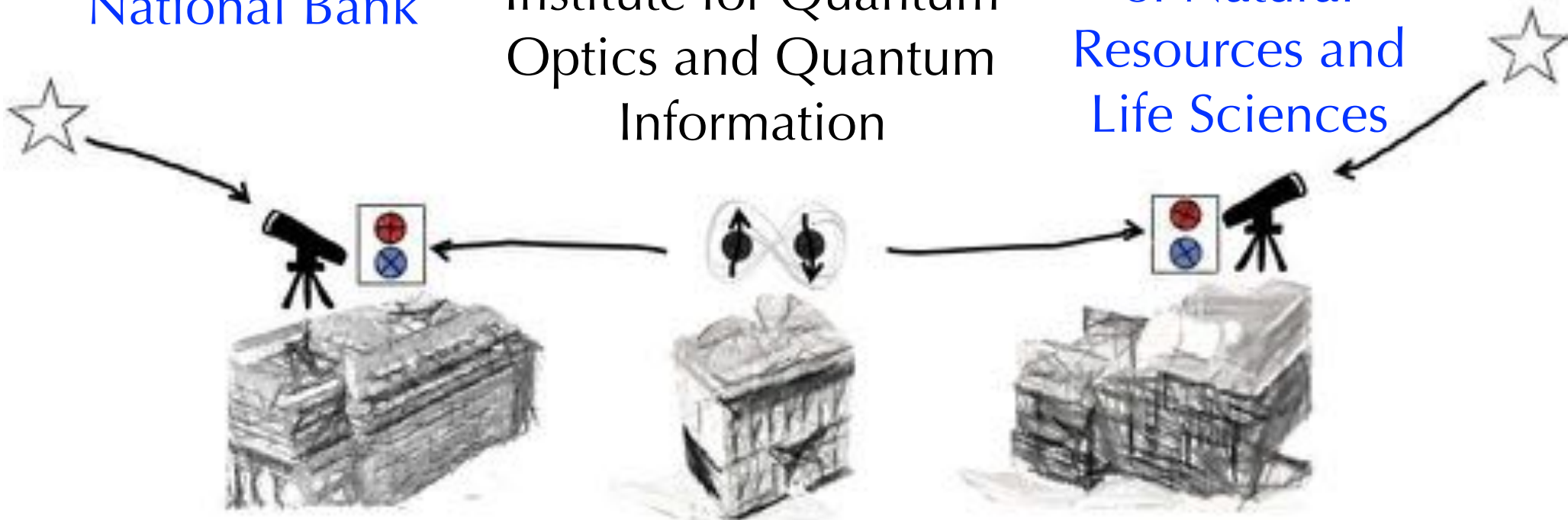
FIRST COSMIC BELL TEST (VIENNA)



Alice: Austrian National Bank

Entangled Particles:
Institute for Quantum Optics and Quantum Information

Bob: University of Natural Resources and Life Sciences



Handsteiner, Friedman+2017 (arXiv:1611.06985)

VIENNA COSMIC BELL TEST



Johannes Handsteiner
with 8-inch stellar
photon telescope



Image Credit: Jason Gallicchio

VIENNA COSMIC BELL TEST



Entangled photon
receiver and
polarization analyzer



Image Credit: Jason Gallicchio

COSMIC SETTING GENERATOR

Red Arm

Guide Camera

Blue Arm



Light In



Credit: Jason Gallicchio, Amy Brown, Calvin Leung (HMC)

