

Digital Information
Binary Coding
Digital Sampling
CDs and DVDs

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Binary Numbers for Digital Representation

- Though we use base-10 for numbers, this isn't the only choice
 - base 2: 1's and 0's only
 - 0 → 00000000 (8-bit)
 - 1 → 00000001 (8-bit)
 - 2 → 00000010 (8-bit)
 - 3 → 00000011 (8-bit) (1 + 2)
 - 4 → 00000100 (8-bit)
 - 127 → 01111111 (8-bit) (1 + 2 + 4 + 8 + 16 + 32 + 64)
- If we want to represent negative numbers, we *could* make up some rule, like:
 - 127 → 11111111 (8-bit): first bit indicates negative

This is one of several representations (esp. for handling negative numbers)

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How Binary Works:

- Instead of a 1's place, 10's place, 100's place, etc.
 - which is 10^0 place, 10^1 place, 10^2 place, etc. for base ten
- We have a 1's place, 2's place, 4's place, 8's place...
 - which is 2^0 place, 2^1 place, 2^2 place, 2^3 place, etc. for base 2
- In decimal, when we get to 9, we've run out of digits
 - next number is 10
 - after 9999 is 10000
- In binary, when we get to 1, we've run out of digits
 - next number is 10
 - after 1111 is 10000

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Example: Binary to Decimal

- What is 01101011 in decimal?
 - we'll ignore our special rule for negative here: only positive
- By analogy, what does 642 mean?
 - 6 100's plus 4 10's plus two 1's
 - $6 \times 10^2 + 4 \times 10^1 + 2 \times 10^0$
- 01101011 is then:
 - $0 \times 2^7 + 1 \times 2^6 + 1 \times 2^5 + 0 \times 2^4 + 1 \times 2^3 + 0 \times 2^2 + 1 \times 2^1 + 1 \times 2^0$
 - $0 \times 128 + 1 \times 64 + 1 \times 32 + 0 \times 16 + 1 \times 8 + 0 \times 4 + 1 \times 2 + 1 \times 1$
 - $64 + 32 + 8 + 2 + 1$
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Example: Decimal to Binary

- Let's represent 99 in binary form
- By analogy, in decimal, we don't need any thousand's-place, or hundred's place (these are zero)
 - meaning you could write 99 as 00000000000099
 - 99 is not big enough to need any of the higher places
- We do need 9 10's, then left over with 9
- If in binary, we have a 128's place, 64's place, etc.:
 - then 99 doesn't need a 128: 128 is too big
 - but does need a 64, leaving 35
 - remaining 35 needs a 32, leaving 3
 - remaining 3 does not need a 16, 8, or 4, but does need 2, leaving 1
 - remaining 1 needs one 1 to finish out
- So result is 01100011

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How many digits/bits

- 3 decimal digits lets you represent 0–999
 - 1000, or 10^3 possible numbers
- Generally, N decimal digits gets you $0-10^N - 1$
 - 10^N possibilities
- 3 binary digits gets you 0–7 ($2^3 = 8$ possibilities)
 - 000, 001, 010, 011, 100, 101, 110, 111
- In general, N binary bits gets you 2^N possibilities
- In a similar way, a license plate with a format
 - ABC 123 has $(26) \times (26) \times (26) \times (10) \times (10) \times (10) = 17,576,000$ possibilities
 - enough for most states

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Adding Binary Numbers

- Same rules apply as for adding decimal numbers:
 - when you exceed the available digits, you “carry” extra digits
- Let's add 46 and 77
 - 00101110 and 01001101
$$\begin{array}{r} 0101110 \\ + 01001101 \\ \hline 01111011 \end{array}$$

$00101110 = 2 + 4 + 8 + 32 = 46$
 $+ 01001101 = 1 + 4 + 8 + 64 = 77$
 $01111011 = 1 + 2 + 8 + 16 + 32 + 64 = 123$

- The rules are:
- $0 + 0 = 00$
- $1 + 0 = 0 + 1 = 01$
- $1 + 1 = 10$ (0, carry a 1)
- $1 + 1 + 1 = 11$ (1, carry a 1)

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Digital Representation of Analog Quantities

- Sound waveform can be *digitized*
- At uniform time intervals, amplitude of waveform is characterized by an integer number
 - 8-bit (from –127 to 127) (low resolution)
 - 12-bit (from –2047 to 2047)
 - 16-bit (from –32767 to 32767) (high resolution)

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Digital Audio Formats

- Must sample at greater than twice the highest frequency you want represented in the sound clip
 - Human hearing sensitive up to 20,000 Hz
 - CDs recorded at 44,100 Hz (44,100 samples/second)
- Must have reasonable resolution (fine-grain)
 - 8-bit has only 42 dB dynamic range (sounds grainy)
 - 16-bit has 84 dB range: CD's at 16-bit
- Stereo is usually desirable (separate waveforms)
- CD's then read $2 \times 44,100 \times 16 = 1.4$ million bits/sec
 - in familiar units: 1411.2 kbits/sec
 - 74-minute disc then contains 6.26 billion bits = 783 MB
 - one second of CD music contains 176 kB of data
 - data CDs use some space for error correction: get 650 MB

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All that information on one little disk?!

- CDs are truly marvels of technology
- Data density: 6.26 billion bits over πR^2 area
 - $R = 60 \text{ mm} = 60,000 \mu\text{m} \rightarrow A = 11$ billion μm^2
 - 0.55 bits per micron-squared: 1.34 micron square per bit
- Bits arranged in spiral pattern from center out
 - Outer 40 mm / 1.34 micron $\rightarrow 30,000$ wraps
 - 74 minutes = 4440 seconds $\rightarrow 6\text{--}7$ revolutions per second
- Bits \leftrightarrow Pits pressed into aluminum foil
 - Pit \rightarrow digital 0; No pit \rightarrow digital 1

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Arrangement on the CD

- Pits are arranged in long spiral, starting at center and spiraling outward toward edge
- Are pits bits? Are non-pits bits?