VIENNA COSMIC BELL TEST



Occupational Hazards

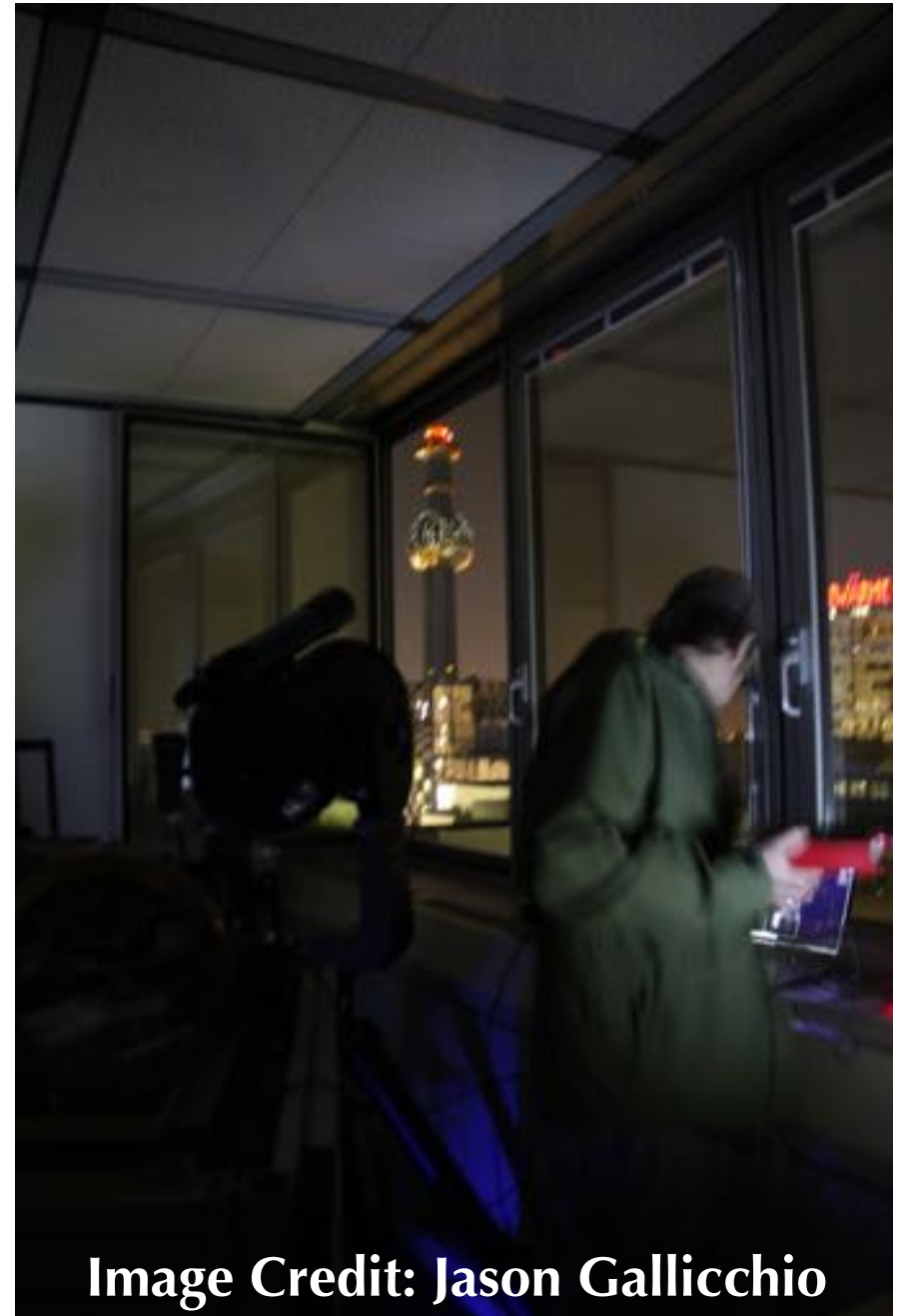


Image Credit: Jason Gallicchio

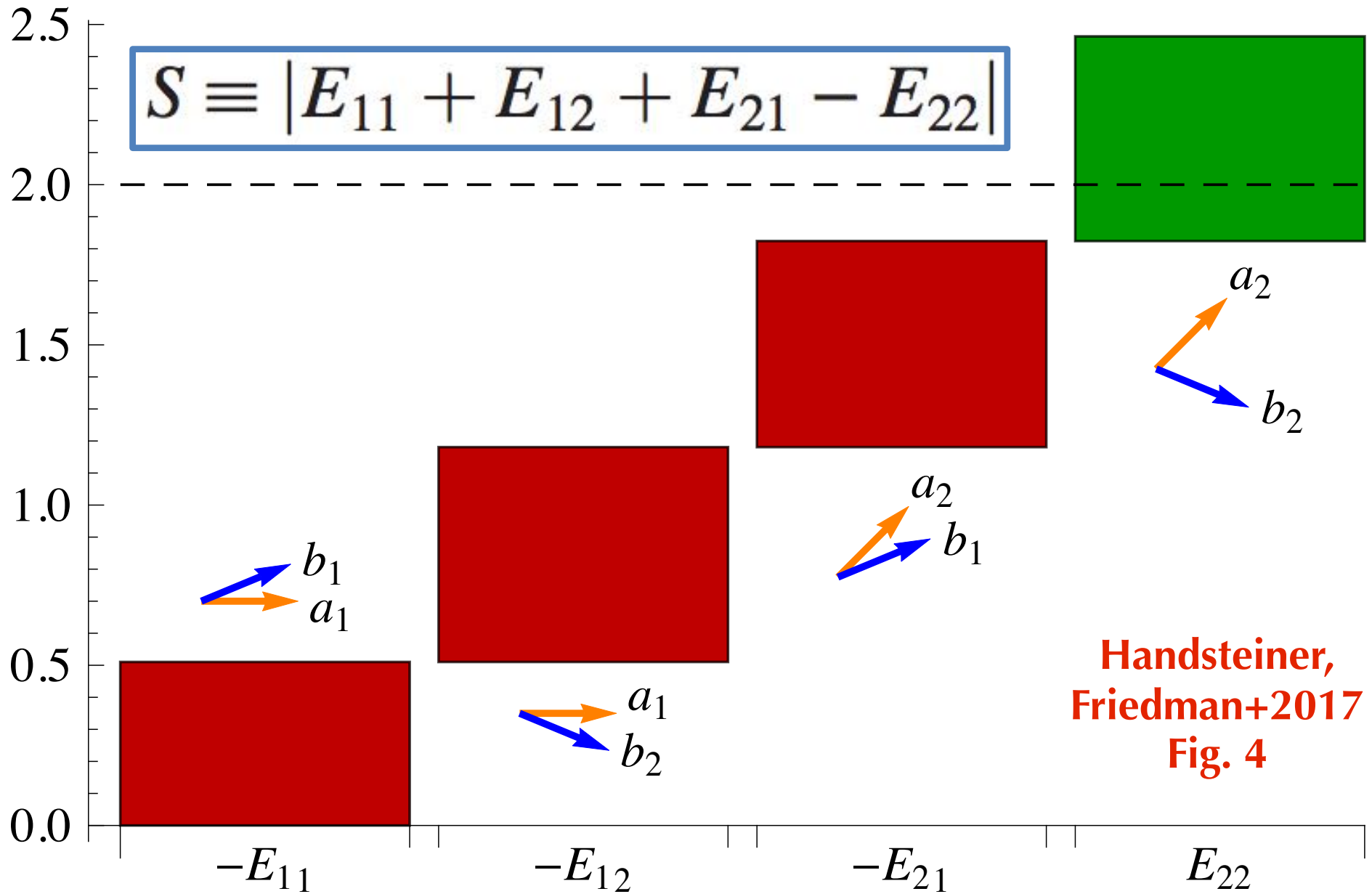
VIENNA COSMIC BELL TEST

Star Selection

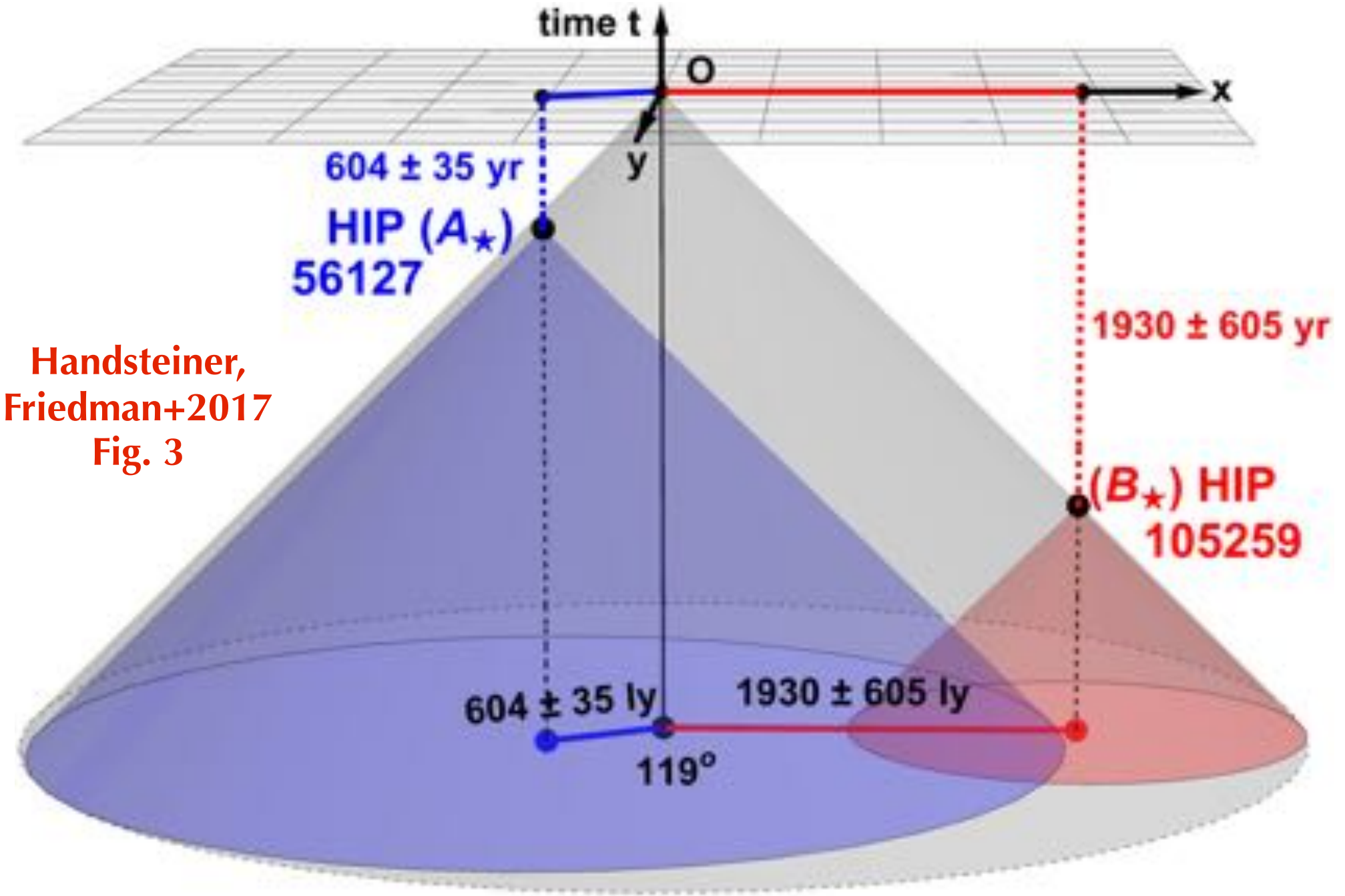


Image Credit: Jason Gallicchio

OBSERVED BELL VIOLATION



SPACE-TIME DIAGRAM: STARS



DATA ANALYSIS

“Noise Loophole”

- Need triggers by genuine cosmic photons, not local “noise” photons: atmospheric airglow, thermal dark counts, errant dichroic mirror reflections
- Conservatively allow $S=4$ for any background events, $S<2$ for cosmic photons. Accounts for bias in red/blue ports.
- Observed sufficient signal-to-noise from cosmic sources

**Highly significant Bell violation still observed:
Run 1: 7.31 sigma, Run 2: 11.93 sigma**

See Handsteiner, Friedman+2017 (Supplemental Material)

OUTLINE

1. Entanglement Tests

2. Bell's Inequality vs. Bell's Theorem

3. Loopholes / Freedom-Of-Choice Loophole

4. Cosmic Bell Test with Milky Way Stars

5. Cosmic Bell Test with Quasars

6. Future Tests

COSMIC BELL DESIGN CONCEPT

PHYSICAL REVIEW D **88**, 044038 (2013)

The shared causal pasts and futures of cosmological events

Andrew S. Friedman,^{1,*} David I. Kaiser,^{1,†} and Jason Gallicchio^{2,‡}

Friedman, Kaiser, & Gallicchio 2013a, *Phys. Rev. D*, Vol. 88, Iss. 4, id. 044038, 18 p. (arXiv:1305.3943)

Why use quasars? Brightest continuous cosmological sources.

$z > 3.65$ quasars at 180 deg have no shared causal past since inflation

PRL **112**, 110405 (2014)

PHYSICAL REVIEW LETTERS

week ending
21 MARCH 2014

Testing Bell's Inequality with Cosmic Photons: Closing the Setting-Independence Loophole

Jason Gallicchio,^{1,*} Andrew S. Friedman,^{2,†} and David I. Kaiser^{2,‡}

Gallicchio, Friedman, & Kaiser 2014, *Phys. Rev. Lett.*, Vol. 112, Issue 11, id. 110405, (arXiv:1310.3288)

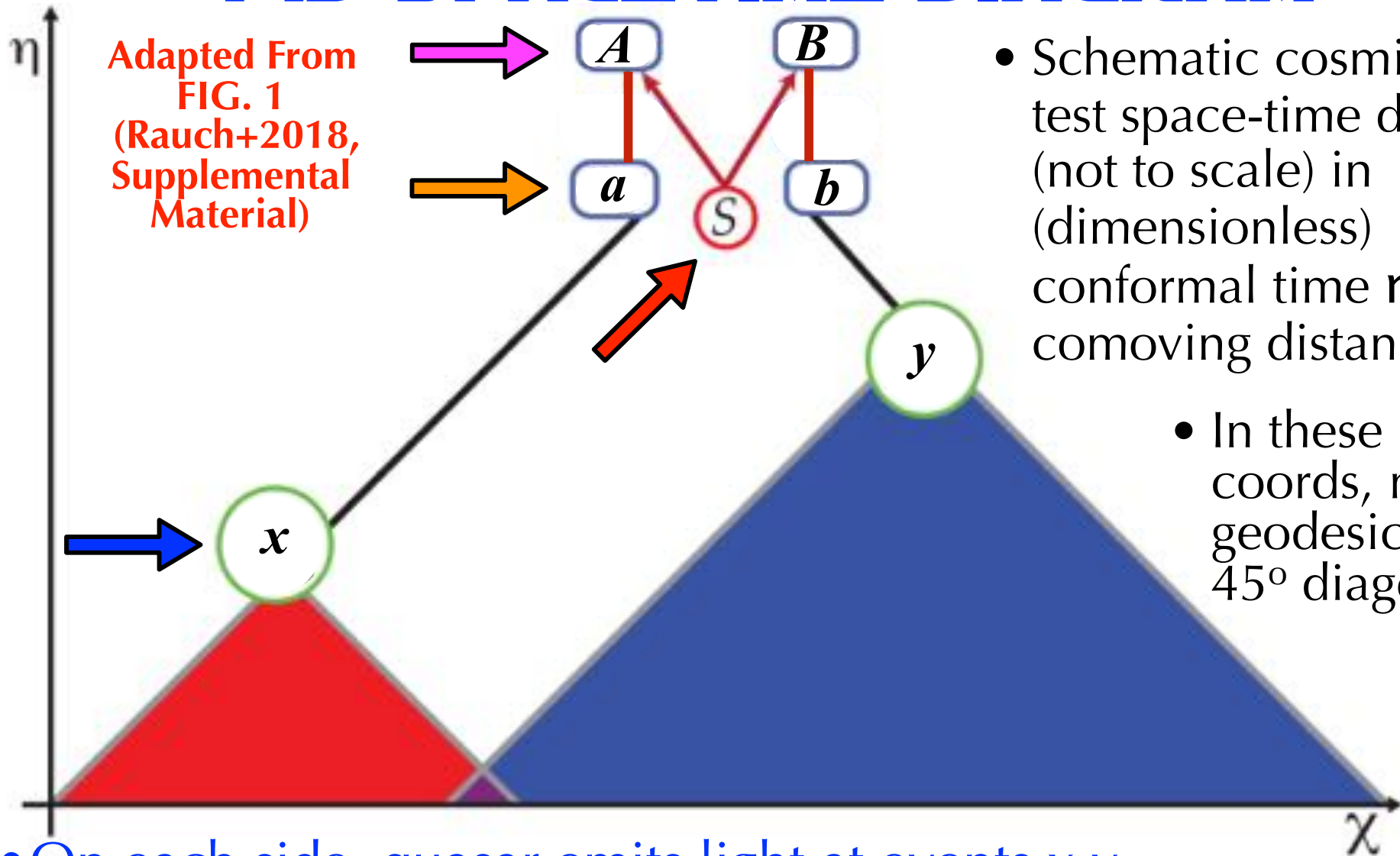
Experiment feasible with existing technology!

$z > 3.65$ quasars bright enough

CMB an intriguing possibility

1+1D SPACETIME DIAGRAM

Adapted From
FIG. 1
(Rauch+2018,
Supplemental
Material)

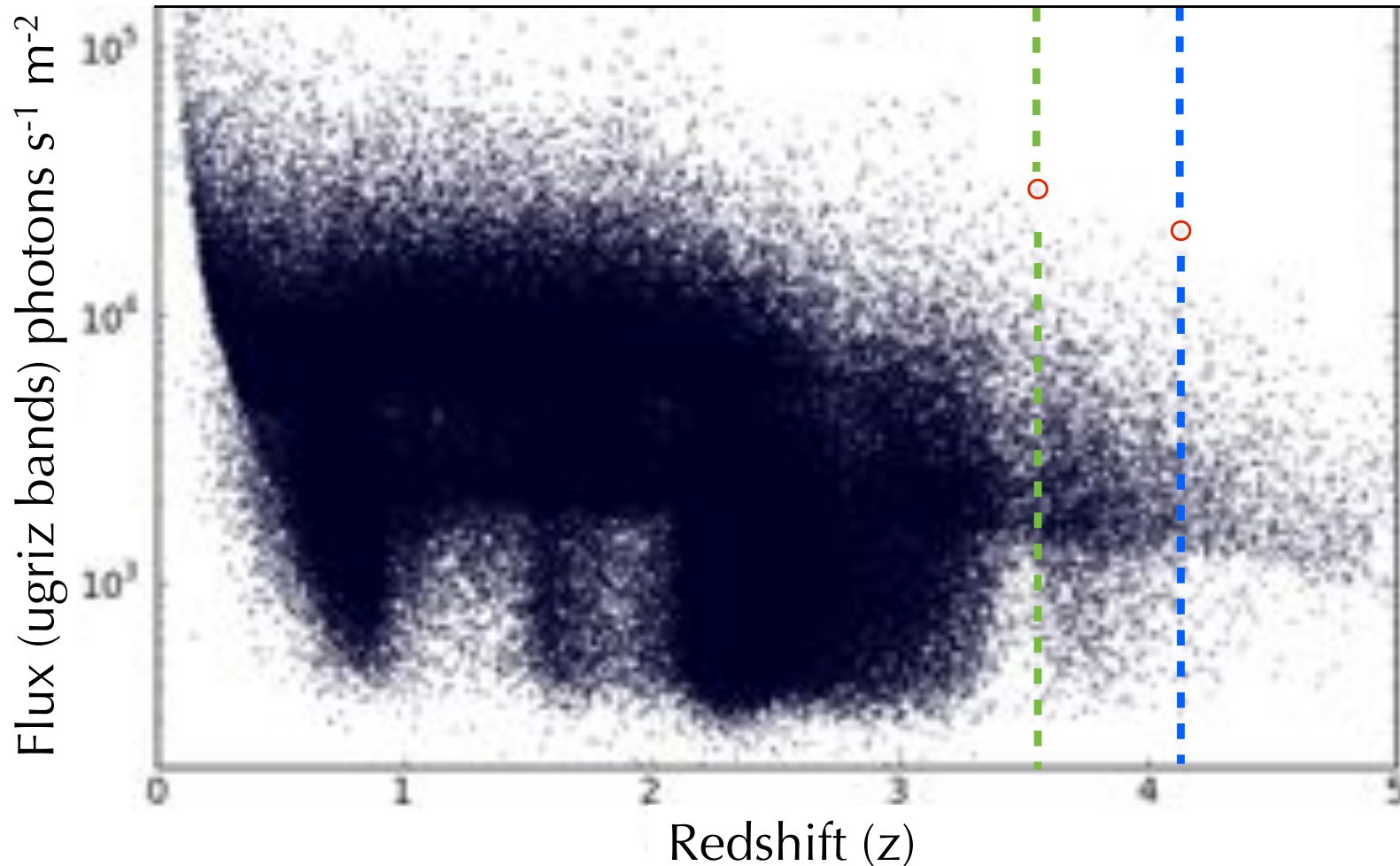


- Schematic cosmic Bell test space-time diagram (not to scale) in (dimensionless) conformal time η vs. comoving distance χ .

- In these coords, null geodesics on 45° diagonals.

- On each side, quasar emits light at events x, y
- Light received on Earth used to set detectors at events a, b
- Meanwhile, spacelike-separated from events x, y , and a, b , source S emits entangled pairs, which are measured at events A, B

QUASAR FLUX VS. REDSHIFT



Ground based
optical flux.

IR only usable
from space

Local Sky
noise!

Adapted
from Fig. 3
(GFK14)

$z \sim 3.65$: $F_{\text{Opt}} \sim 3 \times 10^4$ photons $s^{-1} m^{-2}$ **180 degrees**

$z \sim 4.13$: $F_{\text{Opt}} \sim 2 \times 10^4$ photons $s^{-1} m^{-2}$ **130 degrees**

SDSS quasars - photometric and spectroscopic redshifts

ZEILINGER GROUP EXPERIMENTS



Prof. Anton Zeilinger



COSMIC BELL TEST WITH QUASARS

PHYSICAL REVIEW LETTERS 121, 080403 (2018)

Editors' Suggestion

Rauch, D. + 2018, *Physical Review Letters*, Vol. 121, Issue 8, id. 080403 (arXiv:1808.05966)

Cosmic Bell Test Using Random Measurement Settings from High-Redshift Quasars

Dominik Rauch,^{1,2,*} Johannes Handsteiner,^{1,2} Armin Hochrainer,^{1,2} Jason Gallicchio,³ Andrew S. Friedman,⁴
Calvin Leung,^{1,2,3,5} Bo Liu,⁶ Lukas Bulla,^{1,2} Sebastian Ecker,^{1,2} Fabian Steinlechner,^{1,2} Rupert Ursin,^{1,2}
Beili Hu,³ David Leon,⁴ Chris Benn,⁷ Adriano Ghedina,⁸ Massimo Cecconi,⁸ Alan H. Guth,⁵
David I. Kaiser,^{5,†} Thomas Scheidl,^{1,2} and Anton Zeilinger^{1,2,‡}

Roque de los Muchachos Observatory on Canary Island of La Palma



Image Credit: Jason Gallicchio (Harvey Mudd)

COSMIC BELL TEST WITH QUASARS

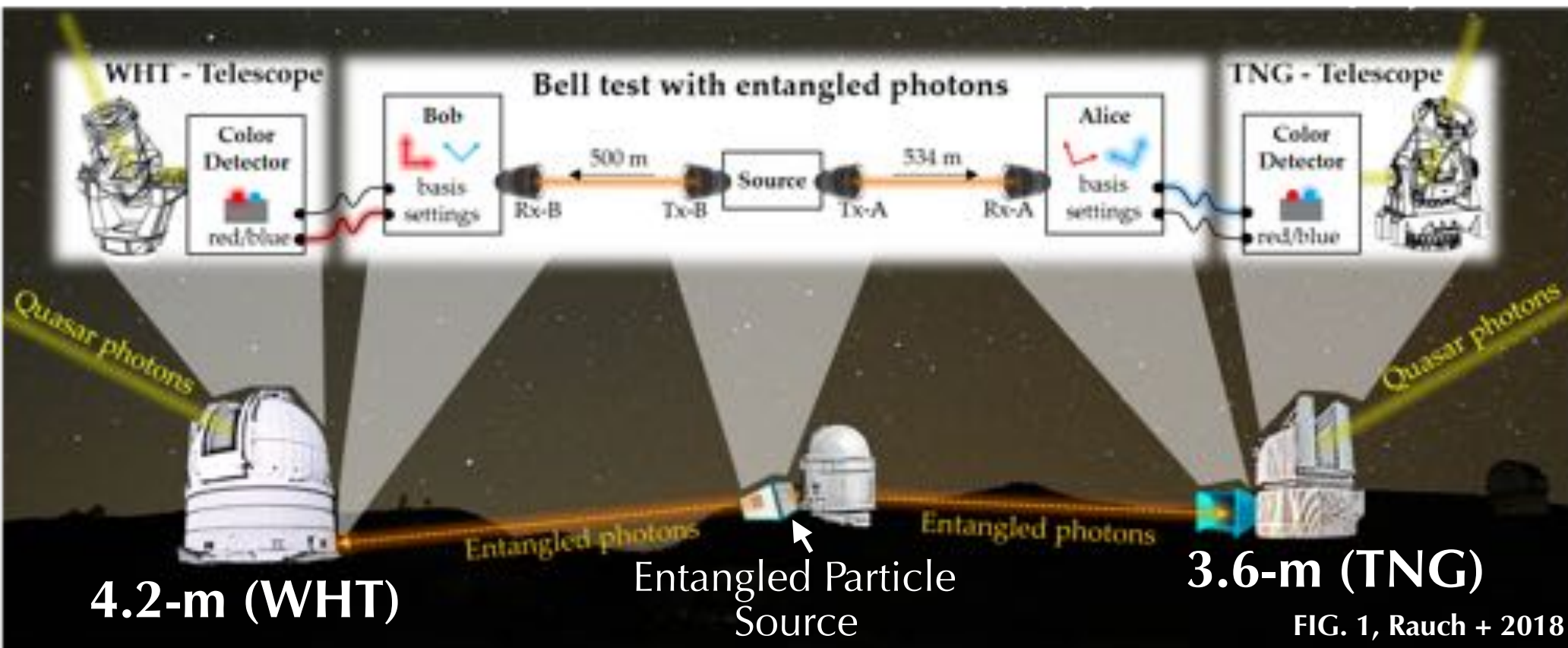
PHYSICAL REVIEW LETTERS 121, 080403 (2018)

Editors' Suggestion

Cosmic Bell Test Using Random Measurement Settings from High-Redshift Quasars

Dominik Rauch,^{1,2,*} Johannes Handsteiner,^{1,2} Armin Hochrainer,^{1,2} Jason Gallicchio,³ Andrew S. Friedman,⁴
Calvin Leung,^{1,2,3,5} Bo Liu,⁶ Lukas Bulla,^{1,2} Sebastian Ecker,^{1,2} Fabian Steinlechner,^{1,2} Rupert Ursin,^{1,2}
Beili Hu,³ David Leon,⁴ Chris Benn,⁷ Adriano Ghedina,⁸ Massimo Cecconi,⁸ Alan H. Guth,⁵
David I. Kaiser,^{5,†} Thomas Scheidl,^{1,2} and Anton Zeilinger^{1,2,‡}

Rauch, D. + 2018, *Physical Review Letters*, Vol. 121, Issue 8, id. 080403 (arXiv:1808.05966)



COSMIC BELL TEST WITH QUASARS

PHYSICAL REVIEW LETTERS 121, 080403 (2018)

Editors' Suggestion

Cosmic Bell Test Using Random Measurement Settings from High-Redshift Quasars

Dominik Rauch,^{1,2,*} Johannes Handsteiner,^{1,2} Armin Hochrainer,^{1,2} Jason Gallicchio,³ Andrew S. Friedman,⁴
 Calvin Leung,^{1,2,3,5} Bo Liu,⁶ Lukas Bulla,^{1,2} Sebastian Ecker,^{1,2} Fabian Steinlechner,^{1,2} Rupert Ursin,^{1,2}
 Beili Hu,³ David Leon,⁴ Chris Benn,⁷ Adriano Ghedina,⁸ Massimo Cecconi,⁸ Alan H. Guth,⁵
 David I. Kaiser,^{5,†} Thomas Scheidl,^{1,2} and Anton Zeilinger^{1,2,‡}

Rauch, D. + 2018, *Physical Review Letters*, Vol. 121, Issue 8, id. 080403 (arXiv:1808.05966)

Pair	Side	ID	az_k°	alt_k°	z	t_{lb} [Gyr]	τ_{valid}^k [μ s]	S_{exp}	p value	ν
1	A	QSO B0350 - 073	233	38	0.964	7.78	2.34	2.65	7.4×10^{-21}	9.3
	B	QSO J0831 + 5245	35	57	3.911	12.21	0.90			
2	A	QSO B0422 + 004	246	38	0.268	3.22	2.20	2.63	7.0×10^{-13}	7.1
	B	QSO J0831 + 5245	21	64	3.911	12.21	0.53			

Standard Deviations



FIG. 1, Rauch + 2018

2+1D SPACETIME DIAGRAM

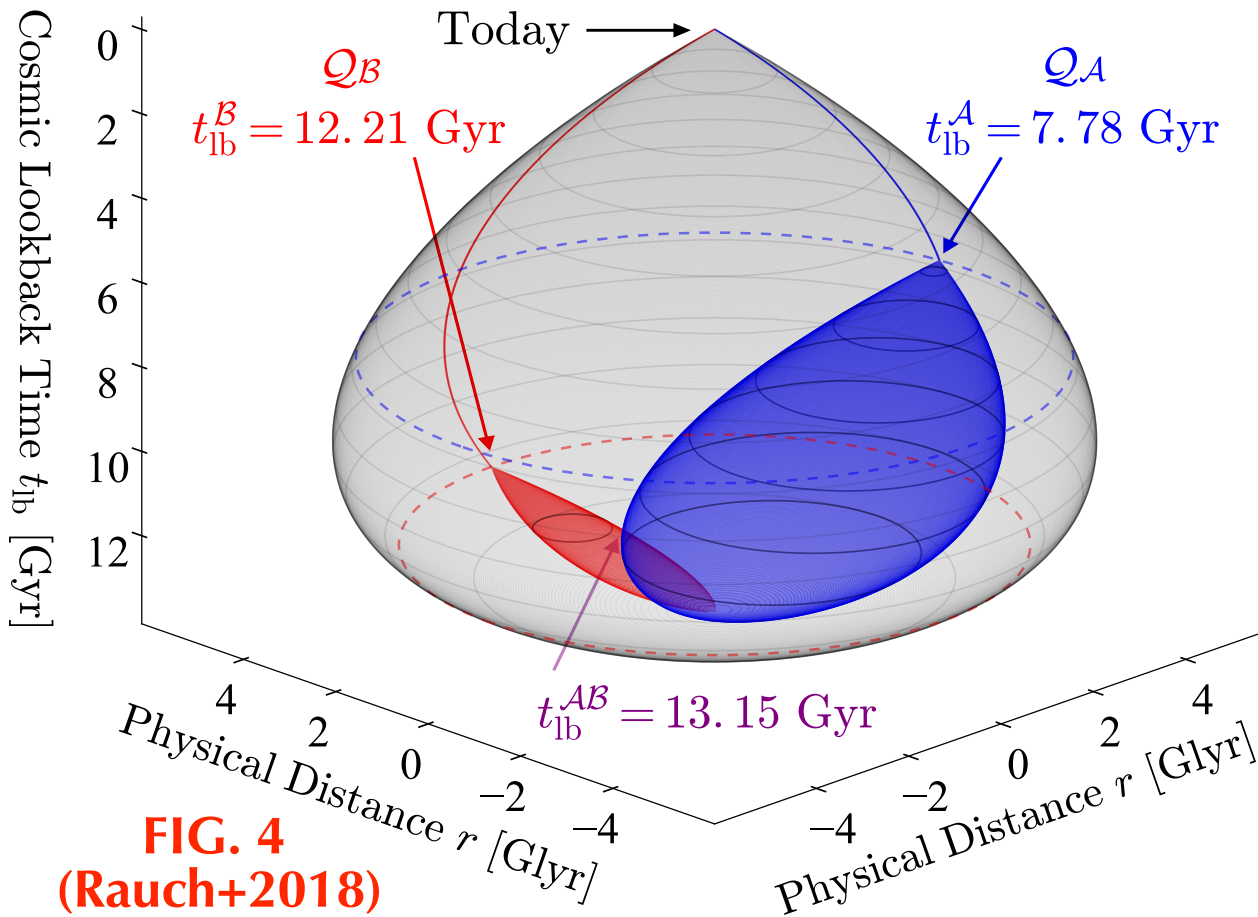


FIG. 4
(Rauch+2018)

- Past light cone of pair 1 experiment (gray)
- Quasar emission events Q_A (blue, 7.78 Gyr ago), Q_B (red, 12.21 Gyr ago)
- Past light cones overlap 13.15 Gyr ago
- Big Bang 13.80 Gyr ago
- Local-realist mechanism would need to have acted at least 7.78 Gyr ago.

• Mechanism must affect detector settings + measurement outcomes from within Q_A (blue), Q_B (red), past light cones (or their overlap), a region with only 4.0% of physical space-time volume within our past light cone.

• **Rules out 96% of space-time from causally influencing our experiment!**

$$F_{\text{excl}} = 1 - \left(\frac{V_Q^{(4)}(\tau_A, \tau_B, \alpha)}{V_{\text{exp}}^{(4)}(\tau_0)} \right) = 0.960$$