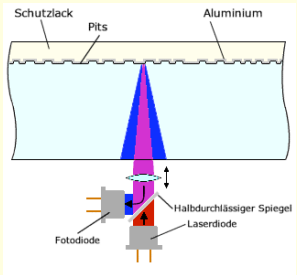


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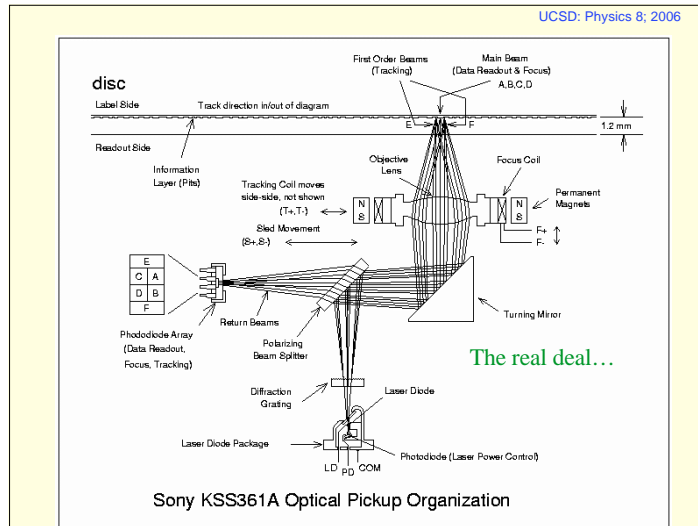
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Read-out Mechanism

- Laser focuses onto pit surface
- Reflected light collected by photodiode (light sensor)
- Intensity of light interpreted as bit value of zero or one
- Separate side beams ensure tracking
 - “ride” between adjacent tracks on spiral
- polarizing beamsplitter separates outgoing from incoming light



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Optical Requirements

- **Pits are *small!***
 - micron size; laser wavelength is $0.78 \mu\text{m}$
- **Cannot (quantum-mechanically) focus laser smaller than its wavelength**
 - and have to work real hard to come close

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Noise Immunity

- **Can scan ahead (array of detectors)**
 - Build up multiple-reads of same block
- **Hardly affected by dust/scratches on surface**
 - beam is 0.5–1 mm in diameter as it encounters disk
 - most of beam sees around dust or scratch

pits actually only $0.11 \mu\text{m}$ deep

1.2 mm

0.8 mm

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Why All the Fuss? Why Go Digital?

- **Sound, images are inherently analog:**
 - sound is continuously variable pressure amplitude
 - light is represented by a continuum of wavelengths and brightnesses
- **But reproduction of these with high fidelity would require precision recording, precision equipment**
 - exact height of ridges in vinyl record groove critical
 - exact signal strength of radio wave determines brightness of pixel on TV screen
 - device-dependent interpretation (tuning) subject to variation
- **Digital information means unambiguous data**
 - CD pit is either there or it isn't
 - Electronically handled as 0V or 5V: easy to distinguish
 - everybody has access to the full-precision information

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DVD Technology

- **DVDs make many leaps beyond CD technology:**
 - 0.65 μm laser: the better to see you with
 - smaller pits \rightarrow greater data density
 - can be double-sided
 - double layer in some cases (4 layers altogether)
 - **data compression**
- **Density of pits up 4 times, plus 4 surfaces**
 - holds 16 times as much as CD
- **Data compression extremely important for DVDs**
 - avoids redundant coding of repetitive information (e.g., still scenes, backdrops, even music waveforms)

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Data Compression

- **Two types: *lossless* and *lossy***
- **Lossless examples**
 - zipped computer files, GIF images, stuffit
 - can **completely** recover **error-free** version of original
 - toy example: 00010001000100010001000100010001
 - notice 0001 appears 8 times
 - *could* represent as 10000001, where first 4 bits indicate number of times repeated, second four is repeated pattern
 - compresses 32 bits into 8, or 4:1 compression ratio
- **Lossy examples**
 - JPEG, MP3, MPEG
 - look/sound okay, mostly by cheating
 - ignoring information they eye/ear is not adept at noticing
 - irrecoverable errors introduced into data

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Audio Compression

- **Imagine a perfect sine wave**
 - could represent this as lots of samples (many bits)
 - or could represent as frequency and amplitude (few bits)
- **MP3 recipe**
 - break into short bits (576 samples)
 - shorter (192) when something abrupt is happening
 - characterize frequencies and amplitudes present
 - represent as fewer numbers of bits
 - if one frequency dominates, can ignore the rest
 - ear's limitation allows us to do this
 - achieve compression of about 11:1

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References & Assignments

- **References:**
 - How CDs work: <http://electronics.howstuffworks.com/cd.htm>
 - DVDs: <http://electronics.howstuffworks.com/dvd.htm>
 - MP3: <http://computer.howstuffworks.com/mp3.htm>
 - also: <http://en.wikipedia.org/wiki/Mp3>
 - <http://computer.howstuffworks.com/file-compression.htm>
 - iPod: <http://electronics.howstuffworks.com/ipod.htm>
- **Assignments**
 - HW4, due 5/11: 11.E.16, 11.E.19, 12.E.13, 12.E.14, 12.E.15, 12.E.16, 12.E.17; **plus 6 additional required questions** accessed through assignments page on website

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