COSMIC BELL TEST WITH QUASARS

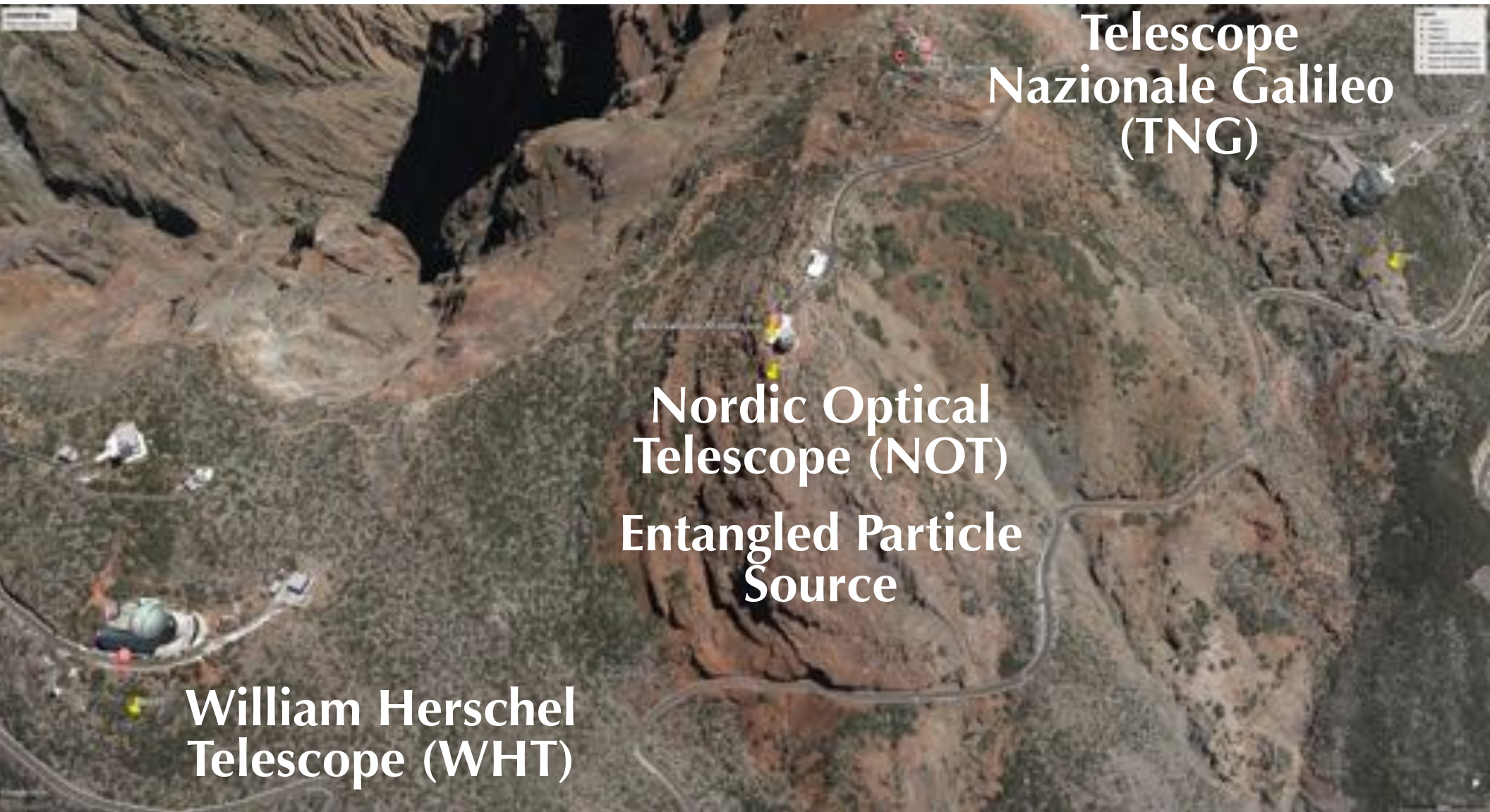


Image ©2018 DigitalGlobe (Google Earth)

LA PALMA COSMIC BELL TEST

Nordic Optical
Telescope (NOT)

Cosmic Bell Test
Entangled
Particle Source
(Shipping
Container)

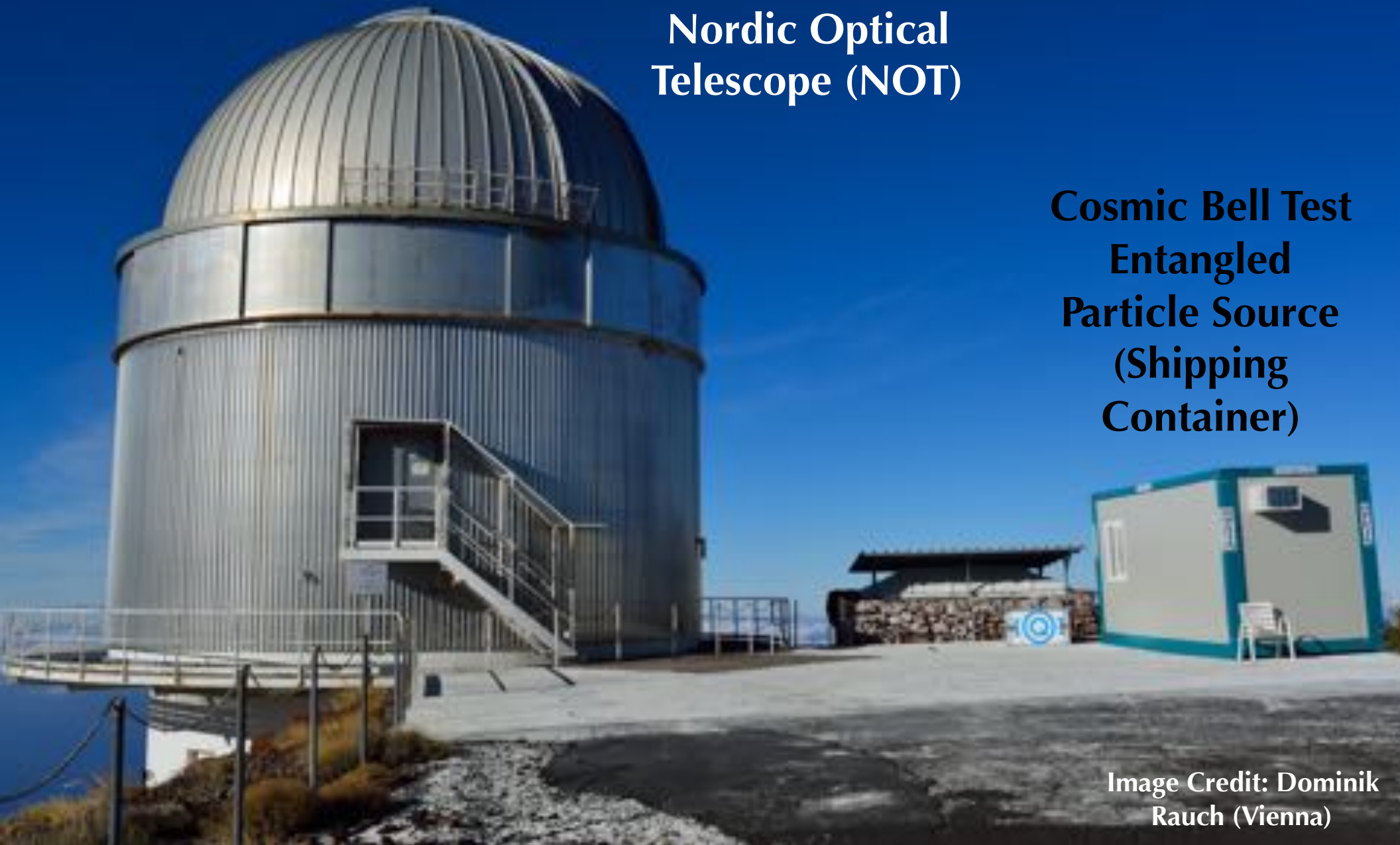


Image Credit: Dominik
Rauch (Vienna)

Nordic Optical
Telescope (NOT)

**NEAR
DISASTER!**

Cosmic Bell Test
Shipping
Container

Image Credit: Dominik
Rauch (Vienna)



Image Credit: Dominik Rauch (Vienna)

**NEAR
DISASTER!**



Image Credit: Dominik
Rauch (Vienna)

Image Credit: Dominik
Rauch (Vienna)

DISASTER AVERTED

Cosmic Bell Test
Shipping
Container



DISASTER AVERTED

Cosmic Bell Test
Shipping
Container



Image Credit: Dominik
Rauch (Vienna)

Entangled photon source fixed, reinstalled in now secured shipping container control room.

ADVENTURES IN LA PALMA

Chris Benn, Head of Astronomy,
Isaac Newton Group of
Telescopes, La Palma

Thomas Scheidl
(Vienna)

Armin Hochrainer
(Vienna)

Dominik Rauch
(Vienna)

Anton Zeilinger
(Vienna)

Image Credit: David Kaiser (MIT)

COSMIC BELL TEST (SUMMARY)

- Free space Bell test with polarization-entangled photons
- Detector settings from real-time wavelength measurements of **high-z quasar photons**, light emitted billions of years ago
- Experiment simultaneously ensures **locality**
- Assumptions: 1) fair sampling for all detected photons, 2) quasar photon wavelengths had not been selectively altered or previewed between emission and detection
- Observed statistically significant **9.3σ Bell inequality violation** (p-value $\leq 7.4 \times 10^{-21}$) for quasar pair 1.
- **Pushes back to ≥ 7.8 Gyr ago most recent time when any local-realist influences could have exploited “freedom-of-choice” loophole to engineer observed Bell violation.**
(Previous tests ~ 600 yr ago. 6 more orders of mag better!)
- **Excludes any such mechanism from 96% of the space-time volume of our experiment’s past light cone since Big Bang.**
(Previous tests $10^{-5}\%$). (~All vs. nothing!)

COSMIC BELL IN THE NEWS



SCIENTIFIC AMERICAN **Observations**

Photons, Quasars and the Possibility of Free Will

Flickers of light from the edge of the cosmos help physicists advance the idea that the future is not predetermined

By Brian Koberlein on November 21, 2018

Discover **SCIENCE FOR THE CURIOUS**

MAGAZINE | BLOGS | TOPICS | PHOTOS | PODCASTS | SEARCH

BLOGS: D-brief | The Cruz | Body Horrors | Citizen Science Salon | Dead Things | ImuGeo | InAFish | Lovelock Cyborg | Neurokaptic | Out There | Science Sushi |

D-brief

Black Holes Bolster Case For Quantum Physics' Spooky Action

By Jake Parks | August 23, 2018 1:28 pm

104

symmetry **topics** follow

Illustration by Sandbox Studio, Chicago with Corinne Mucha

The quest to test quantum entanglement

11/06/18 | By Laura Dattaro

Quantum entanglement, doubted by Einstein, has passed increasingly stringent tests.

Home | Features | Physics

Einstein was wrong: Why 'normal' physics can't explain reality

The most ambitious experiments yet show that the quantum weirdness Einstein famously hated rules the roost – not just here, but across the entire universe



PHYS ORG Nanotechnology | Physics | Earth | Astronomy & Space

Home » Physics » Quantum Physics » August 27, 2018

Physicists race to demystify Einstein's 'spooky' science

August 27, 2018 by Cynthia Dillon, University of California - San Diego

GIZMODO THE A.V. CLUB DEADSPIN JALOPNIK JEZEBEL KOTAKU LIFEHACKER SPLINTER MORE

GIZMODO VIDEO REVIEW SCIENCE ID9 FIELD GUIDE EARTHER DESIGN PALEOFUTURE

PHYSICS

'Spooky' Quantum Entanglement Confirmed Using Distant Quasars

By Ryan F. Mandelbaum

8/21/18 5:10pm | Filed to: SPOOKY ACTION AT A DISTANCE

physicsworld MENU Q

quantum

QUANTUM | RESEARCH UPDATE

Cosmic Bell test uses light from ancient quasars

21 Aug 2018 Hamish Johnston

MOTHERBOARD VICE

ENTANGLEMENT | By Daniel Oberhaus | Aug 21 2018, 7:38am

Ancient Starlight Just Helped Confirm the Reality of Quantum Entanglement

"The real estate left over for the skeptics of quantum mechanics has shrunk considerably."

SPACE

Space.com » Science & Astronomy

Ancient Quasars Provide Incredible Evidence for Quantum Entanglement

By Chelsea Gohd, Space.com Staff Writer | August 21, 2018 04:58pm ET

Astronomy

Quantum entanglement loophole quashed by quasar light

That's what happens when you let quasars decide what to measure.

By Jake Parks | Published: Thursday, August 23, 2018

Astronomy Now

The UK's best astronomy magazine

Closing a loophole in Bell's theorem with light from ancient quasars

© 21 August 2018 | Astronomy Now

MIT News

ON CAMPUS AND AROUND THE WORLD

Browse or Search

The quasar dates back to less than one billion years after the Big Bang.

Image: NASA/ESA/G. Bacon, STScI

Light from ancient quasars helps confirm quantum entanglement

Results are among the strongest evidence yet for "spooky action at a distance."

Jennifer Chu | MIT News Office August 19, 2018

COSMIC BELL IN THE NEWS

ELEMENTS
QUANTUM THEORY BY STARLIGHT
By David Kaiser February 7, 2017



HOME NEWS TECHNOLOGY SPACE PHYSICS HEALTH EARTH HUMANS LIFE TOPICS EVENTS JOBS

NEWS & TECHNOLOGY 7 February 2017
Starlight test shows quantum world has been weird for 600 years



Cosmic Test Bolsters Einstein's "Spooky Action at a Distance"
Physicists harness starlight to support the case for entanglement.
By Elizabeth Gibney, Nature magazine on February 3, 2017



By CALLA COFIELD · SPACE.COM February 13, 2017, 1:00 PM
600-year-old starlight bolsters Einstein's "spooky action" theory



TOPICS BLOGS EDITOR'S PICKS MAGAZINE
LATEST MOST
NEWS QUANTUM PHYSICS
Cosmic test confirms quantum weirdness
Distant stars as source of randomness constrains loophole in entanglement experiments
BY EMILY CONOVER 7:00AM, DECEMBER 5, 2016

600-Year-Old Starlight Bolsters Einstein's 'Spooky Action at a Distance'
By Calla Cofield, Space.com Senior Writer | February 13, 2017 01:25am ET

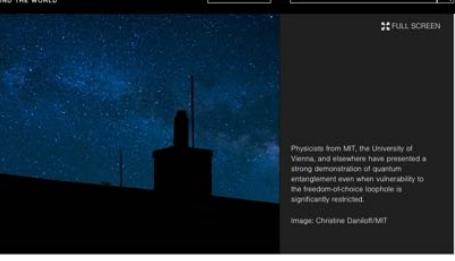


Cosmic experiment is closing another Bell test loophole
A new experiment combines nanoscale measurements and interstellar distances to demonstrate quantum nonlocality.
Andrew Grant

ANIL ANANTHASWAMY SCIENCE 09.05.16 07:00 AM
LOOPHOLES AND THE 'ANTI-REALISM' OF THE QUANTUM WORLD



NEWS | NEWS
Cosmic test backs 'quantum spookiness'
Physicists harness starlight to support the case for entanglement.
Elizabeth Gibney
02 February 2017



Stars align in test supporting "spooky action at a distance"
Physicists address loophole in tests of Bell's inequality, using 600-year-old starlight.
Jennifer Chu | MIT News Office
February 6, 2017

600-year-old starlight addressed a loophole in quantum theory
Physicists created a cosmic experiment to help prove quantum entanglement is real.
Andrew Dalton, @idolftown
02.08.17 in Space
13 Comments 1273 Shares

Science / #WhoaScience
FEB 6, 2017 @ 01:57 PM 16,737 VIEWS

Quantum Physics Tells Us Our Fate Is Not Written In The Stars

Brian Koberlein, CONTRIBUTOR
I write about the Universe as we understand it.
FULL BIO
Opinions expressed by Forbes Contributors are their own.



QUANTUM MECHANICS
Experiment Reaffirms Quantum Weirdness
Physicists are closing the door on an intriguing loophole around the quantum phenomenon Einstein called "spooky action at a distance."

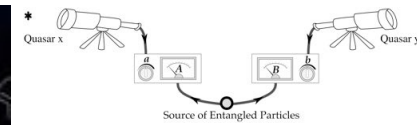
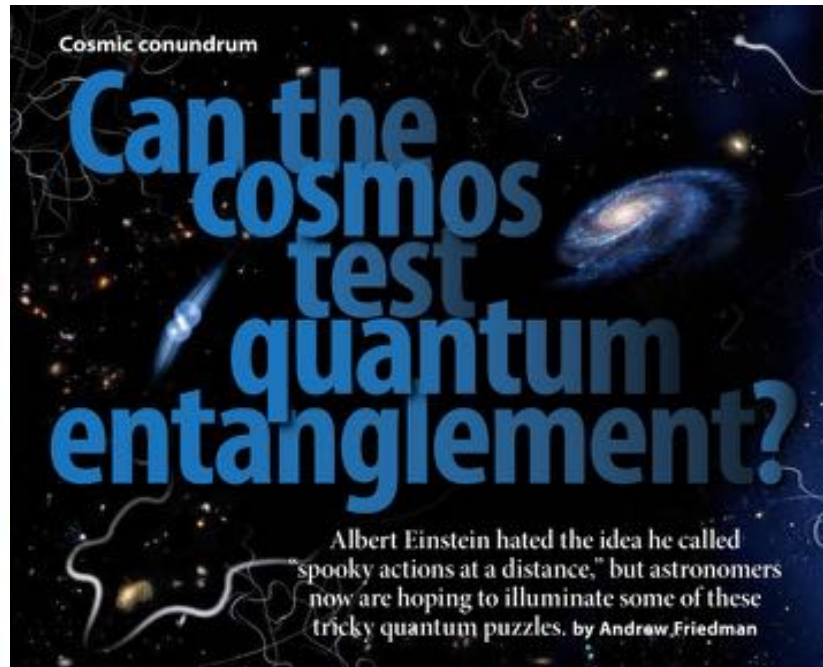
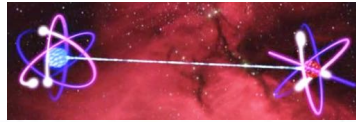


The Universe Is as Spooky as Einstein Thought
In a brilliant new experiment, physicists have confirmed one of the most mysterious laws of the cosmos.
NATALIE WOLCHOVER | FEB 10, 2017 | SCIENCE

http://web.mit.edu/asf/www/media_coverage.shtml

COSMIC BELL IN THE NEWS

MIT News
ON CAMPUS AND AROUND THE WORLD



https://asfriedman.physics.ucsd.edu/media_coverage.shtml

Closing the 'free will' loophole

MIT researchers propose using distant quasars to test Bell's theorem.

Forbes / Tech

Jennifer Chu, MIT News Office
February 20, 2014

JUN 18, 2014 @ 07:00 AM 16,359 VIEWS

Cosmic Test For Quantum Physics' Last Major Loophole



Quasar Experiment May Shed Light on Quantum Physics and Free Will

BY CHARLES Q. CHOI, INSIDE SCIENCE

QUANTUM PHYSICS
The Universe Made Me Do It? Testing "Free Will" With Distant Quasars

By Andrew Friedman on Wed, 19 Mar 2014

Sunday Review

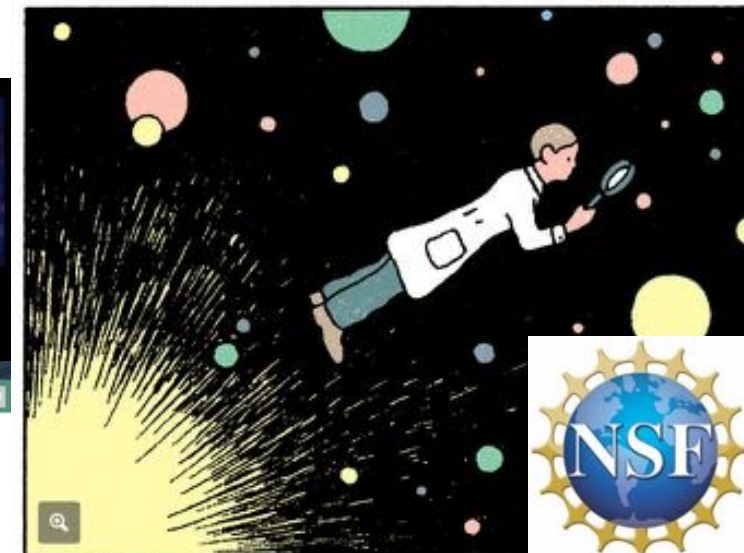
The New York Times

Is Quantum Entanglement Real?

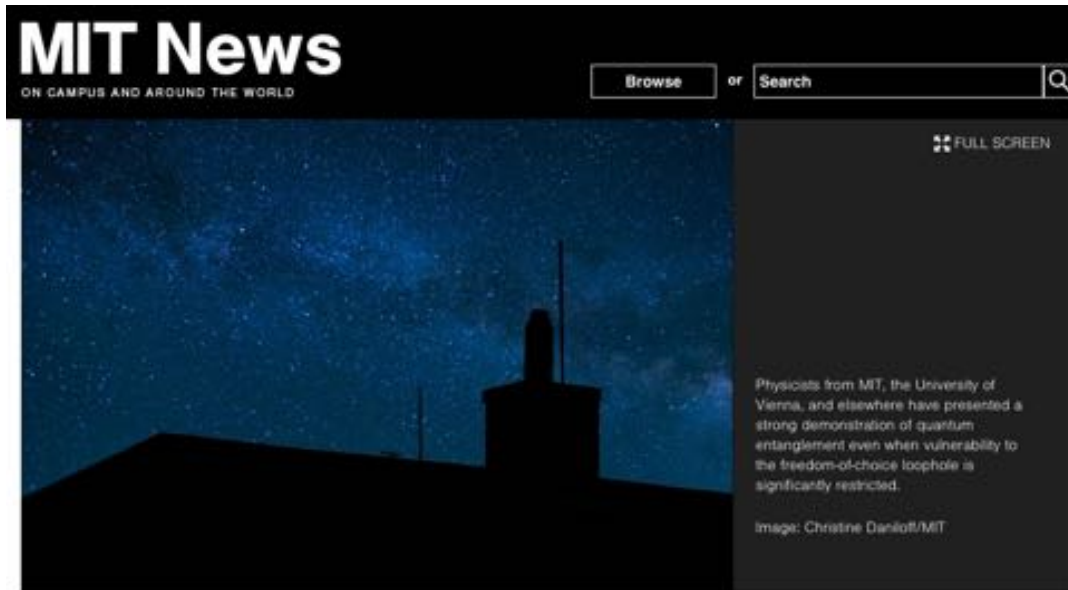
Gray Matter

NOV. 14, 2014

By DAVID KAISER



GAME OF TELEPHONE



Stars align in test supporting “spooky action at a distance”

Physicists address loophole in tests of Bell’s inequality, using 600-year-old starlight.

Jennifer Chu | MIT News Office
February 6, 2017



MIT press release

Author read actual paper!

Interviewed scientists. Fact checked!

Read press release (maybe)

Read 2nd and 3rd round articles



https://asfriedman.physics.ucsd.edu/media_coverage.shtml

OUTLINE

1. Entanglement Tests

2. Bell's Inequality vs. Bell's Theorem

3. Loopholes / Freedom-Of-Choice Loophole

4. Cosmic Bell Test with Milky Way Stars

5. Cosmic Bell Test with Quasars

6. Future Tests

BIG BELL TEST

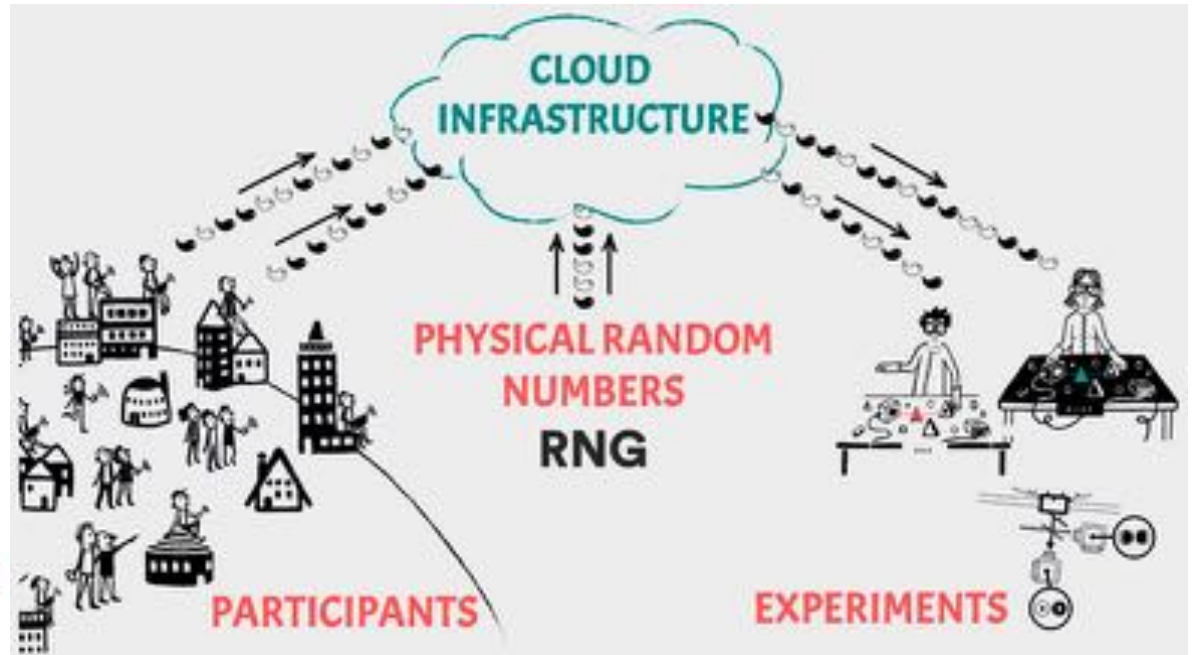


Letter | Published: 09 May 2018

Challenging local realism with human choices

The BIG Bell Test Collaboration

Nature 557, 212–216 (2018)



12 labs in 11 countries on 5 continents, plus 10^5 “Bellster” volunteers who produced 10^8 (quasi) random 0’s and 1’s

DETECTION LOOPHOLE PROGRESS

Editors' Suggestion

PHYSICAL REVIEW LETTERS 121, 080404 (2018)

Test of Local Realism into the Past without Detection and Locality Loopholes

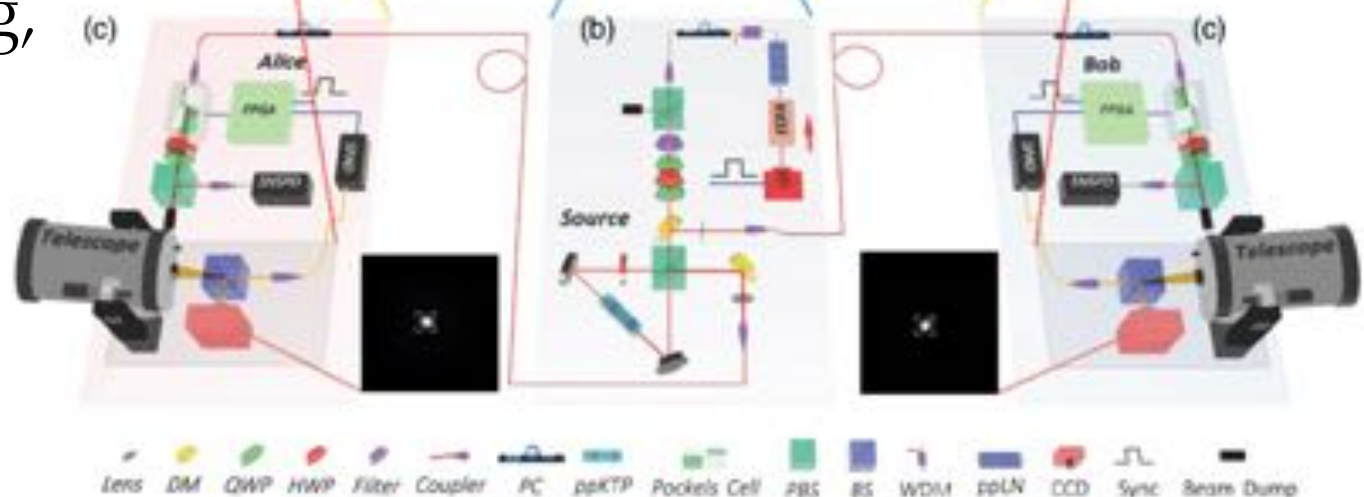
Ming-Han Li,^{1,2} Cheng Wu,^{1,2} Yanbao Zhang,³ Wen-Zhao Liu,^{1,2} Bing Bai,^{1,2} Yang Liu,^{1,2} Weijun Zhang,⁴ Qi Zhao,⁵ Hao Li,⁴ Zhen Wang,⁴ Lixing You,⁴ W. J. Munro,³ Juan Yin,^{1,2} Jun Zhang,^{1,2} Cheng-Zhi Peng,^{1,2} Xiongfeng Ma,⁵ Qiang Zhang,^{1,2} Jingyun Fan,^{1,2} and Jian-Wei Pan^{1,2}

Progress in closing detection loophole in a cosmic Bell test

Closed locality and fair sampling, *and* constrained freedom-of-choice to ~11 years ago.



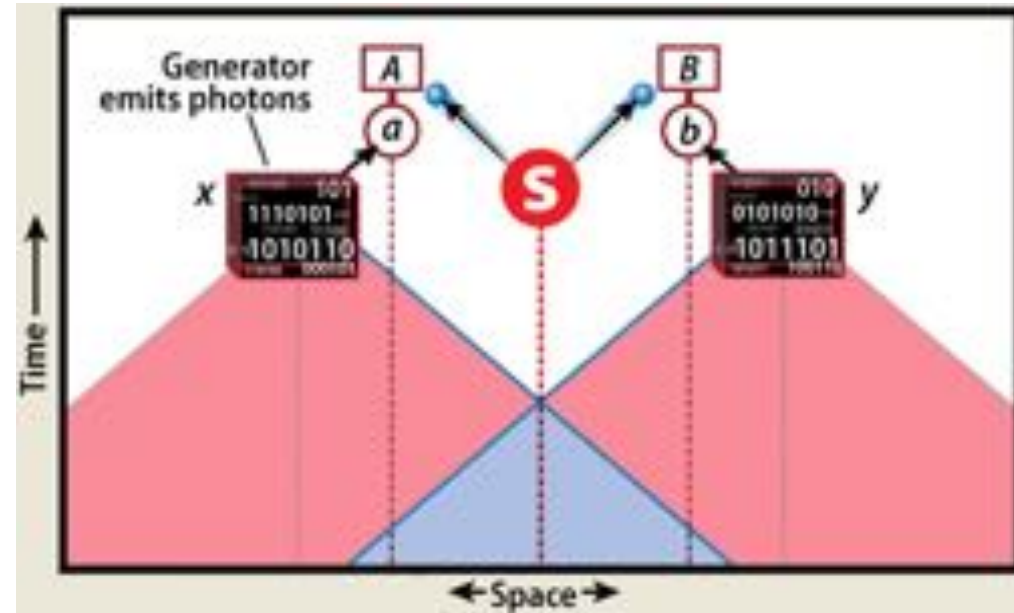
Jian-Wei Pan



Li et al., 1808.07653

SPACE-TIME DIAGRAMMS

Standard Bell Test



Past light cones from random number generators overlap milliseconds before test.

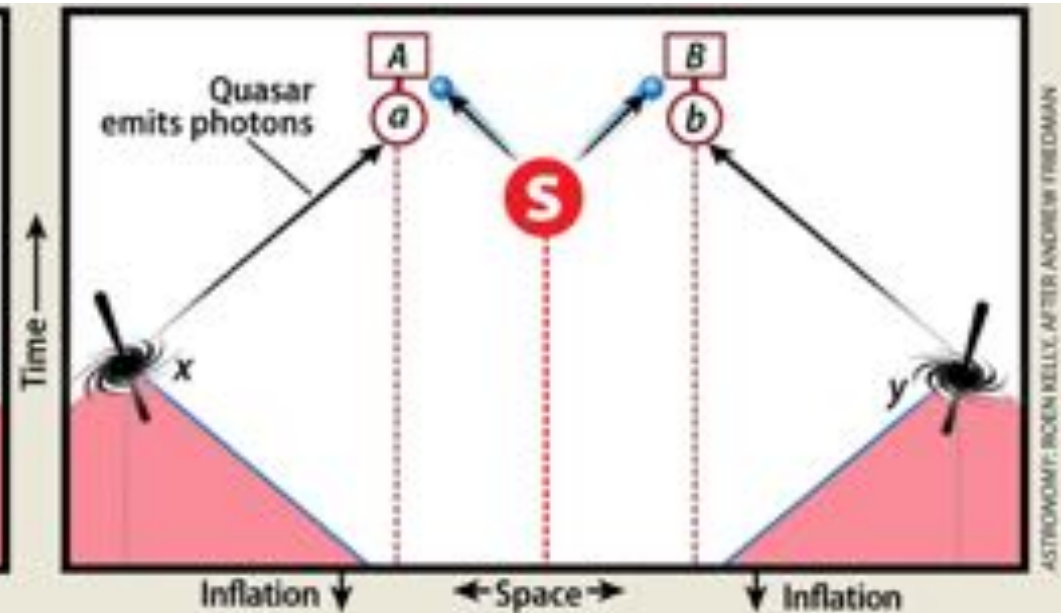
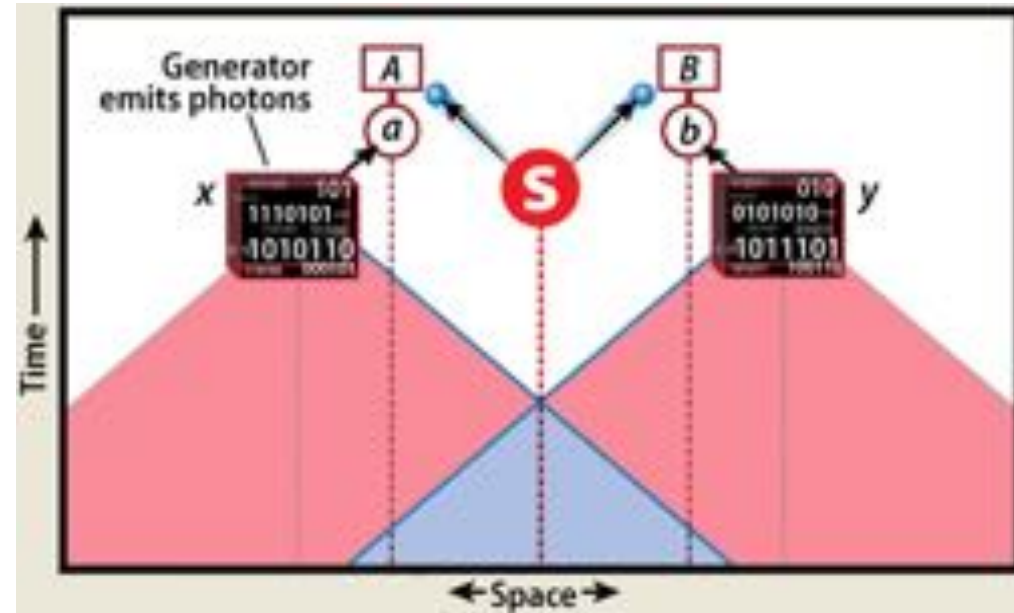


Adapted from: Friedman, Kaiser, & Gallicchio 2013a, *Phys. Rev. D*, Vol. 88, Iss. 4, id. 044038, 18 p. (arXiv:1305.3943)

SPACE-TIME DIAGRAM

Standard Bell Test

Cosmic Bell Test

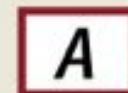


Past light cones from random number generators overlap milliseconds before test.

Past light cones from quasars don't overlap since big bang, 13.8 billion years ago.



Source of entangled particles



Measurement outcomes



Quasar



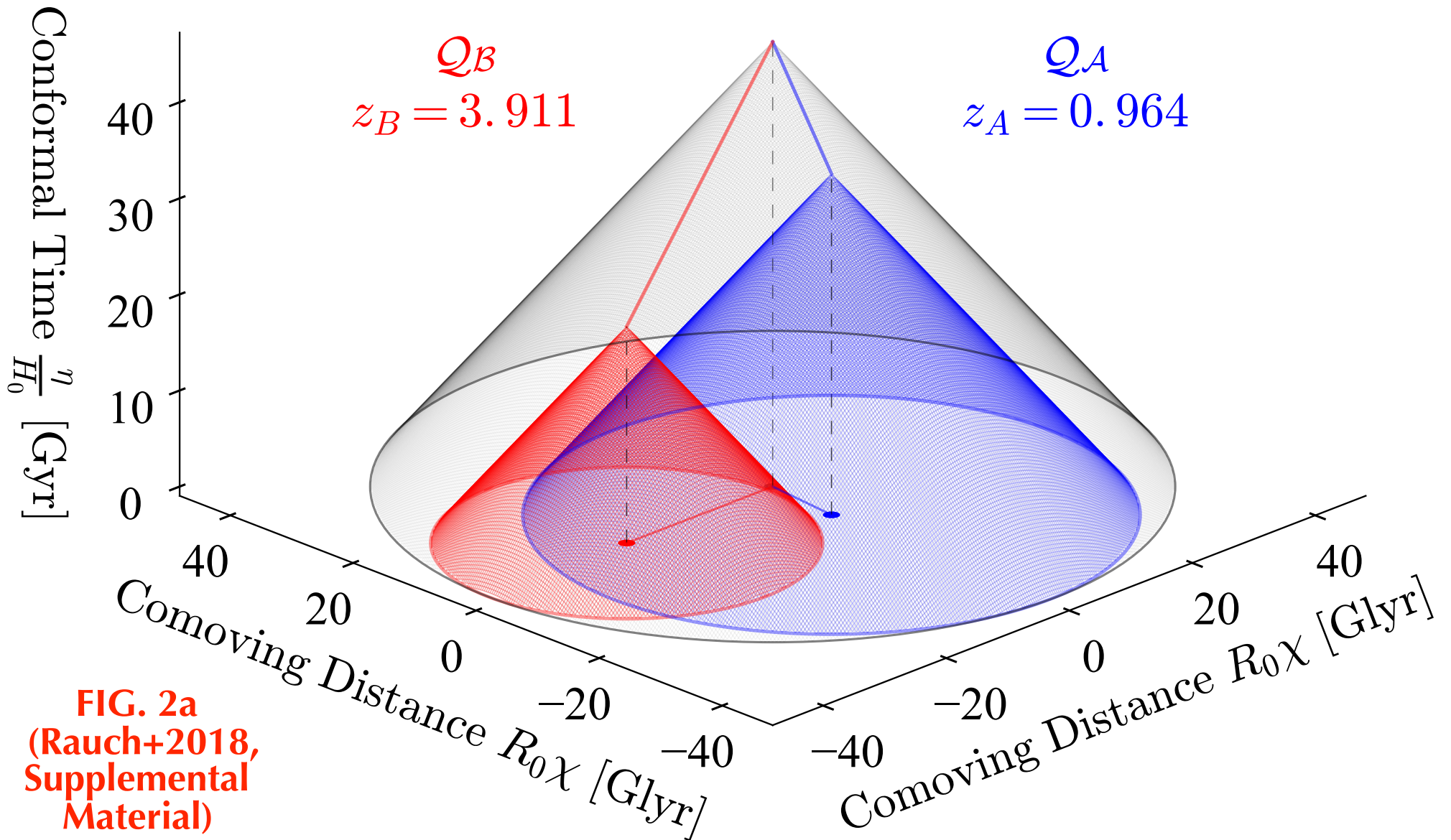
Random-number generator



Detectors set

Adapted from: Friedman, Kaiser, & Gallicchio 2013a, *Phys. Rev. D*, Vol. 88, Iss. 4, id. 044038, 18 p. (arXiv:1305.3943)

2+1D CONFORMAL SPACETIME DIAGRAM



La Palma cosmic Bell test didn't completely remove causal overlap

FUTURE COSMIC BELL TESTS

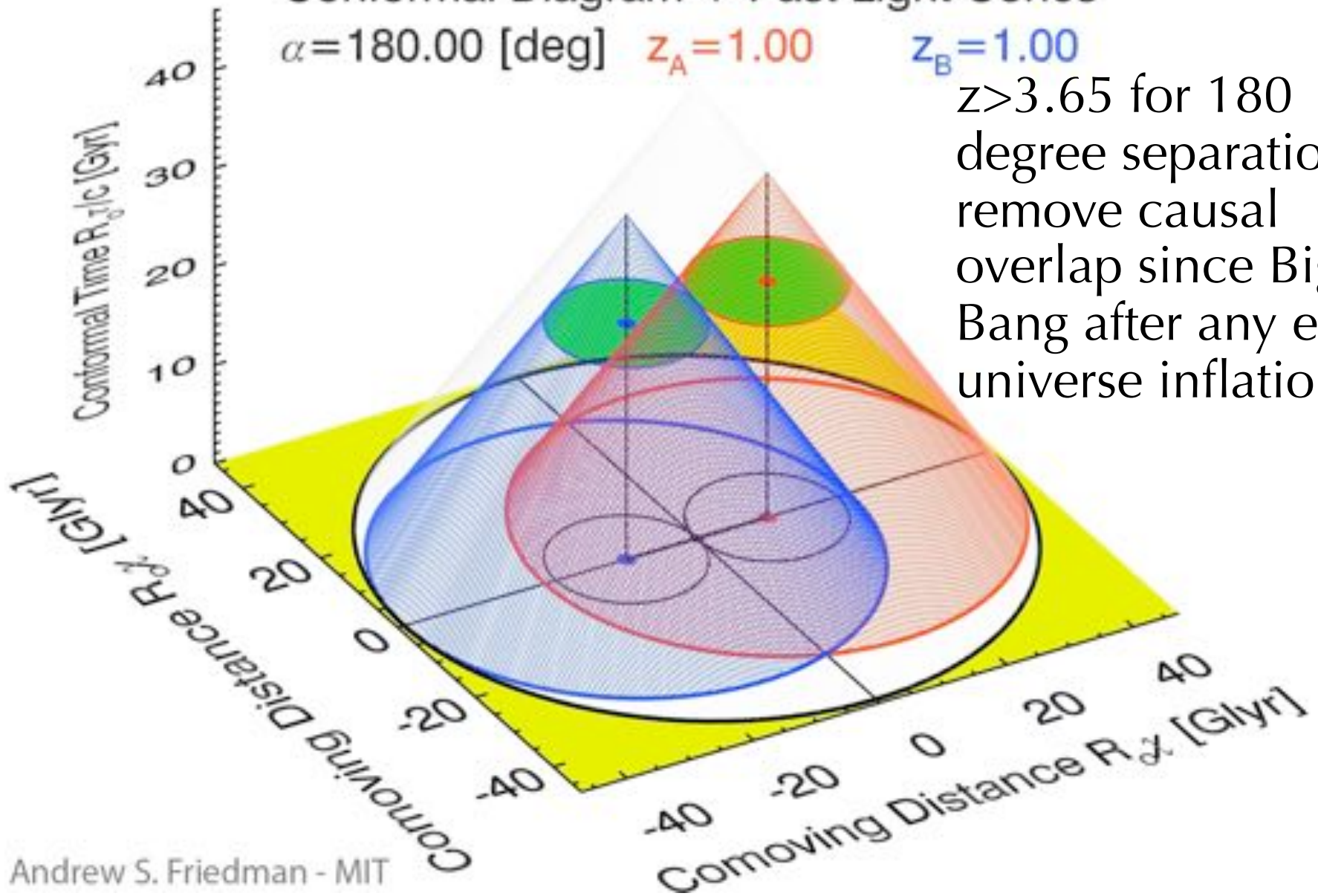
Conformal Diagram + Past Light Cones

$\alpha = 180.00$ [deg]

$z_A = 1.00$

$z_B = 1.00$

$z > 3.65$ for 180 degree separation to remove causal overlap since Big Bang after any early universe inflation



Andrew S. Friedman - MIT

NO SHARED CAUSAL PAST

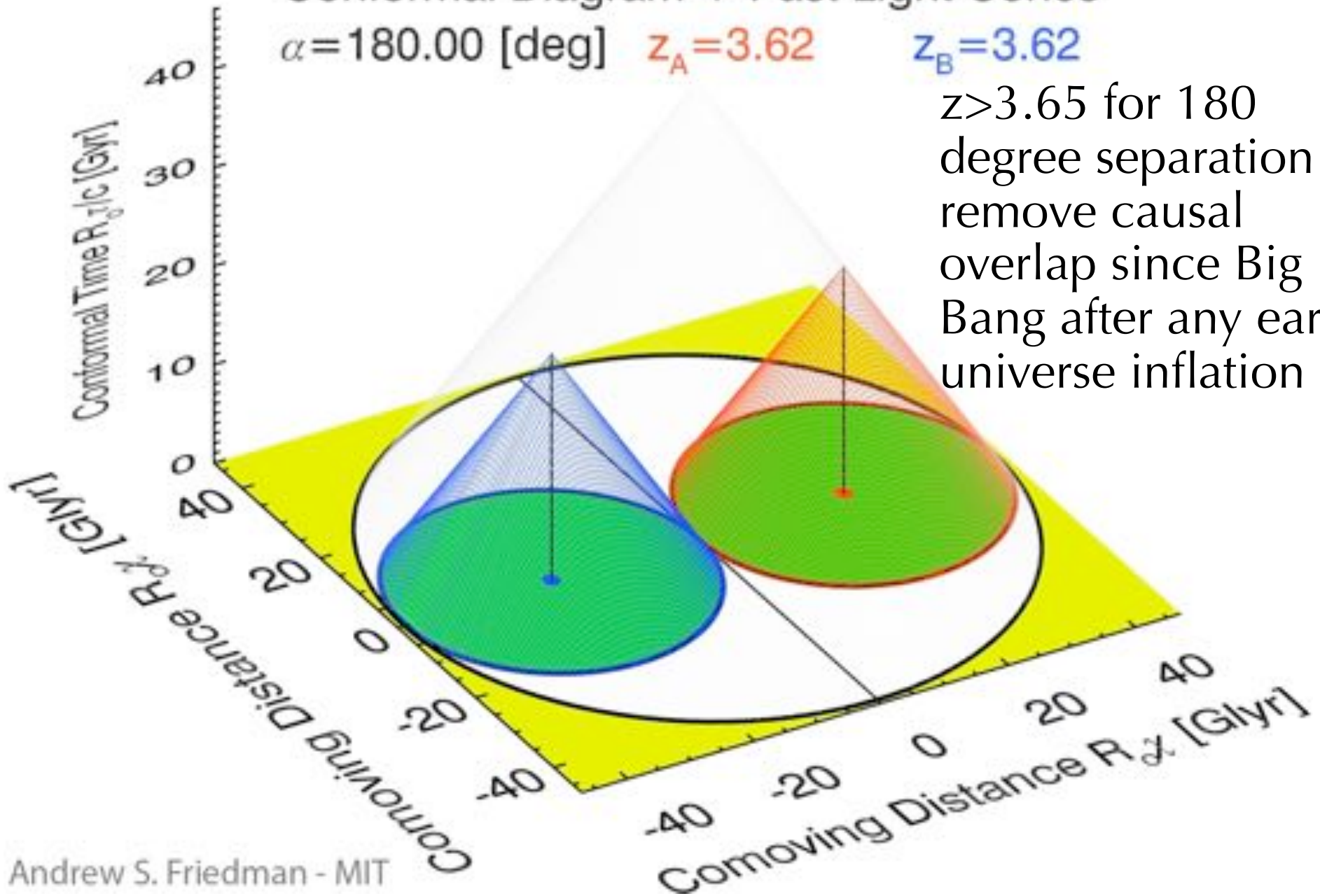
Conformal Diagram + Past Light Cones

$\alpha = 180.00$ [deg]

$z_A = 3.62$

$z_B = 3.62$

$z > 3.65$ for 180 degree separation to remove causal overlap since Big Bang after any early universe inflation



Andrew S. Friedman - MIT

NO SHARED CAUSAL PAST

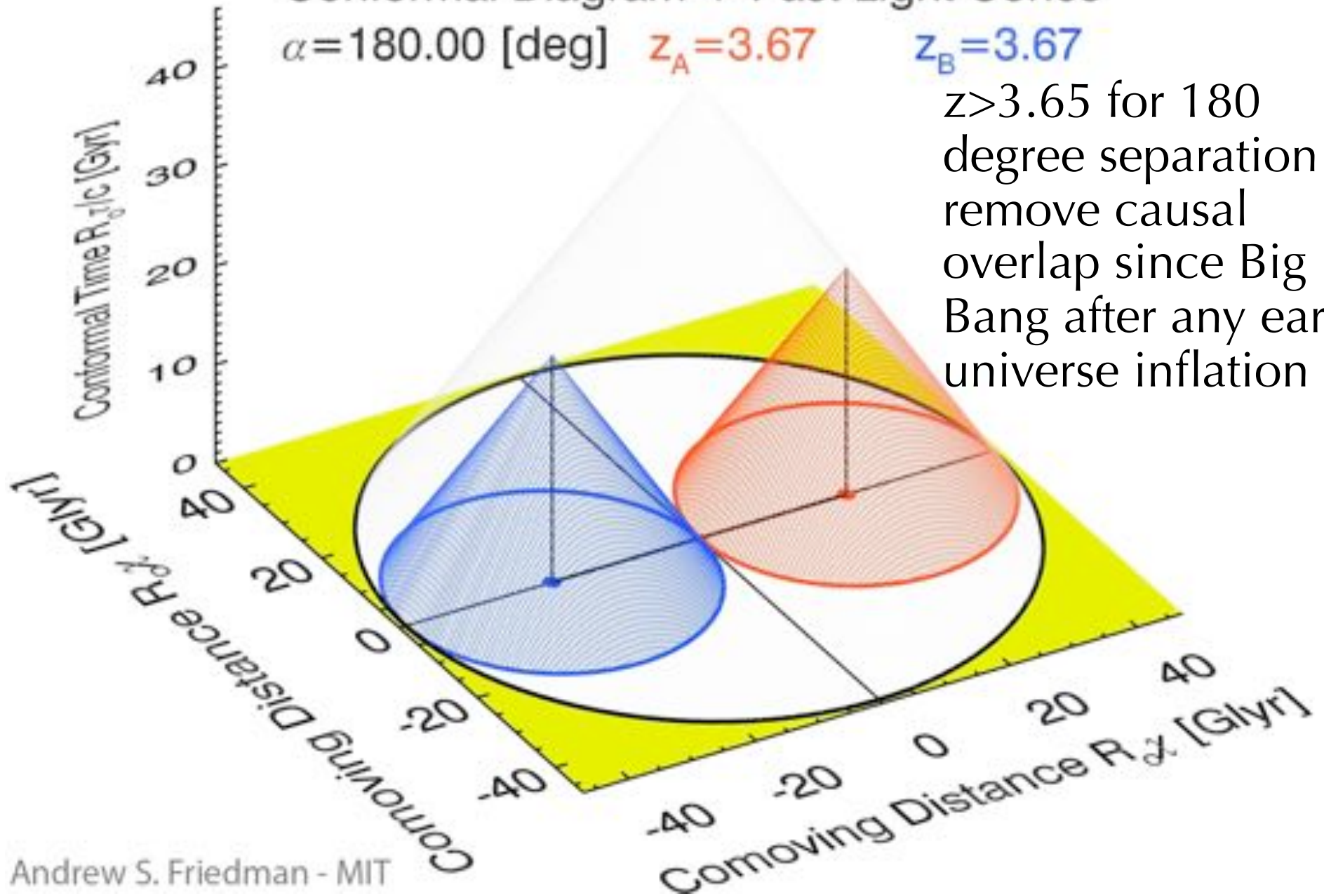
Conformal Diagram + Past Light Cones

$\alpha = 180.00$ [deg]

$z_A = 3.67$

$z_B = 3.67$

$z > 3.65$ for 180 degree separation to remove causal overlap since Big Bang after any early universe inflation



Andrew S. Friedman - MIT

2 OR MORE COSMIC SOURCES

2 (EPR) or 3 or more (GHZ) entangled particles

Greenberger, Horne, Zeilinger 1989; Greenberger+1990; Mermin 1990

Each cosmic source pair in set of $N=2, 3$ (or > 3) satisfies pairwise constraints from **Friedman+2013** for no shared causal past since the Big Bang at the end of

	Angular Separation	Redshift
2-Way Space	180°	$z > 3.65$
2-Way Ground	130°	$z > 4.13$
3-Way Space	120°	$z > 4.37$
3-Way Ground	105°	$z > 4.89$

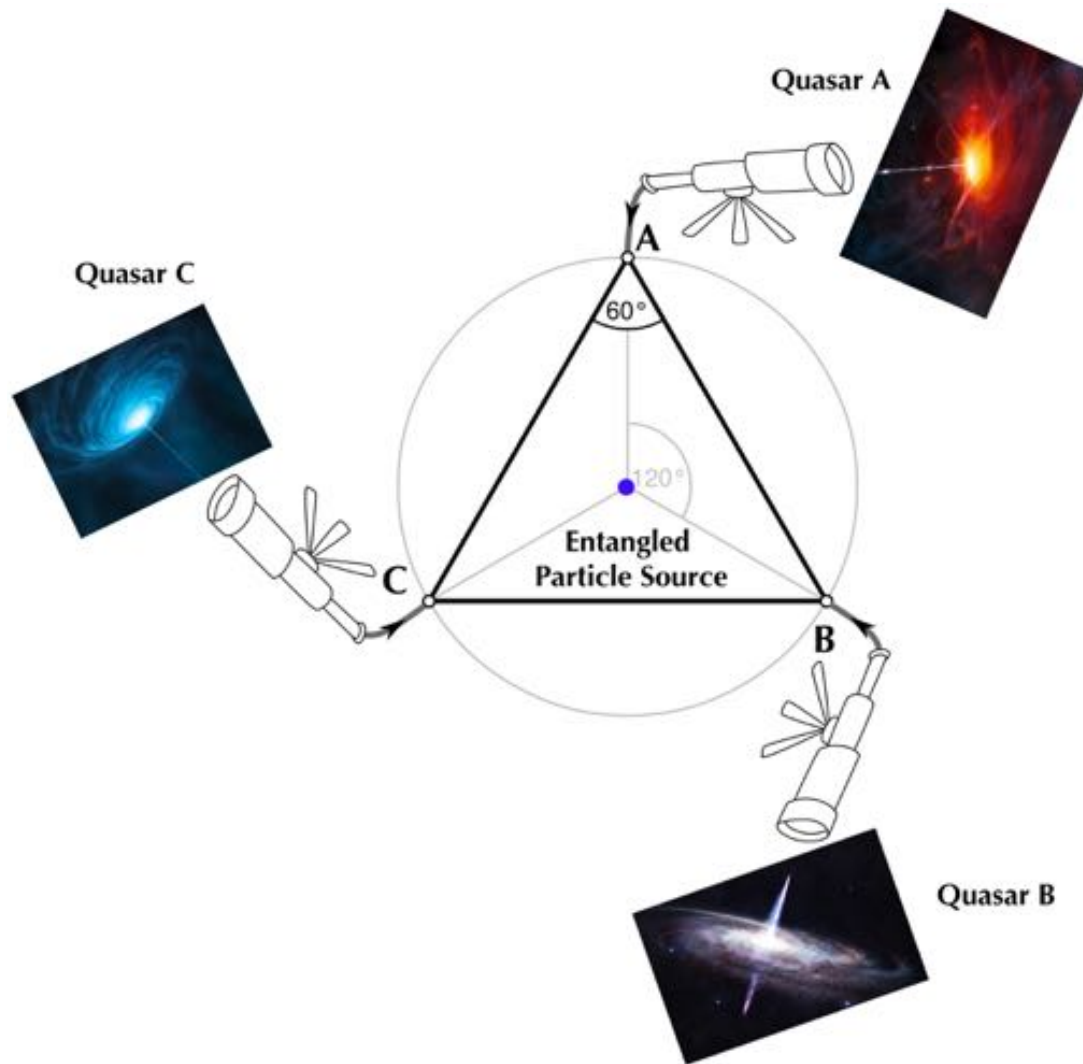
Gallicchio, Friedman, & Kaiser 2014; Friedman+2019 *in prep.*

GHZ WITH QUASARS?

3+ particles, Bell's theorem without inequalities

QM, Local realism give opposite answers to yes/no questions

Greenberger, Horne, Zeilinger 1989; Greenberger+1990; Mermin 1990



Will be difficult to remove all pairwise causal overlap in a ground based test.

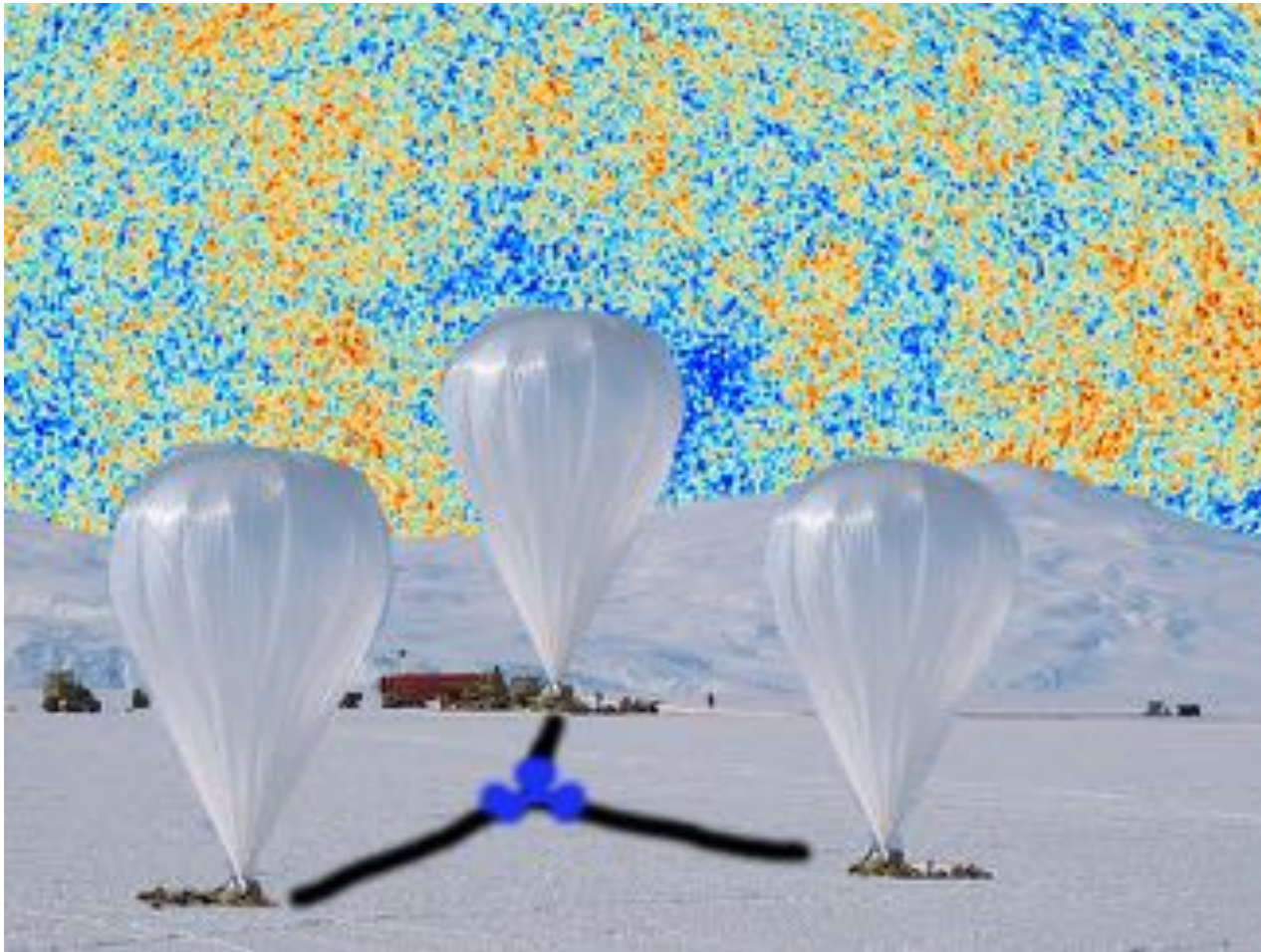
But GHZ pilot test with stars and with brighter, moderate redshift quasars is technologically possible

GHZ WITH CMB?

3+ particles, Bell's theorem without inequalities

QM, Local realism give opposite answers to yes/no questions

Greenberger, Horne, Zeilinger 1989; Greenberger+1990; Mermin 1990



Easy! Pick 3 CMB patches, each separated by 2.3°

Hard! Local noise dominates from ground (**GFK14**)

Noise loophole limits better than 2-particle Bell test (**Hall 2011**)

Balloon based test in Antarctica?

POSSIBLE OUTCOMES

Future 2-quasar Cosmic Bell tests with no causal overlap

3 CMB patch or 3-quasar GHZ test from ground, balloon, or space

Safe Bet

Bell or GHZ/Mermin inequalities always violated.
Strengthen evidence for quantum theory.

Rule out alternative theories, progressively close freedom-of-choice loophole as much as possible.

Longshot

Experimental results depends on which cosmic sources we look at. Maybe Bell's limit is not violated for very distant sources.

Perhaps experimenter's lack complete freedom!



COSMIC BELL PUBLICATIONS

Cosmic Bell Test Using Random Measurement Settings from High-Redshift Quasars, Rauch, D., Handsteiner, J., Hochrainer, A., Gallicchio, J., Friedman, A.S. + 2018, *Physical Review Letters*, Vol. 121, Issue 8, id. 080403 ([arXiv:1808.05966](#) | [PDF](#)) ([DOI](#)) ([Supplemental Material](#)) [Editors' Suggestion]

Astronomical Random Numbers for Quantum Foundations Experiments, Leung, C., Brown, A., Nguyen, H., Friedman, A.S., Kaiser, D.I., and Gallicchio, J., 2018, *Physical Review A*, Vol. 97, Issue 4, id. 042120 ([arXiv:1706.02276](#)) ([DOI](#)) [Featured in Physics]

Cosmic Bell Test: Measurement Settings from Milky Way Stars, Handsteiner, J., Friedman, A.S. + 2017, *Physical Review Letters*, Vol. 118, Issue 6, id. 060401, ([arXiv:1611.06985](#) | [PDF](#)) ([DOI](#)) ([Supplemental Material](#)) [Featured in Physics, Editors' Suggestion]

Testing Bell's Inequality with Cosmic Photons: Closing the Setting-Independence Loophole, Gallicchio, J., Friedman, A.S., and Kaiser, D.I. 2014, *Physical Review Letters*, Vol. 112, Issue 11, id. 110405, 5 pp. ([arXiv:1310.3288](#)) ([DOI](#))

The Shared Causal Pasts and Futures of Cosmological Events, Friedman, A.S., Kaiser, D.I., and Gallicchio, J. 2013, *Physical Review D*, Vol. 88, Issue 4, id. 044038, 18 pp. ([arXiv:1305.3943](#)) ([DOI](#))

Can the Cosmos Test Quantum Entanglement?, Friedman, A.S. 2014, *Astronomy*, Vol. 42, Issue 10, October 2014, pg. 28-33 [[PDF](#)]

The Universe Made Me Do It? Testing "Free Will" With Distant Quasars, Friedman, A.S., *NOVA, The Nature of Reality*, PBS, WGBH Boston, March 19, 2014 [[PDF](#)]

11/30/2018 San Diego State University, Physics and Astronomy Colloquium

REFERENCES

- Ade+2013, *A & A sub.*, (arXiv:1303.5076)
- Aspect+1982, *Phys. Rev. Lett.*, Vol. 49, 25, December 20, p. 1804-1807
- Barret & Gisin 2011, *Phys. Rev. Lett.*, vol. 106, 10, id. 100406
- Bell 1964, *Physics* Vol. 1, No. 3, p. 195-200, *Physics Publishing Co.*
- Bell+1989, *Speakable & Unspeakable in Quantum Mechanics*, *American Journal of Phys.*, Vol. 57, Issue 6, p. 567
- Clauser, Horne, Shimony, & Holt 1969, PRL 23, 880
- Clauser & Shimony 1978, Rep. Prog. Phys. 41, 1881
- Christensen+2013, *Phys. Rev. Lett.*, 111, 120406
- Einstein, Podolsky, & Rosen 1935, *Phys. Rev.*, Vol. 47, 10, p. 777-780
- Freedman & Clauser 1972, *Phys. Rev. Lett.*, vol. 28, 14, p. 938-941
- Friedman, Kaiser, & Gallicchio 2013a, *Phys. Rev. D*, Vol. 88, Iss. 4, id. 044038, 18 p. (arXiv:1305.3943)
- Gallicchio, Friedman, & Kaiser 2014=GFK14, *Phys. Rev. Lett.*, Vol. 112, Issue 11, id. 110405, (arXiv:1310.3288)
- Giustina+2013, *Nature*, Vol. 497, 7448, p. 227-230
- Greenberger, Horne, & Zeilinger 1989, "Going Beyond Bell's Theorem", in *Bell's Theorem, Quantum Theory, and Conceptions of the Universe*, Ed. M. Kafatos, Kluwer Academic, Dordrecht, The Netherlands, p. 73-76
- Greenberger+1990, *American Journal of Physics*, Volume 58, Issue 12, pp. 1131-1143
- Guth 1981, *Phys. Rev. D*, Vol. 23, 2, p. 347-356
- Guth & Kaiser 2005, *Science*, Vol. 307, 5711, p. 884-890
- Handsteiner, J., Friedman, A.S. + 2017, *Physical Review Letters*, Vol. 118, Issue 6, id. 060401, (arXiv:1611.06985)
- Hall 2010, *Phys. Rev. Lett.*, vol. 105, 25, id. 250404
- Hall 2011, *Phys. Rev. A*, vol. 84, 2, id. 022102
- Leung, C.+2018, *Physical Review A*, Vol. 97, Issue 4, id. 042120 (arXiv:1706.02276)
- Maudlin 1994, "Quantum Non-Locality and Relativity", Wiley-Blackwell; 1st edition
- Mermin 1990, *American Journal of Physics*, Volume 58, Issue 8, pp. 731-734
- Rauch, D.+ 2018, *Physical Review Letters*, Vol. 121, Issue 8, id. 080403 (arXiv:1808.05966)
- t'Hooft 2007, (arXiv:quant-ph/0701097)
- Scheidl+2010, *PNAS*, 107, 46, p. 19708-19713
- Weih's+1998, *Phys. Rev. Lett.*, Vol. 81, 23, Dec 7, p. 5039-5043
- Zeilinger 2010, "Dance of the Photons", Farrar, Straus & Giroux; 1st Ed.